



# Investigation of ORR and OER Mechanisms by Co- and Fe-doped Silicon Nanocages (Si<sub>48</sub> and Si<sub>60</sub>) and Co- and Fe-doped Silicon Nanotubes (SiNT(5, 0) and SiNT(6, 0)) as Acceptable Catalysts

Diana Katherine Campoverde Santos<sup>1</sup> · Mohammed Ahmed Mustafa<sup>2</sup> · Pooja Bansal<sup>3,4</sup> · Harpreet Kaur<sup>5,6</sup> · Mahamedha Deorari<sup>7</sup> · Farag M. A. Altalbawy<sup>8,9</sup> · Dheyaa Yahaia Alhameedi<sup>10</sup> · Mahmood Hasen shuhata Alubiady<sup>11</sup> · Ahmed Muzahem Al-Ani<sup>12</sup> · Sally Salih Jumaa<sup>13</sup> · Munther Kadhim Abosaoda<sup>14,15,16</sup> · Li Zhang<sup>17</sup>

Received: 29 October 2023 / Accepted: 13 February 2024

© The Author(s), under exclusive licence to Springer Nature B.V. 2024

## Abstract

In this work, the catalytic activity of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) as catalysts of oxygen reduction reaction (ORR) and oxygen evolution reaction (OER) are examined. The Fe doped Si-nanotubes and Si-nanocages have more negative the formation energy and adoption energy values than Co doped Si-nanotubes and Si-nanocages. Results indicated that the reactions step of OOH\* creation for OER and OH\* elimination for ORR are the potential-determining steps. The \*O has the most negative adsorption energy than \*OH, \*OOH, \*H, O<sub>2</sub> and H<sub>2</sub>O species. The H<sub>2</sub>O is desorbed on Si-nanostructures with low adsorption energy. The Gibbs free energy values of reaction step 1 and step 2 (OH<sup>-</sup> + Si-nanostructure → Si-nanostructure-\*OH + e<sup>-</sup> → Si-nanostructure -\*O + H<sub>2</sub>O + e<sup>-</sup>) on Co and Fe doped Si-nanostructures are negative values. The overpotential of ORR processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are 1.24, 1.20, 1.15, 1.11, 1.07, 1.04, 1.00 and 0.97 eV. The metal doped Si-nanotubes and Si-nanocages have acceptable potential to catalyze the OER and ORR reactions.

**Keywords** Electrochemistry · Silicon · Nanostructures · Gibbs free energy · Overpotential · OER mechanism · ORR processes

✉ Li Zhang  
lizhang1203@chmail.ir

<sup>1</sup> Facultad de Ciencias Pecuarias, Escuela Superior Politécnica de Chimborazo (ESPOCH), Panamericana Sur Km. 1 1/2, Riobamba 060155, Ecuador

<sup>2</sup> Department of Medical Laboratory Technology, University of Imam Jaafar AL-Sadiq, Baghdad, Iraq

<sup>3</sup> Department of Biotechnology and Genetics, Jain (Deemed-to-Be) University, Bengaluru, Karnataka 560069, India

<sup>4</sup> Department of Allied Healthcare and Sciences, Vivekananda Global University, Jaipur, Rajasthan 303012, India

<sup>5</sup> School of Basic & Applied Sciences, Shobhit University, Gangoh, Uttar Pradesh 247341, India

<sup>6</sup> Department of Health & Allied Sciences, Arka Jain University, Jamshedpur, Jharkhand 831001, India

<sup>7</sup> Uttaranchal Institute of Pharmaceutical Sciences, Uttaranchal University, Dehradun, India

<sup>8</sup> Department of Chemistry, University College of Duba, University of Tabuk, Tabuk, Saudi Arabia

<sup>9</sup> National Institute of Laser Enhanced Sciences (NILES), University of Cairo, Giza 12613, Egypt

<sup>10</sup> Department of Anesthesia, College of Health & Medical Technology, Sawa University, Samawah, Aluthana, Iraq

<sup>11</sup> Department of Medical Engineering, Al-Hadi University College, Baghdad 10011, Iraq

<sup>12</sup> Department of Medical Engineering, Al-Nisour University College, Baghdad, Iraq

<sup>13</sup> Department of Medical Engineering, National University of Science and Technology, Nasiriyah, Dhi Qar, Iraq

<sup>14</sup> College of Pharmacy, the Islamic University, Najaf, Iraq

<sup>15</sup> College of Pharmacy, the Islamic University of Al Diwaniyah, Al Diwaniyah, Iraq

<sup>16</sup> College of Pharmacy, the Islamic University of Babylon, Al Diwaniyah, Iraq

<sup>17</sup> School of Mechanical and Electrical Engineering, Guangzhou Railway Polytechnic, Guangzhou 511370, China

## 1 Introduction

In recent years, the new nano-catalysts have been selected for oxygen reduction reaction (ORR) and oxygen evolution reaction (OER) processes in electrochemistry [1–3]. The metal based catalysts have low stability and selectivity to catalyze the ORR and OER processes [4–6]. The metal doped nanostructures such as nanotubes and nanocages have been proposed as acceptable catalysts for reactions in electrochemistry [7–10].

Researchers have been demonstrated that the silicon nanocages and silicon nanotubes can be utilized for ORR and OER processes based on their high surface and high selectivity and high stability [11–13]. Researchers have indicated that the various metal atoms such as Co and Fe can be doped on silicon nanocages and silicon nanotubes and these metals are active sites and potential positions of these catalysts to adsorb the important gas molecules [14–16].

Yu and et al. [17, 18] have used the theoretical models to calculate the effects of point defects on catalytic activity of silicene and their applications in the Li–O batteries. They have examined the nucleation mechanisms and decomposition reactions of  $\text{Li}_4\text{O}_2$  processes on  $\text{Ti}_2\text{O}$  in Li–O batteries by theoretical models. They have confirmed that the adsorbed LiO on  $\text{Ti}_2\text{O}$  cannot change the conductance in ORR and OER processes [17, 18]. They have indicated that the silicenes can catalyze the ORR and OER with high efficiency in normal temperature. They have demonstrated that the silicenes have high performance to use in batteries to obtain the ORR intermediates in normal temperature [17, 18].

Li and et al. [19–21] have examined the activity of  $\text{NbO}$ ,  $\text{MoO}_3$ ,  $\text{MnO}_2$  and  $\text{Nb}_2\text{O}_5$  compounds in reactions of metal batteries and their catalytic activity for OER and ORR. They have proposed the new strategies by oxygen deficiency to improve and increase the catalyst efficiency of OER and ORR processes. They have indicated that the  $\text{MoO}_3$  has important effects to prevent the oxygen production in Li–O batteries and Na–O batteries. They have confirmed that the  $\text{MoO}_3$  can do the reduction of metal peroxides as effective strategy to avoid the un-normal reactions [19–21].

The potential of Co and Fe doped Si-nanotubes (Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0)) and Co and Fe doped Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub>) to catalyze the OER and ORR are studied. The effects of water as solvent on absorption of species of ORR and OER on metal doped Si-nanotubes and Si-nanocages and on catalytic activity of Co and Fe doped Si-nanotubes and Si-nanocages to catalyze the ORR and OER processes are examined in normal temperature [22–24].

The formation energy ( $E_{\text{formation}}$ ) and adoption energy ( $E_{\text{adoption}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT

(6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are calculated and compared [25–27]. The adsorption energy ( $\Delta E_{\text{adsorption}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) to adsorb the ORR and OER species ( $\text{O}^*$ ,  $\text{*OH}$ ,  $\text{*OOH}$ ,  $\text{*H}$ ,  $\text{H}_2\text{O}$  and  $\text{O}_2$ ) are calculated and compared in gas phase and water [28–30].

The orbital energy and charge (q) values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are investigated [31]. The orbital energy and charge (q) values of complexes of metal doped Si nanocages and Co and Fe doped Si nanotubes with ORR and OER species including the  $\text{O}^*$ ,  $\text{*OH}$ ,  $\text{*OOH}$ ,  $\text{*H}$  and  $\text{O}_2$  are calculated [32].

