

LETTER TO THE EDITOR

A UNIVERSAL NOTCH FILTER

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AND

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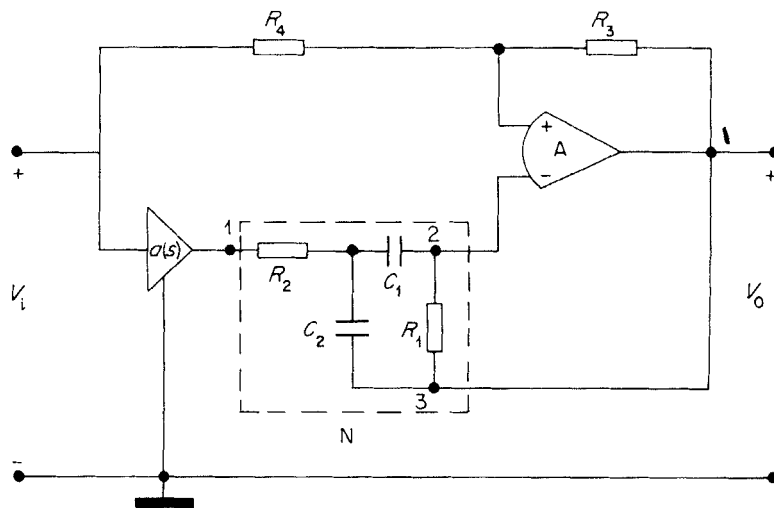
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Recently an active RC configuration for realizing a second-order allpass or a symmetrical notch responses has been given.¹ The circuit is capable of realizing a high pole Q and has the attractive feature of providing a constant gain factor of unity.

In this letter a worthy modification is added to the network¹ in order to provide any notch response. The notch frequency is controlled by a single capacitor. This modification has no effect on the poles of the transfer function, thus the frequency limitation equation of the network is the same as before.¹

Figure 1(a) represents the basic network, which is the same as before,¹ except that the voltage controlled voltage source (VCVS) is replaced by the frequency dependent VCVS, $a(s)$.

The practical realization of $a(s)$ using an operational amplifier is shown in Figure 1(b).



(a)

Figure 1.(a) The basic circuit. (b) The frequency dependent VCVS $a(s)$: ● o.c. for highpass notch, s.c. for notch and lowpass notch; ▲ o.c. for notch and highpass notch, s.c. for lowpass notch

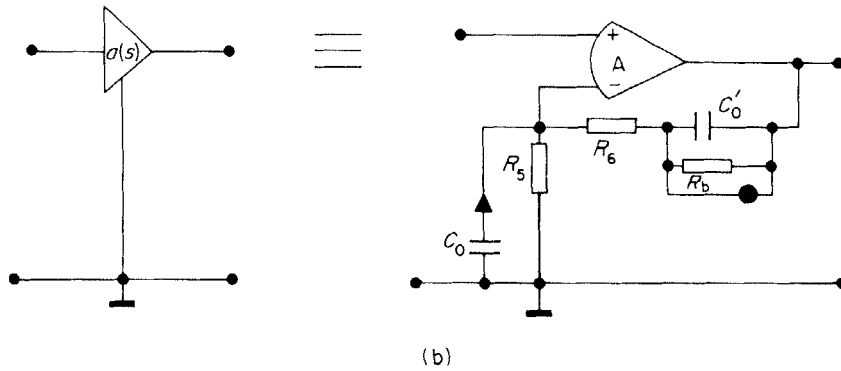


Figure 1—continued

Table I summarizes the results for the two cases of lowpass and highpass notch filters.

The circuit of Figure 1 was constructed in the laboratory using operational amplifiers type LM 741 (National Semiconductor Corp.) with $V_{CC} = \pm 15$ V supply voltages to realize $f_p = 533.3$ Hz and $Q_p = 10$. The element values taken are $R = 30.01$ k Ω and $C = 10$ nF.

For the lowpass notch, C_0 was taken as 2.2 nF and 3.4 nF to realize $f_z = 710$ Hz and 940 Hz, respectively. Figure 2 represents the theoretical and the experimental results obtained.

For the highpass notch, C'_0 was taken as 33 nF and 46 nF to realize $f_z = 335$ Hz and 400 Hz, respectively, and the results are shown in Figure 3.

