

Stat 100

MATHEMATICAL STATISTICS

Lecturer: Areeg Abdalla

Lectures: Sat. 9:00-11:00 Gp (1,2) مدرج مشرفه

Sun. 8:00-10:00 Gp (3,4) مدرج 5

Office Hours: Sat & Sun 10:00- 11:00

TAs: Hossam, Mariam, Rana, and Mohamed

Text Book: Elementary Statistics

by Mario F. Triola, 11th edition

Lectures, Hws, ...etc will be available on

<http://scholar.cu.edu.eg/?q=areegsaid/>

-> Go to Teaching

-> Find the semester

-> Find the course code

-> Click download material

Grading System

60 % Final

10 % Midterm

30 % Quizzes

Quizzes will be in Problem Sessions.

Some quizzes will be announced before; either in class or in problem session; Some quizzes will be pop up quizzes

Hws will be assigned to help you study. Some questions will be picked up to be solved in practice sections

Syllabus

will cover most – Not all –

- **Collection, preparation and tabulation of data, frequency distributions,**
- **central tendency measures: mean, median and mode,**
- **dispersion measures: range, semi-quartile difference, standard deviation,**
- **comparison between distributions, linear regression, correlation (Pearson and Spearman) time series analysis,**
- **introduction to probability: sample space, event, calculus of events, conditional probability and independence, random variables,**
- **probability distribution, some important distributions (binomial, Poisson, normal), sampling and sampling distribution, ratio distribution (small sample, large sample), confidence interval, tests of statistical hypothesis, index number.**

Chapter 1

Introduction to Statistics

1-1 Review and Preview

1-2 Statistical Thinking

1-3 Types of Data

1-4 Critical Thinking

1-5 Collecting Sample Data



Section 1-1

Review and Preview

Preview

Polls, studies, surveys and other data collecting tools collect data from a small part of a larger group so that we can learn something about the larger group. This is a common and important goal of statistics: Learn about a large group by examining data from some of its members.

Preview

In this context, the terms sample and population have special meaning. Formal definitions for these and other basic terms will be given here.

In this section we will look at some of the ways to describe data.

Data

❖ Data

collections of observations (such as measurements, genders, survey responses)

Statistics

❖ Statistics

is the science of planning studies and experiments, obtaining data, and then organizing, summarizing, presenting, analyzing, interpreting, and drawing conclusions based on the data

Population

❖ Population

**the complete collection of ALL individuals
(scores, people, measurements, etc.)
to be studied**

**the population is usually too big to be
studied directly, then statistics is used**

❖ **Parameter**

**a numerical measurement (value)
describing some characteristic of a
population**

population



parameter

Example:

US population (about 300 million)

$$N = 300,000,000$$

Examples of parameters:

1. Proportion of people supporting Health Care Reform

One can denote it by p ($0 < p < 1$)

2. Average weight of Americans

One can denote it by μ ($\mu > 0$)

Census versus Sample

❖ Census التعداد

Collection of data from every member of a population

(must include all **N** measurements)

❖ Sample العينة

Subcollection of members selected from a population

(**n** measurements; **$n < N$** ; **n** is **sample size**)

Statistic



Statistic

a numerical measurement describing some characteristic of a **sample**.

sample



statistic

Data

❖ Data

collections of observations (such as measurements, records, survey responses, etc.)

Next slides will describe types of data

Quantitative Data

❖ Quantitative (or numerical) data

consists of *numbers* representing counts or measurements.

Example: The weights of selected people

Example: The ages of respondents

Categorical Data

❖ Categorical (or qualitative) data

consists of names or “labels”
(representing categories)

Example: The genders (**male/female**) of professional athletes

Example: Answers in a poll (**yes/no**)

Example: Students' grades (**A,B,C,D,F**)

Working with Quantitative Data

**Quantitative (numerical) data
can further be described by
distinguishing between**

**discrete and continuous
types**

Discrete Data



Discrete data

these are numbers whose possible values are either a finite list of values or a 'countable' list of values

(for instance, possible values are

0, 1, 2, 3, . . .)

