

Lecture 2

Ideal gases

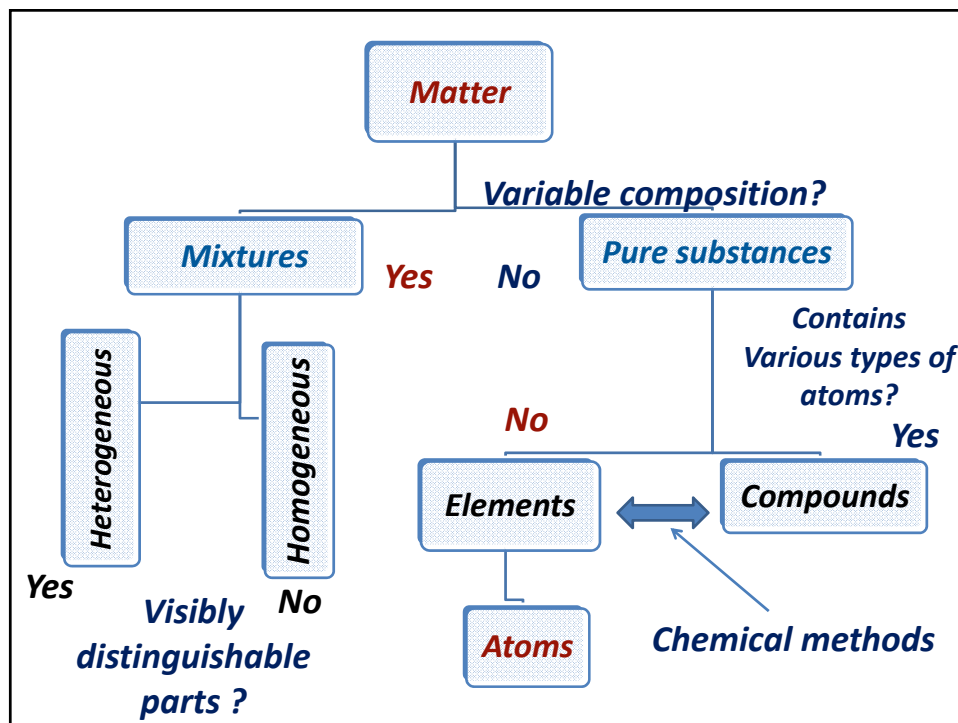


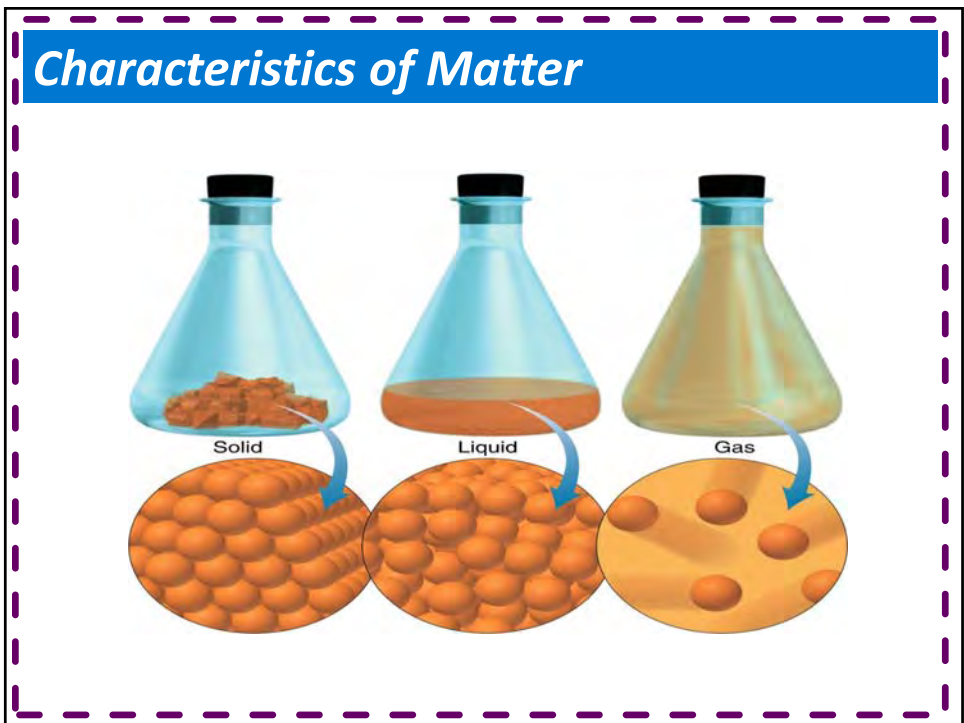
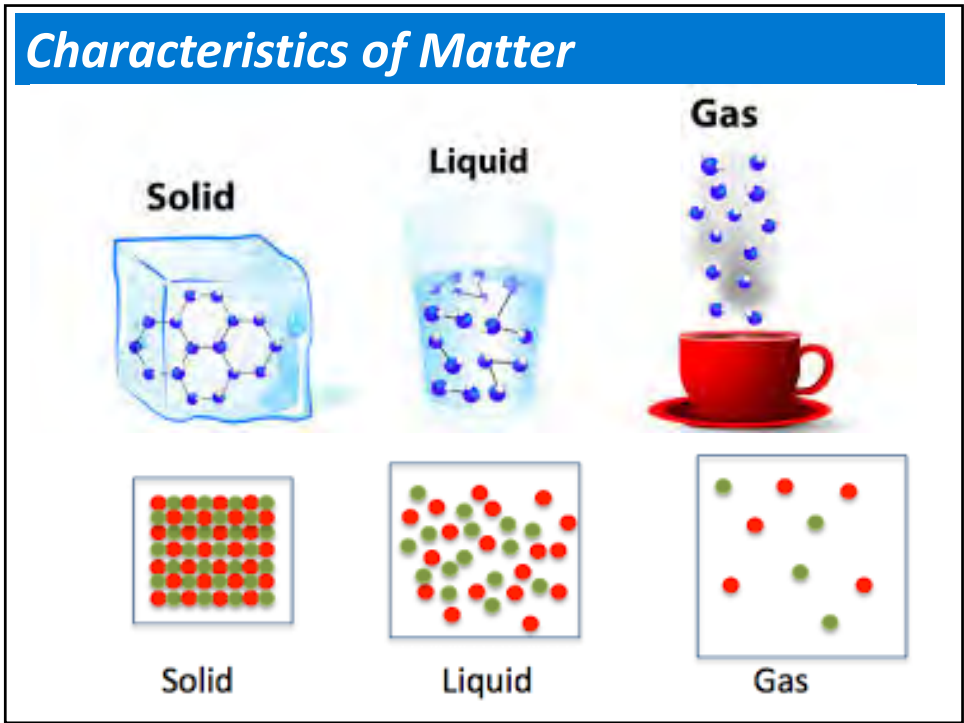
TABLE R.5 > Densities of Various Common Substances* at 20°C

