




SOLVING INEQUALITIES



Solving $A \cdot X + B < C$.

- A, B, C, X will be a continuous fuzzy number
- In the crisp case
$$ax+b \leq c$$
- let $E = A \cdot X + B$

- We write $N = (a/b/c)$ for a triangular fuzzy number.
- We write $T = (a/b, c/d)$ for a trapezoidal fuzzy number.

Example

- Let $A = (2/4/5)$, $B = (-6/-3/-1)$ and $C = (10/14/15)$.

Answer

Since $A > 0$

let us start with assuming $X \approx (x_1/x_2, x_3/x_4)$,

$X > 0$.

- The a-cuts are

$$A[\alpha] = [2 + 2\alpha, 5 - \alpha],$$

$$B[\alpha] = [-6 + 3\alpha, -1 - 2\alpha],$$

$$C[\alpha] = [10 + 4\alpha, 15 - \alpha]$$

- ,
 $X[\alpha] = [x_1(\alpha), x_2(\alpha)].$

- $E[\alpha] =$
 $[(2 + 2\alpha)x_1(\alpha) + (-6 + 3\alpha),$
 $(5 - \alpha)x_2(\alpha) + (-1 - 2\alpha)].$

- We first define $<$ between fuzzy numbers M and N . Let $v(M \leq N) = \sup\{\min(M(x), N(y)) \mid x \leq y\}$, which measures how much N is less than or equal to M . We write $N < M$ if $v(N \leq M) = 1$ but $v(M \leq N) < \vartheta$, where ϑ is some fixed fraction in $(0, 1]$. Let us use $\vartheta = 0.8$ in this book. Then $N < M$ if $v(N \leq M) = 1$ and $v(M \leq N) < 0.8$. We define $M \approx N$ when both $M < N$ and $N < M$ are false. $M \leq N$ means $M < N$ or $M \approx N$.

- $(2 + 2\alpha) \cdot x_1(\alpha) + (-6 + 3\alpha) \leq 10 + 4\alpha$,
- $(5 - \alpha)x_2(\alpha) + (-1 - 2\alpha) \leq 15 - \alpha$
- $x_1(\alpha) \leq \frac{16 + \alpha}{2 + 2\alpha}$
- $x_2(\alpha) \leq \frac{16 + \alpha}{5 - \alpha}$

Since

- $dx_1/d\alpha > 0$,
- $dx_2/d\alpha < 0$
- $x_1(1) \leq x_2(1)$