The  $\Delta G_{\text{reaction}}$  of OER and ORR reaction steps ( $\text{OH}^- + \text{Si-nanostructure} \rightarrow \text{Si-nanostructure-}^*\text{OH} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{O} + \text{H}_2\text{O} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{OOH} + \text{e}^- \rightarrow \text{surface}^* + \text{O}_2 + \text{H}_2\text{O} + \text{e}^-$ ) on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase and water are investigated [33]. The overpotential of ORR and OER on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are examined [34].

## 2 Computational Details

The structures of Co and Fe doped Si nanocages and Co and Fe doped Si nanotubes (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0)) are optimized by M06-2X functional and cc-pVQZ basis set in GAMESS software [35–37]. The structures of complexes of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) with ORR and OER processes are optimized by M06-2X functional and cc-pVQZ basis set [38]. The frequencies of optimized structures of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) and there are examined by M06-2X functional and cc-pVQZ basis set [39–41].

The ability of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) to adsorb the species are investigated by  $\Delta E_{\text{adsorption}}$  via Eqs. 1 and 2 as following [42]:

$$\Delta E_{\text{adsorption}} = E_{\text{Si-nanotube-molecule}} - E_{\text{Si-nanotube}} - E_{\text{molecule}} \quad (1)$$

$$\Delta E_{\text{adsorption}} = E_{\text{Si-nanocage-molecule}} - E_{\text{Si-nanocage}} - E_{\text{molecule}} \quad (2)$$

The  $E_{\text{Si-nanotube}}$  and  $E_{\text{Si-nanocage}}$  are total energy of Co and Fe doped Si-nanotubes (Co-SiNT (5, 0), Co-SiNT (6, 0),

Fe-SiNT (5, 0) and Fe-SiNT (6, 0)) and Co and Fe doped Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub>), respectively. The  $E_{\text{molecule}}$  are total energy of important species of ORR and OER processes including the O\*, \*OH, \*OOH, \*H, H<sub>2</sub>O and O<sub>2</sub>. The  $E_{\text{Si-nanotube-molecule}}$  and  $E_{\text{Si-nanocage-molecule}}$  are total energy of complexes of Co and Fe doped Si-nanotubes (Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0)) and Co and Fe doped Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub>) with species including the O\*, \*OH, \*OOH, \*H and O<sub>2</sub>, respectively.

The main reaction for OER and ORR processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) is presented in Eq. 3 and the  $\Delta G_{\text{reaction}}$  of OER and ORR processes are calculated by Eq. 4 as following [43]:



$$\Delta G_{\text{reaction}} = \Delta G_{\text{adsorption}} + \Delta G_{\text{U}} + \Delta G_{\text{pH}} \quad (4)$$

The  $\Delta G_{\text{reaction}}$  is free Gibbs energy of complexes of Co and Fe doped Si-nanotubes and Co and Fe doped Si-nanocages with species and the  $\Delta G_{\text{U}}$  is defined by  $-neU$ , the  $U$  is electrode potential and  $\Delta G_{\text{pH}}$  is free energy correction [44–46].

The effects of water as solvent on absorption of species on Co and Fe doped Si-nanotubes and Si-nanocages and on catalytic activity of Co and Fe doped Si-nanotubes and Si-nanocages to catalyze the ORR and OER processes are examined by COSMO ((COnductor-like Screening MOdel)) model [47–50].

The orbital energy and charge ( $q$ ) values of Co and Fe doped Si nanocages and Co and Fe doped Si nanotubes (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0)) and their complexes including the O\*, \*OH, \*OOH, \*H and O<sub>2</sub> are calculated by M06-2X functional and cc-pVQZ basis set [51–53].

### 3 Results and Discussion

#### 3.1 Co and Fe Doped Si-nanostructures

The structures of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are presented in Fig. 1. The important bond lengths of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are reported in Fig. 1. The formation energy ( $E_{\text{formation}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are calculated by Eqs. 5 and 6 [54–56]:

$$E_{\text{formation}} = E_{\text{Si-nanotube}} - n * E_{\text{Si}} - E_{\text{Metal}} \quad (5)$$

$$E_{\text{formation}} = E_{\text{Si-nanocage}} - m * E_{\text{Si}} - E_{\text{Metal}} \quad (6)$$

The  $E_{\text{Si-nanotube}}$  and  $E_{\text{Si-nanocage}}$  are total energy of Co and Fe doped Si-nanotubes (Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0)) and Co and Fe doped Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub>), respectively. The  $E_{\text{Metal}}$  is total energy of an Fe and Co atoms in their bulk crystal. The  $n$  is the number of silicon atoms in Co and Fe doped Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub>) and the  $m$  is the number of silicon atoms in Co and Fe doped Si-nanotubes (Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0)).

The formation energy ( $E_{\text{formation}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are reported in Table 1. In gas phase, the  $E_{\text{formation}}$  of Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -4.35, -4.45, -4.79 and -4.90 eV, respectively. In gas phase, the  $E_{\text{formation}}$  of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub> are -4.15, -4.25, -4.56 and -4.67 eV, respectively. In water, the  $E_{\text{formation}}$  of Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -5.37, -5.50, -5.91 and -6.05 eV. The  $E_{\text{formation}}$  of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub> are -5.11, -5.24, -5.63 and -5.77 eV, respectively.

The adoption energy ( $E_{\text{adoption}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are calculated by Eqs. 7 and 8 [57–59]:

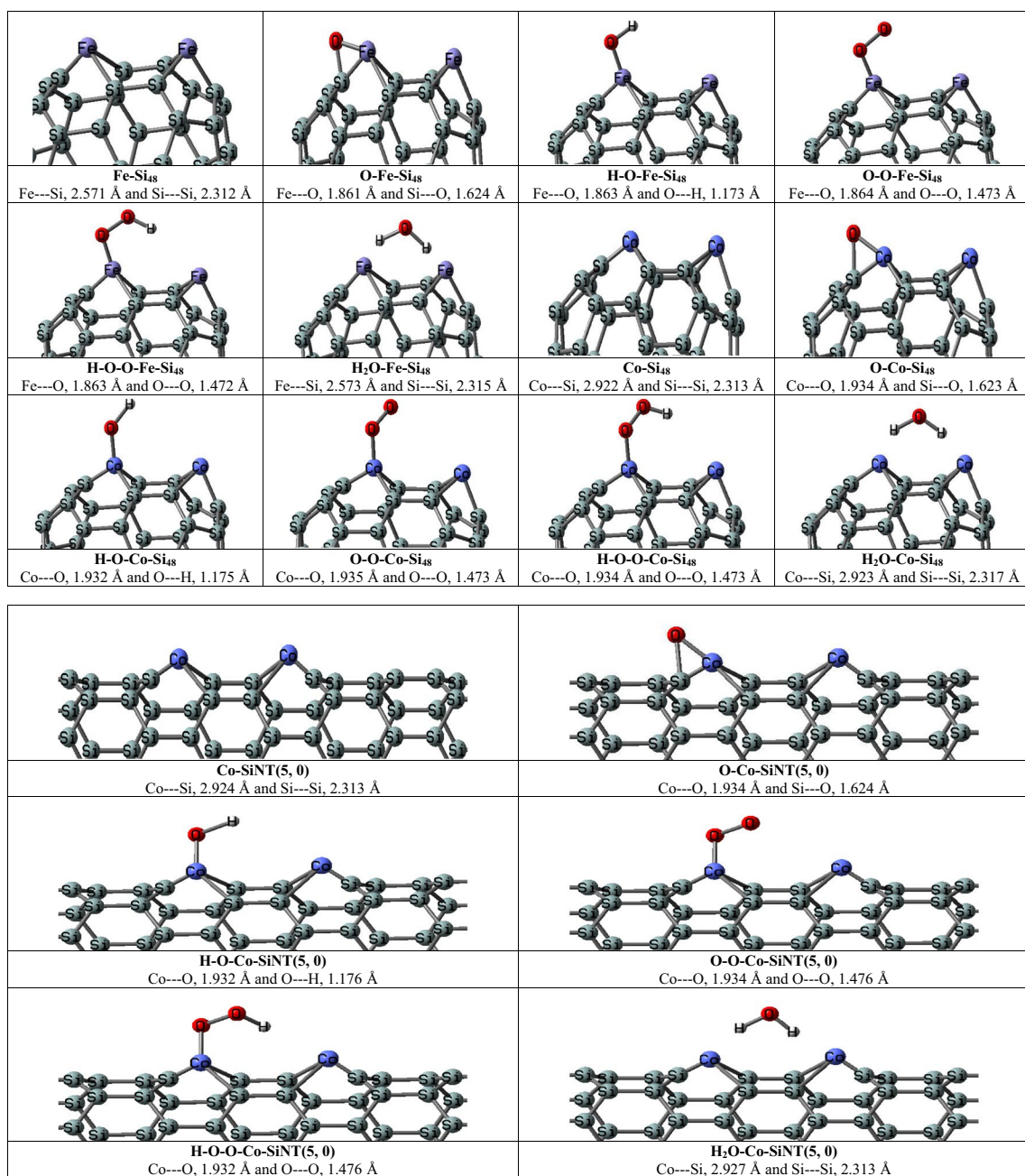
$$E_{\text{adoption}} = E_{\text{Metal-Si-nanotube}} - E_{\text{Si-nanocage}} - E_{\text{Metal}} \quad (7)$$

$$E_{\text{adoption}} = E_{\text{Metal-Si-nanocage}} - E_{\text{Si-nanocage}} - E_{\text{Metal}} \quad (8)$$