| Substance | Physical State | Density (g/cm ³) |
|------------------------|----------------|------------------------------|
| Oxygen | Gas | 0.00133 |
| Hydrogen | Gas | 0.000084 |
| Ethanol | Liquid | 0.789 |
| Benzene | Liquid | 0.880 |
| Water | Liquid | 0.9982 |
| Magnesium | Solid | 1.74 |
| Salt (sodium chloride) | Solid | 2.16 |
| Aluminum | Solid | 2.70 |
| Iron | Solid | 7.87 |
| Copper | Solid | 8.96 |
| Silver | Solid | 10.5 |
| Lead | Solid | 11.34 |
| Mercury | Liquid | 13.6 |
| Gold | Solid | 19.32 |

*At 1 atmosphere pressure.

Characteristics of Matter

| Character | Solid | Liquid | Gas |
|---|---------------------------|--|------------------------------|
| <i>Particle packing "arrangement"</i> | <i>Regular</i> | <i>Irregular</i> | <i>Irregular</i> |
| <i>Shape</i> | <i>Fixed</i> | <i>Not fixed</i> | <i>Not fixed</i> |
| <i>Volume</i> | <i>Fixed</i> | <i>Fixed</i> | <i>Not fixed</i> |
| <i>Motion</i> | <i>Only vibrating</i> | <i>Move around past each other</i> | <i>Freely - randomly</i> |
| <i>Compressibility</i> | <i>No</i> | <i>little</i> | <i>high</i> |



Elements that exist as gases at 25°C and 1 atmosphere

| | | | | | | | | | | | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|----|----|
| 1A | | | | | | | | | | | | | | | | | | | 8A |
| H | | | | | | | | | | | | | | | | | | | He |
| Li | Be | | | | | | | | | | | B | C | N | O | F | | Ne | |
| Na | Mg | | | | | | | | | | | Al | Si | P | S | Cl | | Ar | |
| K | Ca | Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | | Kr | |
| Rb | Sr | Y | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I | | Xe | |
| Cs | Ba | La | Hf | Ta | W | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | | Rn | |
| Fr | Ra | Ac | Rf | Db | Sg | Bh | Hs | Mt | | | | | | | | | | | |

Some Substances Found as Gases at 1 atm and 25°C

Elements

H₂ (molecular hydrogen)
 N₂ (molecular nitrogen)
 O₂ (molecular oxygen)
 O₃ (ozone)
 F₂ (molecular fluorine)
 Cl₂ (molecular chlorine)
 He (helium)
 Ne (neon)
 Ar (argon)
 Kr (krypton)
 Xe (xenon)
 Rn (radon)

Compounds

HF (hydrogen fluoride)
 HCl (hydrogen chloride)
 HBr (hydrogen bromide)
 HI (hydrogen iodide)
 CO (carbon monoxide)
 CO₂ (carbon dioxide)
 NH₃ (ammonia)
 NO (nitric oxide)
 NO₂ (nitrogen dioxide)
 N₂O (nitrous oxide)
 SO₂ (sulfur dioxide)
 H₂S (hydrogen sulfide)
 HCN (hydrogen cyanide)*