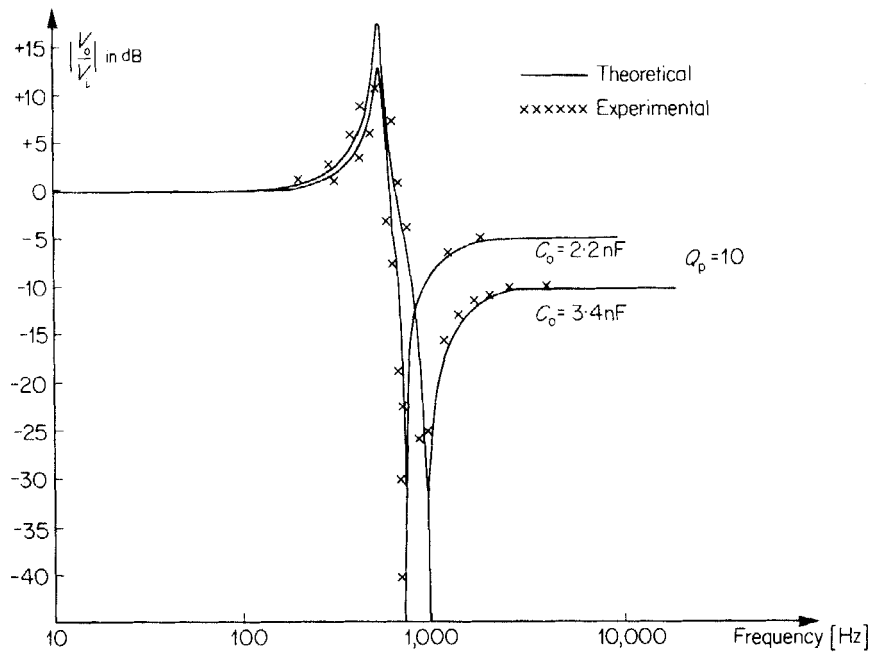


Figure 2. Frequency response of the lowpass notch filter

Table I

Network Type	Lowpass notch	Highpass notch	
Network Parameters			
The transfer function of a generalized passive RC bandpass network N	$T(s) = \frac{K\omega_p s}{s^2 + \left(\frac{\omega_p}{q_p}\right)s + \omega_p^2}$	$0 < q_p < 0.5$ and $Kq_p \leq 1$	
The gain of the frequency dependent VCVS	$a(s) = a_0 + s\tau$ where $a_0 = 1 + \frac{R_6}{R_5}, \tau = C_0 R_6$	$a(s) = a_0 + \frac{1}{s\tau'}$ where $a_0 = 1 + \frac{R_6}{R_5}, \tau' = C_0' R_5$	
The overall voltage transfer function V_o/V_i (assuming ideal OA's)	$G(s) = \frac{s^2 \left(1 - \frac{K\omega_p \tau}{m}\right) + \omega_p^2}{s^2 + s\omega_p \left(\frac{1}{q_p} - \frac{K}{m}\right) + \omega_p^2}$ where $m = R_3/(R_3 + R_4)$	$G(s) = \frac{s^2 + \left(\omega_p^2 - \frac{K\omega_p}{m\tau'}\right)}{s^2 + s\omega_p \left(\frac{1}{q_p} - \frac{K}{m}\right) + \omega_p^2}$	
Stability condition		$m > Kq_p$	
Notch condition		$a_0 = \frac{m}{Kq_p} = \frac{1}{1 - (q_p/Q_p)}$	
Notch radian frequency	$\omega_z = \frac{\omega_p}{\sqrt{1 - (\omega_p K \tau / m)}}$	$\omega_z = \omega_p \sqrt{\left(1 - \frac{K}{\omega_p \cdot m \tau'}\right)}$	
Design equations	N parameters	$R_2 = R, C_2 = C = \frac{1}{\omega_p \cdot R}$	$R_1 = Q_p \cdot R, C_1 = \frac{C}{Q_p}$
	Potential divider parameters	$m = \frac{1}{2}, R_3 = R_4 = R'$	
	Controlled source parameters	$R_6 = R, R_5 = 2Q_p R$ $C_0 = \frac{C}{2} \left[1 - \left(\frac{\omega_p}{\omega_z}\right)^2\right]$	$R_5 = R, R_6 = \frac{R}{2Q_p}$ $C_0' = \frac{2C}{1 - \left(\frac{\omega_z}{\omega_p}\right)^2}$
Effect of the rolloff of the OA gain ¹		$\frac{\Delta\omega_p}{\omega_p} \approx -\frac{2\omega_p}{GB}$ & $\frac{\Delta Q_p}{Q_p} = \frac{2\omega_p}{GB}$ for $Q_p \gg \frac{1}{2}$	

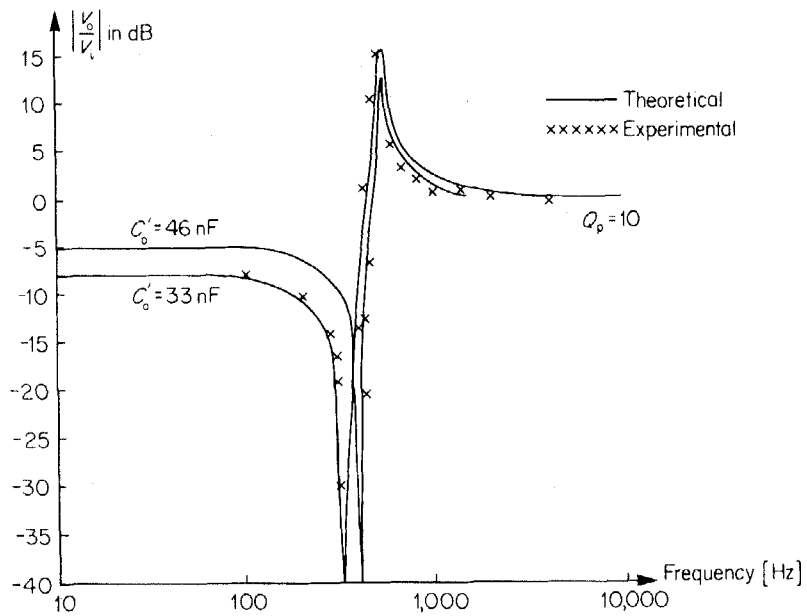


Figure 3. Frequency response of the highpass notch filter

REFERENCE

1. A. M. Soliman, 'A new active RC configuration for realizing nonminimum phase transfer functions', *Int. J. Cir. Theor. Appl.* **2**, 307-315 (1974).