The  $E_{\text{Metal}}$  is total energy of an Fe and Co atoms in their bulk crystal. The  $E_{\text{Metal-Si-nanotube}}$  and  $E_{\text{Metal-Si-nanocage}}$  are total energy of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0), respectively. The  $E_{\text{Si-nanotube}}$  and  $E_{\text{Si-nanocage}}$  are total energy of Si-nanotubes (SiNT (5, 0), SiNT (6, 0), SiNT (5, 0) and SiNT (6, 0)) and Si-nanocages (Si<sub>48</sub>, Si<sub>60</sub>, Si<sub>48</sub> and Si<sub>60</sub>), respectively.

The adoption energy ( $E_{\text{adoption}}$ ) of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are reported in Table 1. In gas phase, the  $E_{\text{adoption}}$  of Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -3.13, -3.27, -3.71 and -3.87 eV, respectively. In gas phase, the  $E_{\text{adoption}}$  of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub> are -2.88, -3.00, -3.41 and -3.56 eV, respectively. In water, the  $E_{\text{adoption}}$  of Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -3.86, -4.03, -4.58 and -4.78 eV, respectively. In water, the  $E_{\text{adoption}}$  of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub> are -3.55, -3.70, -4.21 and -4.39 eV, respectively.

The  $E_{\text{adoption}}$  and  $E_{\text{formation}}$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are negative values and these metal



**Fig. 1** The structures of metal doped Si-nanostructures and their complexes of ORR and OER species and their important bond lengths

doped Si-nanotubes and Si-nanocages are stable from thermodynamic view point. The  $E_{\text{adoption}}$  and  $E_{\text{formation}}$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are negative values and these metal doped Si-nanotubes and Si-nanocages are stable from thermodynamic view point.

The calculated orbital energy of HOMO ( $E_{\text{HOMO}}$ ), LUMO ( $E_{\text{LUMO}}$ ) and HOMO–LUMO gap ( $E_{\text{HLG}} = E_{\text{HOMO}} - E_{\text{LUMO}}$ ) and charge ( $q$ ) values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are presented in Table 2. The  $E_{\text{HLG}}$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 2.04, 1.86, 1.68, 1.49, 1.31, 1.13, 0.93 and 0.67 eV, respectively. The  $q$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 0.912, 0.925, 0.938, 0.952, 0.966, 0.978, 0.990 and 0.998  $e$ , respectively. The Fe doped Si-nanotubes and Si-nanocages have lower  $E_{\text{HLG}}$  values and higher  $q$  values than Co doped Si-nanotubes and Si-nanocages. The metal doped Si-nanotubes have

(6, 0) are presented in Table 2. The  $E_{\text{HLG}}$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 2.04, 1.86, 1.68, 1.49, 1.31, 1.13, 0.93 and 0.67 eV, respectively. The  $q$  values of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 0.912, 0.925, 0.938, 0.952, 0.966, 0.978, 0.990 and 0.998  $e$ , respectively. The Fe doped Si-nanotubes and Si-nanocages have lower  $E_{\text{HLG}}$  values and higher  $q$  values than Co doped Si-nanotubes and Si-nanocages. The metal doped Si-nanotubes have



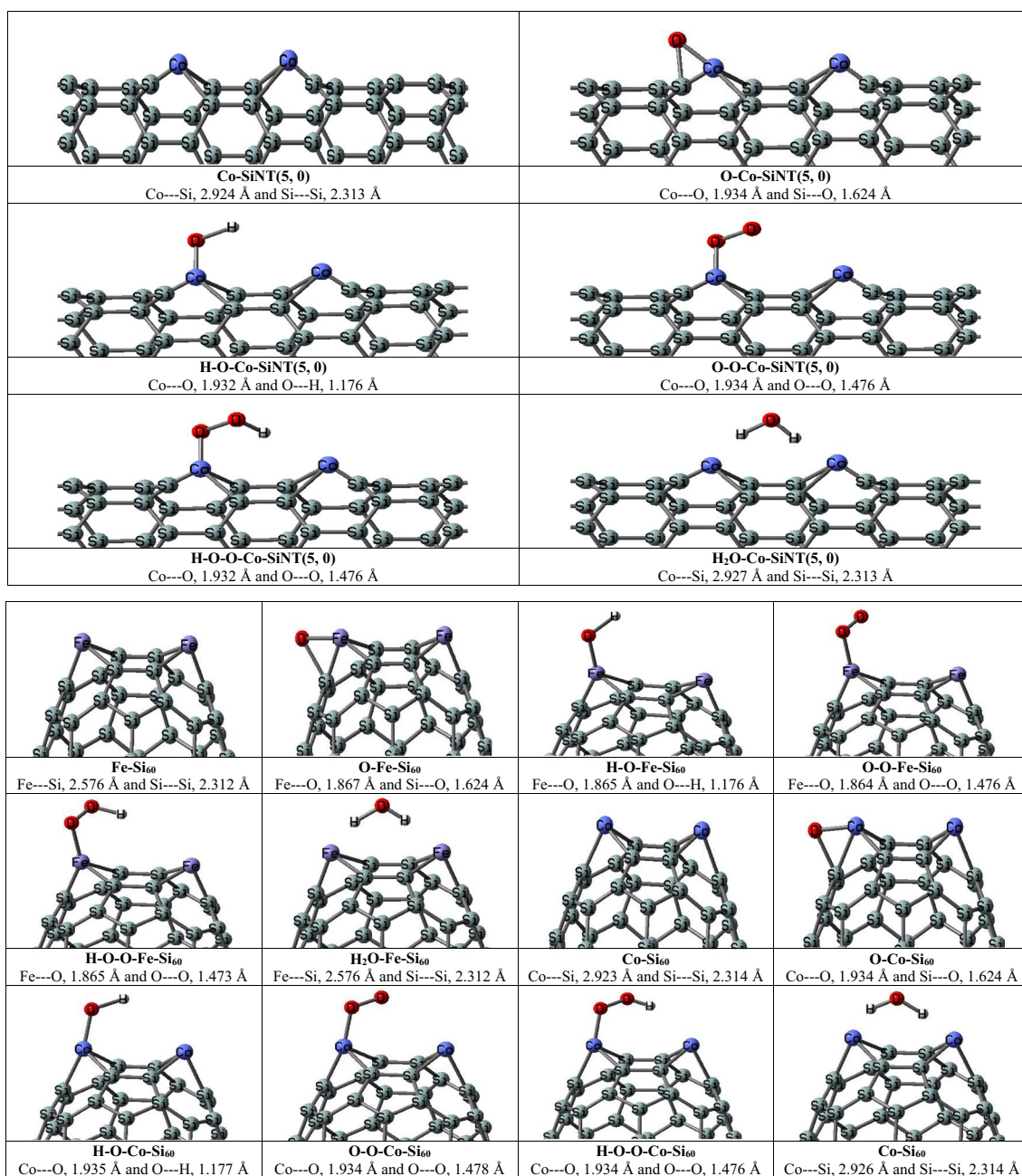


Fig. 1 (continued)

lower  $E_{\text{HLG}}$  values and higher  $q$  values than Co and Fe doped Si-nanocages.