Example: The number of children in a family

Continuous Data

❖ Continuous (numerical) data

these are numbers with infinitely many possible values that correspond to some continuous scale that covers a range of values without gaps, interruptions, or jumps

Example: The weight of a person

Example: The annual income of a person

Working with Categorical Data

Categorical data can further be described by distinguishing between

**nominal and ordinal
types**

❖ **Nominal data types**

these are data types that consist of names, labels, or categories only, i.e. the data cannot be arranged in any ordering scheme (such as low to high)

Example: Survey responses (yes, no, undecided)

Example: Genders (male, female)

❖ Ordinal data

these are data types that can be arranged in some order, but there are no numerical differences between data values

Example: Course grades (**A, B, C, D, or F**)

Example: Survey responses such as

(**highly satisfied/satisfied/unsatisfied/very unsatisfied**)

Simple Random Sample

❖ Simple Random Sample

of n subjects selected in such a way that every possible **sample of the same size n** has the same chance of being chosen

Example: Pulse Rates of Females and Males

Original data:

Table 2-1 Pulse Rates (beats per minute) of Females and Males

Females																			
76	72	88	60	72	68	80	64	68	68	80	76	68	72	96	72	68	72	64	80
64	80	76	76	76	80	104	88	60	76	72	72	88	80	60	72	88	88	124	64
Males																			
68	64	88	72	64	72	60	88	76	60	96	72	56	64	60	64	84	76	84	88
72	56	68	64	60	68	60	60	56	84	72	84	88	56	64	56	56	60	64	72

Frequency Distribution Pulse Rates of Females

Table 2-2 Pulse Rates of Females

Pulse Rate	Frequency
60-69	12
70-79	14
80-89	11
90-99	1
100-109	1
110-119	0
120-129	1