### 3.2 Adsorption of ORR and OER Species on Metal Doped Si-Nanostructures

The potential of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) to adsorb the ORR and OER species (O\*, \*OH, \*OOH, \*H, H<sub>2</sub>O and O<sub>2</sub>) are calculated by  $\Delta E_{\text{adsorption}}$  via Eqs. 1

and 2. The  $\Delta E_{\text{adsorption}}$  of ORR and OER species (O\*, \*OH, \*OOH, \*H, H<sub>2</sub>O and O<sub>2</sub>) on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are reported in Table 1. The structures of complexes of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) with species are presented in Fig. 2. The important bond lengths of complexes of Fe- and Co-doped Si-nanostructures with OER and ORR species are reported in Fig. 2.

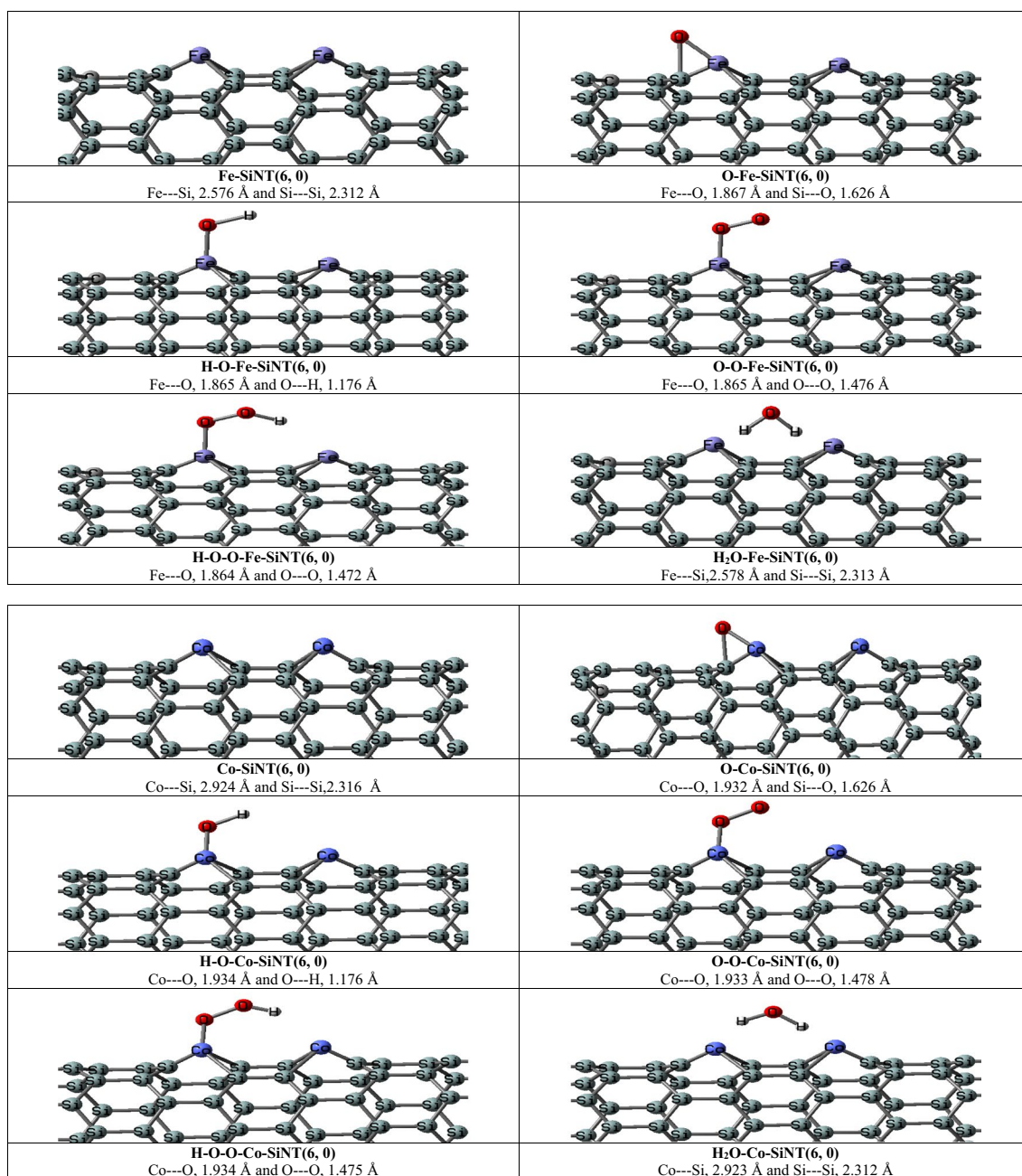


Fig. 1 (continued)

In gas phase, the  $\Delta E_{\text{adsorption}}$  of \*OH on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0) and Co-SiNT (6, 0) are -3.26, -3.48, -3.71 and -3.96 eV, respectively. The  $\Delta E_{\text{adsorption}}$  of \*OH on Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -4.21, -4.51, -4.81 and -5.13 eV, respectively. In gas phase, the  $\Delta E_{\text{adsorption}}$  of O<sub>2</sub> on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0) and Co-SiNT (6, 0) are -0.45, -0.48, -0.51 and -0.55 eV, respectively. The  $\Delta E_{\text{adsorption}}$  of O<sub>2</sub> on Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -0.72, -0.77, -0.82 and -0.87 eV, respectively.

In gas phase, the  $\Delta E_{\text{adsorption}}$  of \*O on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0) and Co-SiNT (6, 0) are -3.54, -3.78, -4.03 and -4.30 eV, respectively. The  $\Delta E_{\text{adsorption}}$  of \*O on Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -5.66, -6.04, -6.45 and -6.68 eV, respectively. In gas phase, the  $\Delta E_{\text{adsorption}}$  of \*OOH on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0) and Co-SiNT (6, 0) are -1.73, -1.84, -1.97 and -2.10 eV, respectively. The  $\Delta E_{\text{adsorption}}$  of \*OOH on Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -2.76, -2.95, -3.14 and -3.35 eV, respectively.

**Table 1** The  $E_{\text{formation}}$  in eV and  $E_{\text{adoption}}$  in eV of metal doped Si-nanostructures in gas phase and water, the  $\Delta E_{\text{adsorption}}$  in eV of species on metal doped Si-nanostructures at  $T = 298 \text{ K}$  in gas phase and water

Catalysts	$E_{\text{formation}}$ in gas phase	$E_{\text{adoption}}$ in gas phase	Catalysts	$E_{\text{formation}}$ in water	$E_{\text{adoption}}$ in water			
Co-Si <sub>48</sub>	-4.15	-2.88	Co-Si <sub>48</sub>	-5.11	-3.55			
Co-Si <sub>60</sub>	-4.25	-3.00	Co-Si <sub>60</sub>	-5.24	-3.70			
Co-SiNT(5, 0)	-4.35	-3.13	Co-SiNT(5, 0)	-5.37	-3.86			
Co-SiNT(6, 0)	-4.45	-3.27	Co-SiNT(6, 0)	-5.50	-4.03			
Fe-Si <sub>48</sub>	-4.56	-3.41	Fe-Si <sub>48</sub>	-5.63	-4.21			
Fe-Si <sub>60</sub>	-4.67	-3.56	Fe-Si <sub>60</sub>	-5.77	-4.39			
Fe-SiNT(5, 0)	-4.79	-3.71	Fe-SiNT(5, 0)	-5.91	-4.58			
Fe-SiNT(6, 0)	-4.90	-3.87	Fe-SiNT(6, 0)	-6.05	-4.78			
$\Delta E_{\text{adsorption}}$ in gas phase								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	-3.26	-3.48	-3.71	-3.96	-4.22	-4.51	-4.81	-5.13
Catalyst-*O	-3.54	-3.78	-4.03	-4.30	-4.59	-4.90	-5.22	-5.57
Catalyst-*OOH	-1.73	-1.84	-1.97	-2.10	-2.24	-2.39	-2.55	-2.72
Catalyst-O <sub>2</sub>	-0.45	-0.48	-0.51	-0.55	-0.58	-0.62	-0.66	-0.71
Catalyst-H <sub>2</sub> O	-0.23	-0.25	-0.27	-0.28	-0.30	-0.32	-0.35	-0.37
Catalyst-H*	-0.20	-0.22	-0.23	-0.25	-0.27	-0.28	-0.30	-0.32
$\Delta E_{\text{adsorption}}$ in water								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	-4.02	-4.29	-4.58	-4.88	-5.21	-5.56	-5.93	-6.33
Catalyst-*O	-4.37	-4.66	-4.97	-5.31	-5.66	-6.04	-6.45	-6.88
Catalyst-*OOH	-2.13	-2.27	-2.43	-2.59	-2.76	-2.95	-3.14	-3.35
Catalyst-O <sub>2</sub>	-0.55	-0.59	-0.63	-0.67	-0.72	-0.77	-0.82	-0.87
Catalyst-H <sub>2</sub> O	-0.29	-0.31	-0.33	-0.35	-0.37	-0.40	-0.43	-0.45
Catalyst-H*	-0.25	-0.27	-0.29	-0.31	-0.33	-0.35	-0.37	-0.40

The \*O has the most negative  $\Delta E_{\text{adsorption}}$  than \*OH, \*OOH, \*H, O<sub>2</sub> and H<sub>2</sub>O species on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase and water. The \*H and H<sub>2</sub>O species have the lowest  $\Delta E_{\text{adsorption}}$  than \*OH, \*OOH, \*O and O<sub>2</sub> species on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase and water. The H<sub>2</sub>O is adsorbed on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) with low  $\Delta E_{\text{adsorption}}$  in gas phase and water, so it can be desorbed from surfaces of catalysts with low energy. The H<sub>2</sub>O desorption is final step of ORR and OER processes and Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) have acceptable potential to desorb the H<sub>2</sub>O in normal temperature.

The calculated orbital energy of and charge (q) values of complexes of metal doped Si-nanostructures with species are presented in Table 2. The  $E_{\text{HLG}}$  values of complexes of \*OH with Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 3.771,

3.403, 3.046, 2.692, 2.362, 2.033, 1.714 and 1.404 eV, respectively. The  $E_{\text{HLG}}$  values of complexes of H<sub>2</sub>O with Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 3.032, 2.736, 2.449, 2.169, 1.899, 1.636, 1.378 and 1.128 eV, respectively. The  $E_{\text{HLG}}$  values of complexes of O<sub>2</sub> with Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 3.372, 3.043, 2.723, 2.413, 2.111, 1.819, 1.533 and 1.255 eV, respectively.

The q values of complexes of \*OOH with Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 0.816, 0.828, 0.840, 0.852, 0.865, 0.877, 0.890 and 0.816 e, respectively. The q values of complexes of \*O with Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 0.891, 0.904, 0.917, 0.930, 0.944, 0.957, 0.971 and 0.891 e, respectively. The q values of complexes of \*H on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are 0.315, 0.319, 0.324, 0.329, 0.333, 0.338, 0.343 and 0.315 e, respectively.

**Table 2** The  $E_{\text{HOMO}}$ ,  $E_{\text{LUMO}}$  and  $E_{\text{HLG}}$  in eV and charge (q) in  $e$  of metal doped Si-nanostructures and their complexes with species

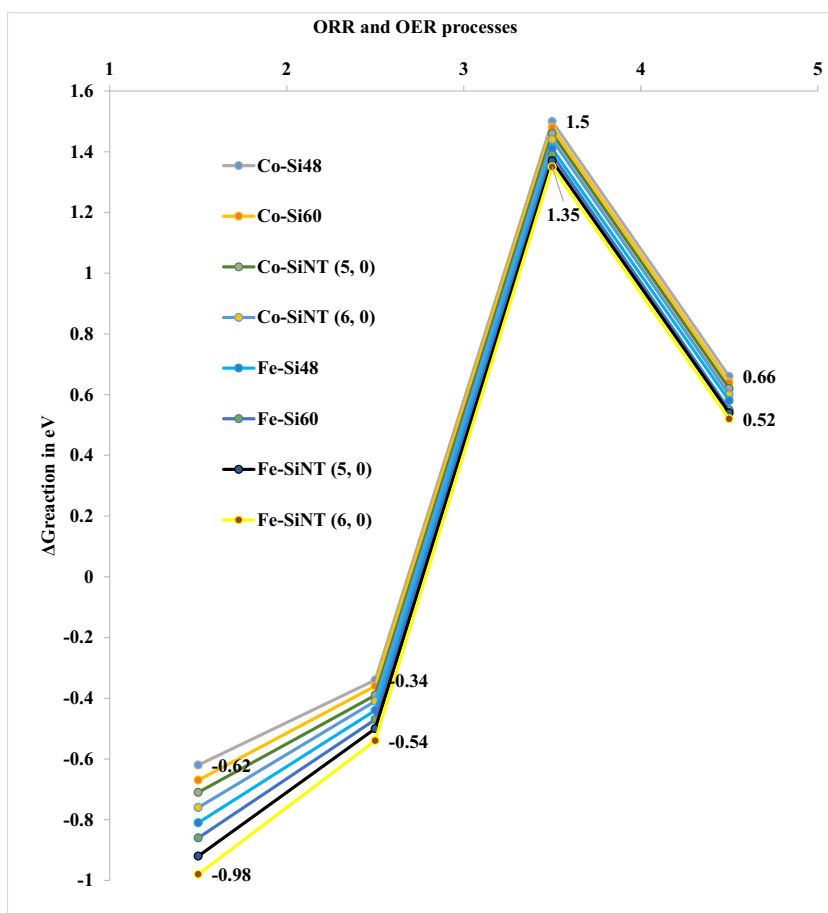
Catalysts	$E_{\text{HOMO}}$	$E_{\text{LUMO}}$	$E_{\text{HLG}}$	Charge (q)				
Co-Si <sub>48</sub>	-5.22	-3.18	2.04	0.912				
Co-Si <sub>60</sub>	-5.11	-3.25	1.86	0.925				
Co-SiNT(5, 0)	-5.01	-3.33	1.68	0.938				
Co-SiNT(6, 0)	-4.92	-3.41	1.49	0.952				
Fe-Si <sub>48</sub>	-4.81	-3.49	1.31	0.966				
Fe-Si <sub>60</sub>	-4.70	-3.57	1.13	0.978				
Fe-SiNT(5, 0)	-4.61	-3.67	0.93	0.990				
Fe-SiNT(6, 0)	-4.51	-3.75	0.76	0.998				
$E_{\text{HOMO}}$ in eV								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	-6.779	-6.484	-6.203	-5.933	-5.676	-5.428	-5.193	-4.967
Catalyst-*O	-6.716	-6.424	-6.145	-5.878	-5.622	-5.377	-5.144	-4.920
Catalyst-*OOH	-6.154	-5.887	-5.630	-5.385	-5.152	-4.927	-4.714	-4.509
Catalyst-O <sub>2</sub>	-6.063	-5.800	-5.548	-5.307	-5.076	-4.856	-4.645	-4.443
Catalyst-H <sub>2</sub> O	-5.450	-5.213	-4.987	-4.770	-4.563	-4.365	-4.174	-3.993
Catalyst-H*	-5.211	-4.985	-4.768	-4.561	-4.362	-4.173	-3.992	-3.818
$E_{\text{LUMO}}$ in eV								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	-3.008	-3.145	-3.288	-3.437	-3.593	-3.757	-3.928	-4.106
Catalyst-*O	-2.98	-3.115	-3.257	-3.405	-3.56	-3.722	-3.891	-4.068
Catalyst-*OOH	-2.731	-2.855	-2.985	-3.12	-3.262	-3.41	-3.565	-3.727
Catalyst-O <sub>2</sub>	-2.691	-2.813	-2.941	-3.074	-3.214	-3.36	-3.513	-3.673
Catalyst-H <sub>2</sub> O	-2.418	-2.528	-2.643	-2.763	-2.889	-3.02	-3.158	-3.301
Catalyst-H*	-2.312	-2.417	-2.527	-2.642	-2.762	-2.888	-3.019	-3.156
$E_{\text{HLG}}$ in eV								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	3.771	3.403	3.046	2.699	2.362	2.033	1.714	1.404
Catalyst-*O	3.736	3.371	3.017	2.673	2.339	2.014	1.698	1.390
Catalyst-*OOH	3.423	3.089	2.764	2.449	2.143	1.845	1.556	1.274
Catalyst-O <sub>2</sub>	3.372	3.043	2.723	2.413	2.111	1.819	1.533	1.255
Catalyst-H <sub>2</sub> O	3.032	2.736	2.449	2.169	1.899	1.636	1.378	1.128
Catalyst-H*	2.899	2.616	2.342	2.075	1.815	1.564	1.318	1.079
Charge (q) in $e$								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
Catalyst-*OH	0.899	0.912	0.926	0.939	0.953	0.966	0.980	0.899
Catalyst-*O	0.891	0.904	0.917	0.930	0.944	0.957	0.971	0.891
Catalyst-*OOH	0.816	0.828	0.840	0.852	0.865	0.877	0.890	0.816
Catalyst-O <sub>2</sub>	0.503	0.511	0.518	0.526	0.533	0.541	0.549	0.503
Catalyst-H <sub>2</sub> O	0.421	0.427	0.433	0.440	0.446	0.452	0.459	0.421
Catalyst-H*	0.315	0.319	0.324	0.329	0.333	0.338	0.343	0.315