Table 2-3 Relative Frequency Distribution of Pulse Rates of Females

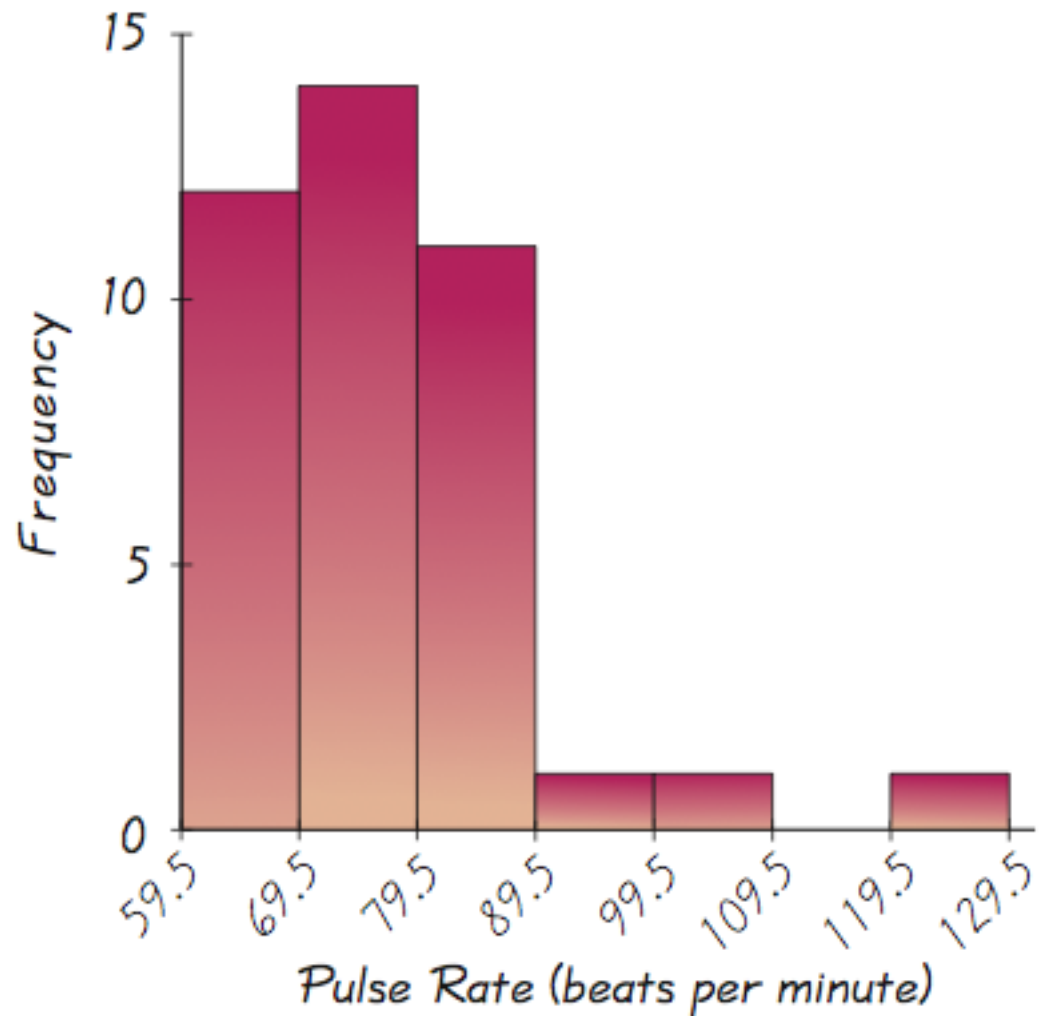
Pulse Rate	Relative Frequency
60-69	30%
70-79	35%
80-89	27.5%
90-99	2.5%
100-109	2.5%
110-119	0
120-129	2.5%

Histogram

Basically a graphic version of a frequency distribution.

Table 2-2 Pulse Rates of Females

Pulse Rate	Frequency
60-69	12
70-79	14
80-89	11
90-99	1
100-109	1
110-119	0
120-129	1



Another graph describing pulse rates of female:

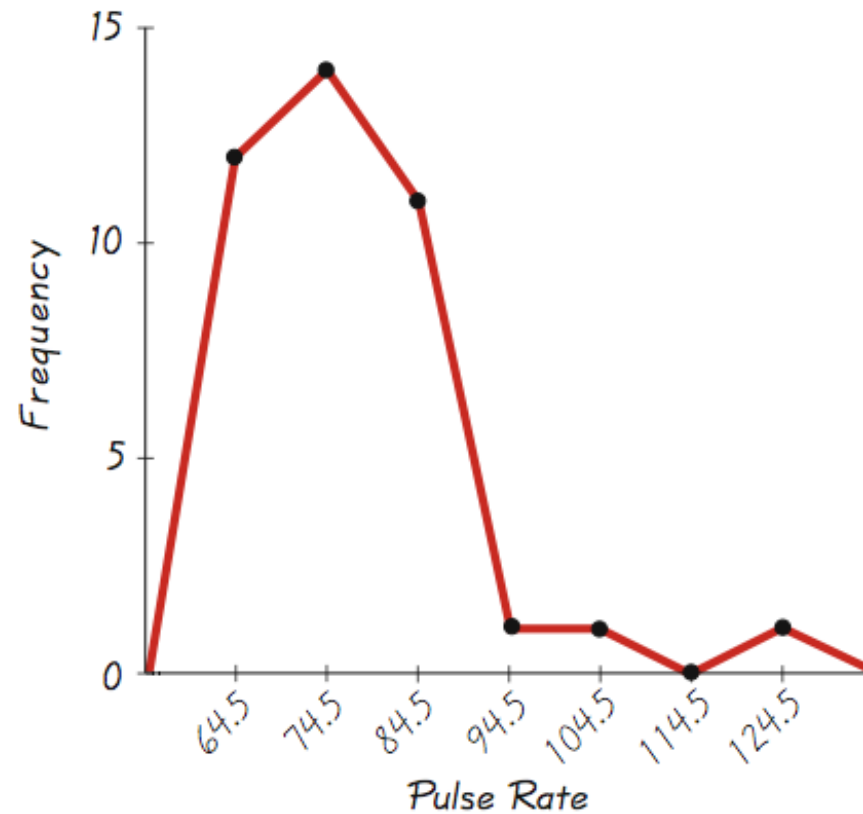


Figure 2-5 Frequency Polygon: Pulse Rates of Women

Two graphs allow us to compare two distributions:

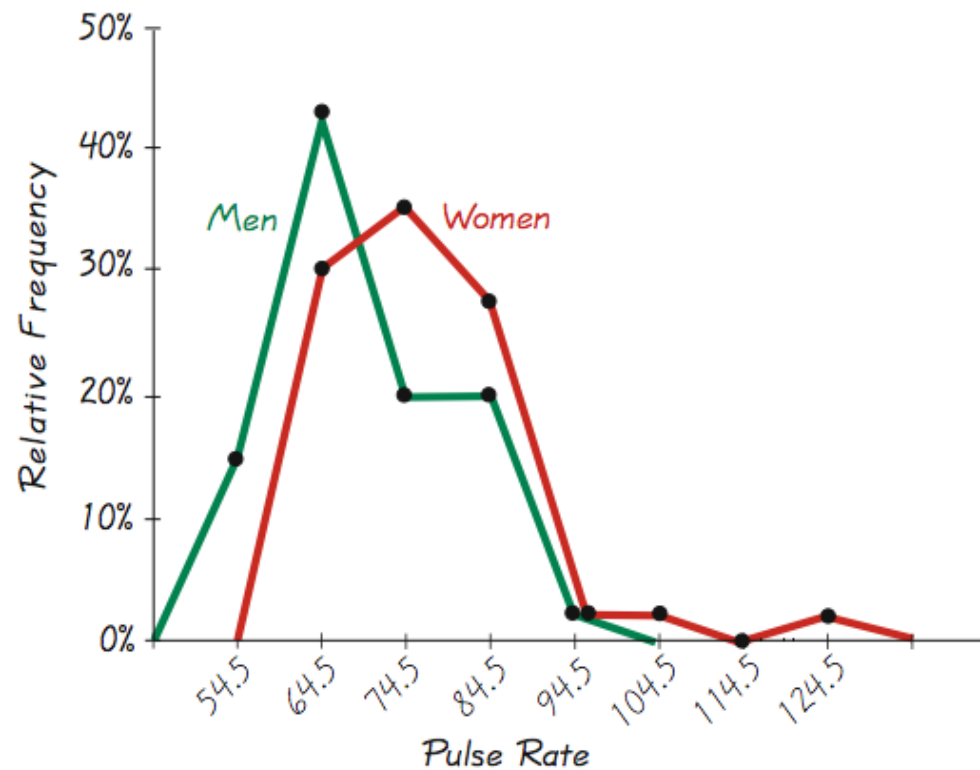
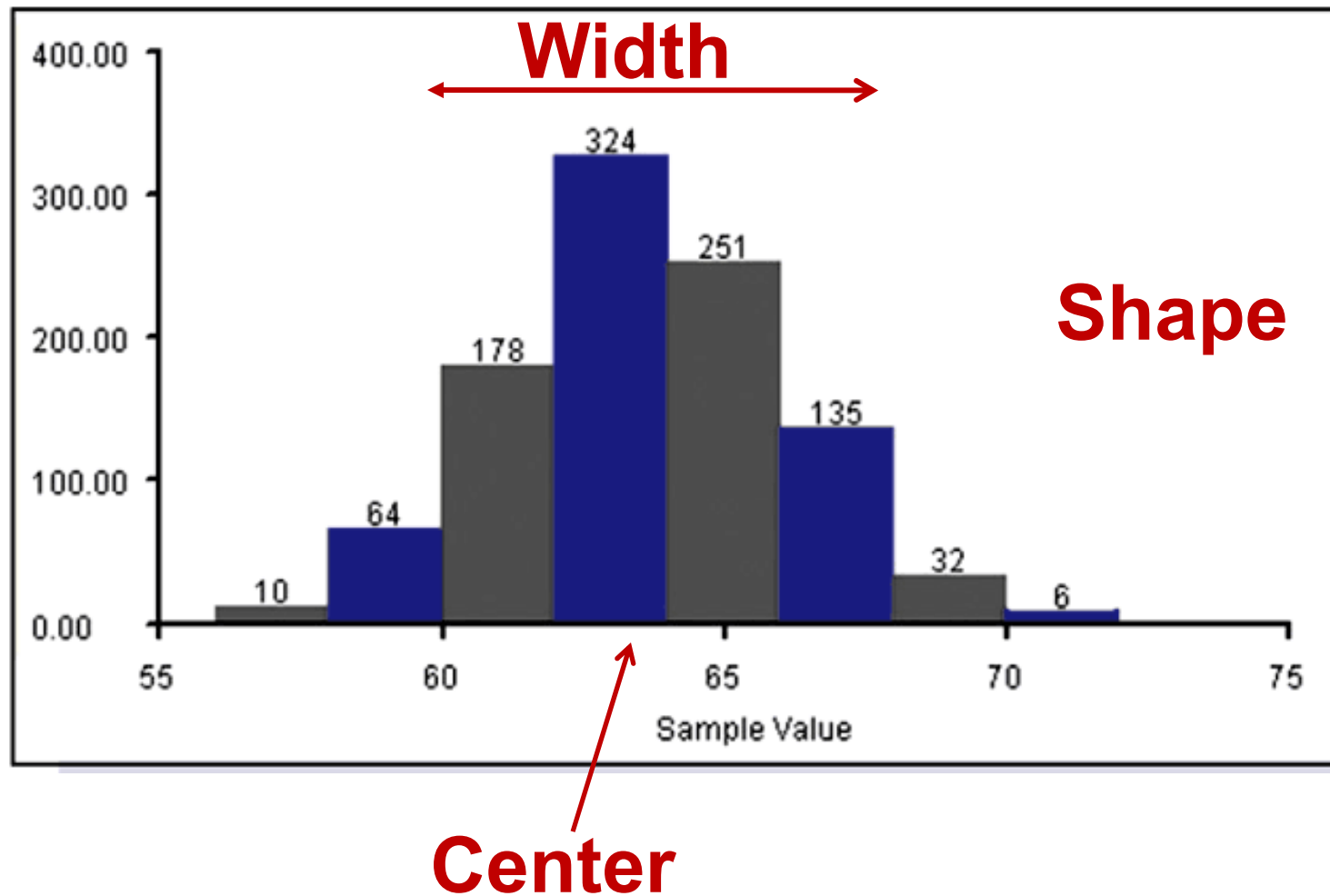


Figure 2-6 Relative Frequency Polygons: Pulse Rates of Women and Men

Characteristics of a distribution



The most common (typical) shape is a “bell” shape, looks like a hill. It is called a **normal distribution**. It has the following properties:

- ❖ The frequencies start low on the left, then increase to one or two highest frequencies in the middle, then decrease again to low frequencies on the right.
- ❖ The distribution is approximately symmetric, with frequencies preceding the maximum being roughly a mirror image of those that follow the maximum.

Normal distribution is characterized by two numbers (parameters):

- 1. Center** (most typical data value)
- 2. Width** (degree of **variation** of data values); also called **spread** or **variability** of data values