The \*O has the lowest  $E_{\text{HLG}}$  values and the highest q values than \*OH, \*OOH, \*H, O<sub>2</sub> and H<sub>2</sub>O species on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>,

Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0). The \*H and H<sub>2</sub>O species have the highest  $E_{\text{HLG}}$  values and the lowest q



**Fig. 2** The chart of  $\Delta G_{\text{reaction}}$  on metal doped Si-nanostructures



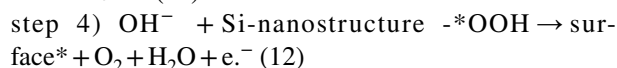
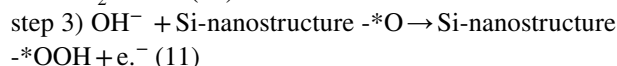
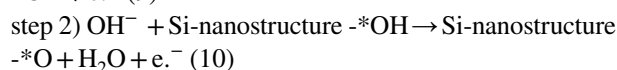
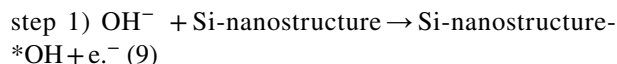
values than  $^*\text{OH}$ ,  $^*\text{OOH}$ ,  $^*\text{O}$  and  $\text{O}_2$  species on Co and Fe doped Si-nanotubes and Co and Fe doped Si-nanocages.

### 3.3 ORR and OER Mechanisms on Metal Doped Si-Nanostructures

In the ORR and OER processes as the first step the  $\text{O}_2$  molecules are adsorbed on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0). In the next step for ORR and OER processes the adsorbed  $\text{O}_2$  molecules are joined to  $^*\text{H}$  and then the  $^*\text{OOH}$  is created on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0). The adsorption of  $\text{O}_2$  molecules and the creation of  $^*\text{OOH}$  on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) have low activation barrier energy in normal temperature. It can be concluded that the formation of  $^*\text{OOH}$  on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) can be considered as the first step for ORR and OER processes.

The overall reaction steps for ORR and OER processes through 4 electron reaction steps on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>,

Fe-SiNT (5, 0), Fe-SiNT (6, 0) can be calculated via Eqs. 9, 10, 11 and 12 as following [60–62]:



The calculated  $\Delta G_{\text{reaction}}$  of these reaction steps ( $\text{OH}^- + \text{Si-nanostructure} \rightarrow \text{Si-nanostructure-}^*\text{OH} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{O} + \text{H}_2\text{O} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{OOH} + \text{e}^- \rightarrow \text{surface}^* + \text{O}_2 + \text{H}_2\text{O} + \text{e}^-$ ) on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase and water are presented in Table 3. The calculated overpotential of OER and ORR ( $\eta_{\text{OER}}$  and  $\eta_{\text{ORR}}$ ) processes on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase and water are reported in Table 3. The chart of  $\Delta G_{\text{reaction}}$  of ORR and OER processes on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>,

**Table 3** The  $\Delta G_{\text{reaction}}$  in eV of reaction steps on metal doped Si-nanostructures at T=298 K in gas phase and water and overpotential in V on metal doped Si-nanostructures in gas phase and water

$\Delta G_{\text{reaction}}$ in gas phase								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
$\text{OH}^- \rightarrow \text{*OH}$	-0.62	-0.67	-0.71	-0.76	-0.81	-0.86	-0.92	-0.98
$\text{OH}^- + \text{*OH} \rightarrow \text{*O} + \text{H}_2\text{O}$	-0.34	-0.36	-0.39	-0.41	-0.44	-0.47	-0.50	-0.54
$\text{OH}^- + \text{*O} \rightarrow \text{*OOH}$	1.50	1.48	1.46	1.44	1.41	1.39	1.37	1.35
$\text{OH}^- + \text{*OOH} \rightarrow \text{O}_2 + \text{H}_2\text{O}$	0.66	0.64	0.62	0.60	0.58	0.55	0.54	0.52
$\Delta G_{\text{reaction}}$ in water								
Catalysts	Co-Si <sub>48</sub>	Co-Si <sub>60</sub>	Co-SiNT (5, 0)	Co-SiNT (6, 0)	Fe-Si <sub>48</sub>	Fe-Si <sub>60</sub>	Fe-SiNT (5, 0)	Fe-SiNT (6, 0)
$\text{OH}^- \rightarrow \text{*OH}$	-0.77	-0.82	-0.88	-0.94	-1.00	-1.07	-1.14	-1.21
$\text{OH}^- + \text{*OH} \rightarrow \text{*O} + \text{H}_2\text{O}$	-0.42	-0.45	-0.48	-0.51	-0.55	-0.58	-0.62	-0.66
$\text{OH}^- + \text{*O} \rightarrow \text{*OOH}$	1.22	1.20	1.18	1.16	1.15	1.13	1.11	1.09
$\text{OH}^- + \text{*OOH} \rightarrow \text{O}_2 + \text{H}_2\text{O}$	0.54	0.52	0.50	0.48	0.47	0.45	0.43	0.42
Catalysts	$\eta_{\text{OER}}$ in gas phase		$\eta_{\text{ORR}}$ in gas phase		Catalysts		$\eta_{\text{OER}}$ in water	$\eta_{\text{ORR}}$ in water
Co-Si <sub>48</sub>	1.54		1.37		Co-Si <sub>48</sub>		1.38	1.24
Co-Si <sub>60</sub>	1.48		1.32		Co-Si <sub>60</sub>		1.33	1.20
Co-SiNT(5, 0)	1.43		1.28		Co-SiNT(5, 0)		1.28	1.15
Co-SiNT(6, 0)	1.38		1.23		Co-SiNT(6, 0)		1.24	1.11
Fe-Si <sub>48</sub>	1.32		1.19		Fe-Si <sub>48</sub>		1.19	1.07
Fe-Si <sub>60</sub>	1.28		1.15		Fe-Si <sub>60</sub>		1.15	1.04
Fe-SiNT(5, 0)	1.23		1.11		Fe-SiNT(5, 0)		1.10	1.00
Fe-SiNT(6, 0)	1.18		1.07		Fe-SiNT(6, 0)		1.06	0.97

Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are presented in Fig. 2.

In the step 1 ( $\text{OH}^- + \text{Si-nanostructure} \rightarrow \text{Si-nanostructure-}^*\text{OH} + e^-$ ) the OH is adsorbed on surface of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0). The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are -0.62, -0.67, -0.71, -0.76, -0.81, -0.86, -0.92 and -0.98 eV. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -0.77, -0.82, -0.88, -0.94, -1.00, -1.07, -1.14 and -1.21 eV, respectively.

In the step 2 ( $\text{OH}^- + \text{Si-nanostructure-}^*\text{OH} \rightarrow \text{Si-nanostructure-}^*\text{O} + \text{H}_2\text{O} + e^-$ ) the \*OH on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) is adsorbed the other OH<sup>-</sup>. The H<sub>2</sub>O molecule is released from surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) and the Si-nanostructure-<sup>\*</sup>O is created [63–65]. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are -0.34, -0.36, -0.39, -0.41, -0.44, -0.47, -0.50 and -0.54 eV. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>,

Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are -0.42, -0.45, -0.48, -0.51, -0.55, -0.58, -0.62 and -0.66 eV, respectively.

In step 3 ( $\text{OH}^- + \text{Si-nanostructure-}^*\text{O} \rightarrow \text{Si-nanostructure-}^*\text{OOH} + e^-$ ) the Si-nanostructure-<sup>\*</sup>O is adsorbed the other OH<sup>-</sup> on surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) and the Si-nanostructure-<sup>\*</sup>OOH is created. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are 1.50, 1.48, 1.46, 1.44, 1.41, 1.39, 1.37 and 1.35 eV. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are 1.22, 1.20, 1.18, 1.16, 1.15, 1.13, 1.11 and 1.09 eV, respectively.

In step 4 ( $\text{OH}^- + \text{Si-nanostructure-}^*\text{OOH} \rightarrow \text{surface}^* + \text{O}_2 + \text{H}_2\text{O} + e^-$ ) the Si-nanostructure-<sup>\*</sup>OOH is adsorbed the other OH<sup>-</sup> and the second H<sub>2</sub>O molecule is released from surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0). The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are 0.66, 0.64, 0.62, 0.60, 0.58, 0.55, 0.54 and 0.52 eV, respectively. The  $\Delta G_{\text{reaction}}$  values of this step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT

(5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are 0.54, 0.52, 0.50, 0.48, 0.47, 0.45, 0.43 and 0.42 eV.

The overpotential of OER processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are 1.54, 1.48, 1.43, 1.38, 1.32, 1.28, 1.23 and 1.18 eV, respectively. The overpotential of ORR processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are 1.38, 1.33, 1.28, 1.24, 1.19, 1.15, 1.10 and 1.06 eV.

Results indicated that the reactions step for OOH\* creation for OER processes is the potential-determining step on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) [66]. The potential-determining step for ORR processes is the step of OH\* elimination from surfaces of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0).

The overpotential of OER processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are 1.37, 1.32, 1.28, 1.23, 1.19, 1.15, 1.11 and 1.07 eV, respectively. The overpotential of ORR processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in water are 1.24, 1.20, 1.15, 1.11, 1.07, 1.04, 1.00 and 0.97 eV, respectively.

The  $\Delta G_{\text{reaction}}$  values of reaction steps 1 and 2 of ORR and OER processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) are negative values. The Fe doped Si-nanotubes and Si-nanocages for reaction steps of ORR and OER processes have more negative the  $\Delta G_{\text{reaction}}$  values than Co doped Si-nanotubes and Si-nanocages. The Co and Fe doped Si-nanotubes for reaction steps of ORR and OER processes have more negative  $\Delta G_{\text{reaction}}$  values than Co and Fe doped Si-nanocages. Finally, the Co and Fe doped Si-nanotubes and Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0)) have acceptable potential to catalyze the OER and ORR processes.

## 4 Conclusion

The potential of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) to catalyze the ORR and OER are investigated in gas phase and water. The  $E_{\text{formation}}$  of Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Fe-Si<sub>48</sub> and Fe-Si<sub>60</sub> are -4.15, -4.25, -4.56 and -4.67 eV, respectively. The  $E_{\text{adoption}}$  of Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -3.86, -4.03, -4.58 and -4.78 eV, respectively. The Fe doped Si-nanotubes and Si-nanocages have lower  $E_{\text{HLG}}$  values and higher  $q$  values than Co doped

Si-nanotubes and Si-nanocages. The H<sub>2</sub>O is adsorbed on Si-nanostructures with low  $\Delta E_{\text{adsorption}}$ , so it can be desorbed from surfaces of catalysts with low energy. The reaction steps of ORR on Si-nanostructures are  $\text{OH}^- + \text{Si-nanostructure} \rightarrow \text{Si-nanostructure-}^*\text{OH} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{O} + \text{H}_2\text{O} + \text{e}^- \rightarrow \text{Si-nanostructure-}^*\text{OOH} + \text{e}^- \rightarrow \text{surface}^* + \text{O}_2 + \text{H}_2\text{O} + \text{e}^-$ . In the step 1 the  $\Delta G_{\text{reaction}}$  on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0) and Co-SiNT (6, 0) are -0.62, -0.67, -0.71 and -0.76 eV. The  $\Delta G_{\text{reaction}}$  of step 2 on Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0) and Fe-SiNT (6, 0) are -0.44, -0.47, -0.50 and -0.54 eV, respectively. Results indicated that the reactions step of OOH\* creation for OER and OH\* elimination for ORR are the potential-determining steps. The overpotential of OER processes on Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0) in gas phase are 1.54, 1.48, 1.43, 1.38, 1.32, 1.28, 1.23 and 1.18 eV. Finally, the Co and Fe doped Si-nanotubes and Si-nanocages (Co-Si<sub>48</sub>, Co-Si<sub>60</sub>, Co-SiNT (5, 0), Co-SiNT (6, 0), Fe-Si<sub>48</sub>, Fe-Si<sub>60</sub>, Fe-SiNT (5, 0), Fe-SiNT (6, 0)) have acceptable potential to catalyze the OER and ORR processes.

**Supplementary Information** The online version contains supplementary material available at <https://doi.org/10.1007/s12633-024-02915-y>.

**Acknowledgements** We thank for or university for their helps.

**Authors' Contributions** Diana Katherine Campoverde Santos: Conceptualization, Methodology, Software, Mohammed Ahmed Mustafa: Formal analysis, Investigation Resources, Pooja Bansal: Validation, Validation, Formal analysis, Harpreet Kaur: Software, Validation, Writing—Original Draft, Mahamedha Deorari: Writing—Review & Editing, Visualization, Data Curation, Farag M. A. Altalbawy: Validation, Formal analysis, Investigation Resources, Dheyaa Yahaia Alhameedi: Validation, Validation, Formal analysis, Mahmood Hasen shuhata Alubiady: Writing—Original Draft, Writing—Review & Editing, Ahmed Muzahem Al-Ani: Conceptualization, Methodology, Software, Visualization, Sally Salih Jumaa: Validation, Formal analysis, Investigation Resources, Munther Kadhim Abosaoda: Software, Validation, Writing—Original Draft, Li Zhang: Formal analysis, Investigation Resources, Validation.

**Funding** Not applicable.

**Availability of Data and Material** Not applicable.

**Code Availability** Not applicable.

## Declarations

**Consent to Participate** I confirmed.

**Consent for Publication** I confirmed.

**Ethical Approval** All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional and/or national research committee and with the 1964 Helsinki declaration and its later amendments or comparable ethical standards.

**Competing Interests** The authors declare no competing interests.

## References

- Zhang SL, Zhang J, Li Y, Pan Z, Zhang J, Wang W, Xing Z, Cheng W, Cheng H, Tham N, Wang J, Liu Z (2023) *ACS Appl Mater Interfaces* 15(51):59454–59462
- Lin F, Li M, Zeng L, Luo M, Guo S (2023) *Chem Rev* 123(22):12507–12593
- Qiu Y, Fan J, Wu J, Lu W, Wang S, Wang D, Ge X, Zhao X, Zhang W, Zheng W, Cui X (2023) *Nano Lett* 23(20):9555–9562
- Ying J, Xiao Y, Chen J, Hu Z-Y, Tian G, Van Tendeloo G, Zhang Y, Symes MD, Janiak C, Yang X-Y (2023) *Nano Lett.* 23(16):7371–7378
- Pal S, Ahmed T, Khatun S, Roy P (2023) *ACS Appl Energy Mater* 6(15):7737–7784
- Shen J-F, Hu S-N, Tian N, Li M-Y, Yang S-L, Tian S-Y, Chen M-S, Zhou Z-Y, Sun S-G (2023) *ACS Sustain Chem Eng* 11(31):11660–11667
- Wang Z, Tian P, Zhang H, Deng K, Yu H, Xu Y, Li X, Wang H, Wang L (2023) *Ino Chem* 62(14):5622–5629
- Young Kim H, Jun M, Lee K, HoonJoo S (2023) *ACS Catal.* 13(1):355–374
- Cao F, Zhang H, Duan X, Li X, Ding R, Hua K, Rui Z, Wu Y, Yuan M, Wang J, Li J, Han M, Liu J (2022) *ACS Appl Mater Interfaces* 14(46):51975–51982
- Yang L, Hou S, Zhu S, Shi Z, Wang X, Jiang J, Chu Y, Bai J, Wang Y, Zhang L, Jiang Z, Liu C, Xing W, Ge J (2022) *ACS Catal* 12(21):13523–13532
- Liu J, Liu S, Yan F, Wen Z, Chen W, Liu X, Liu Q, Shang J, Yu R, Su D, Shui J (2022) *J Am Chem Soc* 144(41):19106–19114
- Zhang K, He Y, Guo R, Wang W, Zhan Q, Li R, He T, Wu C, Jin M (2022) *ACS Energy Lett* 7(10):3329–3336
- Xie M, Zhang B, Jin Z, Li P, Yu G (2022) *ACS Nano* 16(9):13715–13727
- Wang H, Zhou T, Deng K, Tian W, Yu H, Xu Y, Li X, Wang Z, Wang L (2022) *Energy Fuels* 36(14):7775–7781
- Hu J, Fang C, Jiang X, Zhang D, Cui Z (2022) *Inorg Chem* 61(24):9352–9363
- Wu H, Zhong H, Pan Y, Li H, Zeng J (2022) *Ind Eng Chem Res* 61(22):7504–7512
- Yu YX (2019) *J Phys Chem C* 123:205–213
- Li JH, Wu J, Yu YX (2020) *J Phys Chem C* 124:9089–9098
- Li JH, Yu YX (2021) *Nanoscale* 13:20637–20648
- Li JH, Wu J, Yu YX (2021) *J Mater Chem A* 9:10186–10198
- Li JH, Yu YX (2021) *Chemsuschem* 14:5488–5498
- Huang Y, Kong F, Tian H, Pei F, Chen Y, Meng G, Chang Z, Chen C, Cui X, Shi J (2022) *ACS Sustain Chem Eng* 10(19):6370–6381
- Campos-Roldán CA, Parnière A, Donzel N, Pailloux F, Blanchard P-Y, Jones DJ, Rozière J, Cavaliere S (2022) *ACS Appl Energy Mater* 5(3):3319–3328
- Chen Y, Li W, Yao Y, Gogoi P, Deng X, Xie Y, Yang Z, Wang Y, Li YC (2022) *ACS Appl Mater Interfaces* 14(10):12257–12263
- Nair AS, Anoop A, Ahuja R, Pathak B (2022) *J Phys Chem A* 126(8):1345–1359
- Wang W, Liu S, Min C, Zeng M, Shi H, Shao R, Liu S, Xu Z, Xia Y, Li N (2022) *ACS Appl Energy Mater* 5(2):2036–2044
- Tang Y, Zeng Z, Yi L, Zhu S, Li X, Li H, Lv N, Xu Y, Zhang Q, Wang Y (2022) *Energy Fuels* 36(4):2068–2074
- Noh S, Le T-H, Jo H, Kim S, Yoon H (2021) *ACS Appl Nano Mater* 4(12):14094–14104
- Lim J, Shin K, Bak J, Han Roh J, Jae Lee S (2021) *Chem Mater* 33(22):8895–8903
- Campos-Roldán CA, Pailloux F, Blanchard P-Y, Jones DJ, Rozière J, Cavaliere S (2021) *ACS Catal.* 11(21):13519–13529
- Huang L, Zheng X, Gao G, Zhang H, Rong K, Chen J, Liu Y, Zhu X, Wu W, Wang Y, Wang J, Dong S (2021) *J Am Chem Soc* 143(18):6933–6941
- Peng B, Liu H, Liu Z, Duan X, Huang Y (2021) *J Phys Chem Lett* 12(11):2837–2847
- Wang J, Liu X, Zhao C-X, Song Y-W, Liu J-N, Li X-Y, Bi C-X, Wan X, Shui J, Peng H-J, Li B-Q, Huang J-Q (2024) *J Energy Chem* 90:511–517
- Qian Y, Zhang F, Luo X, Zhong Y, Kang DJ, Hu Y (2024) *Small* 895:1–10
- Bartók AP, Kondor R, Csányi G (2013) *Phys Rev B: Condens Matter Mater Phys* 87:184115
- De S, Bartok AP, Csanyi G, Ceriotti M (2016) *Phys Chem Chem Phys* 18:13754–13769
- Zhu L, Amsler M, Fuhrer T, Schäfer B, Faraji S, Rostami S, Ghassemi SA, Sadeghi A, Grauzinyte M, Wolverson C, Goedecker S (2016) *J Chem Phys* 144:034203
- Sadeghi A, Ghasemi SA, Schäfer B, Mohr S, Lill MA, Goedecker S (2013) *J Chem Phys* 139:184118
- Rupp M, Tkatchenko A, Müller K-R, von Lilienfeld OA (2012) *Phys Rev Lett* 108:058301
- Behler J (2015) *Int J Quantum Chem* 115:1032–1050
- Gillan MJ, Alfé D, Michaelides A (2016) Perspective: How good is DFT for water. *J Chem Phys* 144:130901
- Del Ben M, Schönherr M, Hutter J, VandeVondele J (2013) *J Phys Chem Lett* 4:3753–3759
- Del Ben M, Hutter J, VandeVondele J (2015) *J Chem Phys* 143:054506
- Verlet L (1967) *Phys Rev* 159:98–103
- Elstner M, Porezag D, Jungnickel G, Elsner J, Haugk M, Frauenheim T, Suhai S, Seifert G (1998) *Phys Rev B: Condens Matter Mater Phys* 58:7260–7268
- Hu H, Lu Z, Elstner M, Hermans J, Yang W (2007) *J Phys Chem A* 111:5685–5691
- Skinner LB, Huang C, Schlesinger D, Pettersson LGM, Nilsson A, Benmore CJ (2013) *J Chem Phys* 138:074506
- Hutter J, Iannuzzi M, Schiffmann F, VandeVondele J (2014) *Rev: Comput Mol Sci* 4:15–25
- VandeVondele J, Krack M, Mohamed F, Parrinello M, Chassaing T, Hutter J (2005) *Comput Phys Commun* 167:103–128
- Lippert G, Hutter J, Parrinello M (1997) *Mol Phys* 92:477–488
- Perdew JP, Burke K, Ernzerhof M (1996) *Phys Rev Lett* 77:3865–3868
- Yao J, Li C, Sun K, Li H, Li H (2023) *IEEE/CVF Int Conf Comput Vis* 1:9455–9465
- Kong Z, Zhang P, Chen J, Zhou H, Ma X, Liang LJ (2021) *ACS Omega* 6:10936–10943
- Cui RF, Chen QH, Chen JX (2020) *Nanoscale* 12:12275–12280
- Li L, Xu W, Tan Y, Yang J, Tan D (2023) *Mech Syst Signal Process* 189:110058
- Li P, Abbas J, Wang Q, Zhang Q, Shah SAR (2024) *Gondwana Res* 128:86–105
- Huang J, Cho Y, Zhang Z, Jan A, Kummel AC (2022) *ACS Appl Mat Interf* 14:15716–15727
- Cho Y, Huang J, Ahles CF, Zhang Z, Wong K (2022) *Appl Sur Sci* 600:154010
- Zhang Z, Passlack M, Pitner G, Kuo CH (2022) *ACS Appl Mat Interf* 14:11873–11882
- Jiao Y, Gu L, Jiang Y, Weng M, Yang M (2023) *Bioinformatics* 39:btac719
- Jiao Y, Xie N, Gao Y, Wang CC, Sun Y (2022) *Euro Conf Comput Vis* 1:19–35



62. Jiao Y, Weng M, Yang M (2019) IEEE/CVF Conf Comput Pattern Recog 1:1–10
63. Chen Q, Wang J, Gao M, Liu L, Tao J (2022) Emerg Manag Sci Technol 2:10
64. Qian S, Fang Y, Yao C, Wang Y, Zhang Z et al (2022) Oncol Res 30:53–64
65. Willong L, Gangshin SJ (2023) Synth Chem 2:252–264
66. Kazemi M, Karezani N (2023) Biol Mol Chem 1:15–26

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor (e.g. a society or other partner) holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s); author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.