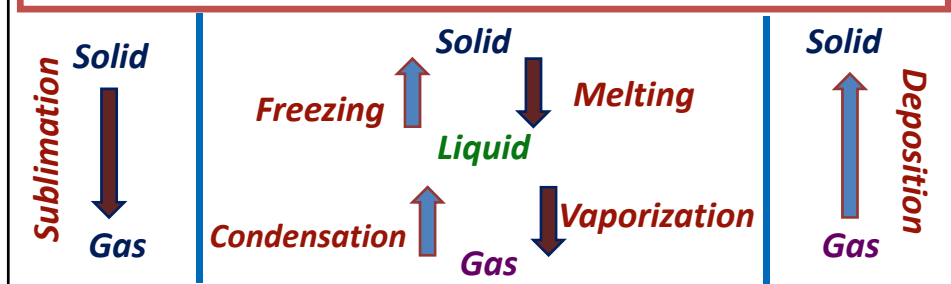
* The boiling point of HCN is 26°C, but it is close enough to qualify as a gas at ordinary atmospheric conditions.

| Gas | Liquid | Solid |
|--|---|--|
| Particles are far apart, run in rapid random motion (translation, rotational, vibrational) | Particles lies in-between, intermediate motion (translation, rotational) | Particles are very close together, vibrate only in place |
| High volumes and Low densities | Intermediate volumes and densities | Small volumes and high densities |
| Very weak attraction forces | Intermediate forces | Strong forces |
| assumes the shape and volume of its container | assumes the shape of the part of the container which it occupies – has a fixed volume | retains a fixed volume and shape rigid - particles locked into place |
| compressible lots of free space between particles | not easily compressible little free space between particles | not easily compressible little free space between particles |
| flows easily particles can move past one another | flows easily particles can move/slide past one another | does not flow easily rigid - particles cannot move/slide past one another |

Liquids and Solids: condensed phases
Liquids and Gases: Fluids

Conversion of States

- **Sublimation** is the process of changing from the solid phase right to a gas phase, without passing by the liquid state.
- **Deposition** is a process in which a gas will form a solid, again without any apparent liquid phase in between.
- **Boiling point:** The temperature at which a liquid boils and at which the vapor pressure of the liquid equal the atmospheric pressure.



Pressure: a normal force exerted by a fluid per unit area

✚ It has the unit (N/m^2), which is called a pascal (Pa).

$$1 \text{ bar} = 10^5 \text{ Pa} = 0.1 \text{ MPa} = 100 \text{ kPa}$$

$$1 \text{ atm} = 101,325 \text{ Pa} = 101.325 \text{ kPa} = 1.01325 \text{ bars}$$

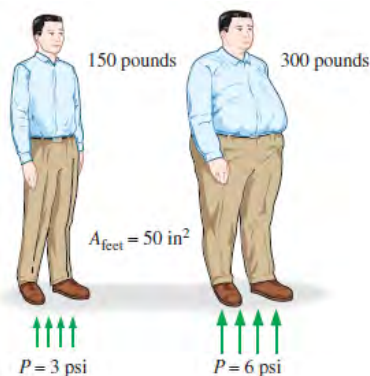
kilogram-force per square centimeter

$$\begin{aligned} 1 \text{ kgf}/\text{cm}^2 &= 9.807 \text{ N}/\text{cm}^2 = 9.807 \times 10^4 \text{ N}/\text{m}^2 = 9.807 \times 10^4 \text{ Pa} \\ &= 0.9807 \text{ bar} \\ &= 0.9679 \text{ atm} \end{aligned}$$

- In the English system, the pressure unit is pound-force per square inch (lbf/in^2 , or **psi**), and $1 \text{ atm} = 14.696 \text{ psi}$.
- **Pressure** is also used on solid surfaces as synonymous to normal stress, which is the force acting perpendicular to the surface per unit area.

✚ A 150-pound person with a total foot imprint area of 50 in^2 exerts a pressure of $150 \text{ lbf}/50 \text{ in}^2 = 3.0 \text{ psi}$ on the floor.

✚ If the person stands on one foot, the pressure doubles.



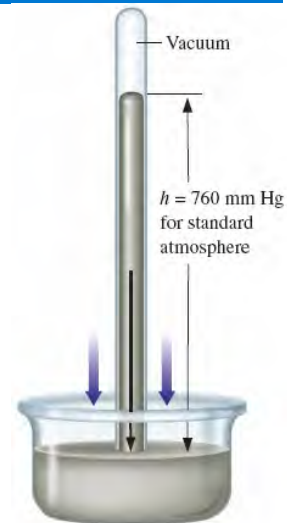
✚ If the person gains excessive weight, he or she is likely to encounter foot discomfort because of the increased pressure on the foot (the size of the bottom of the foot does not change with weight gain).

✚ This explains:

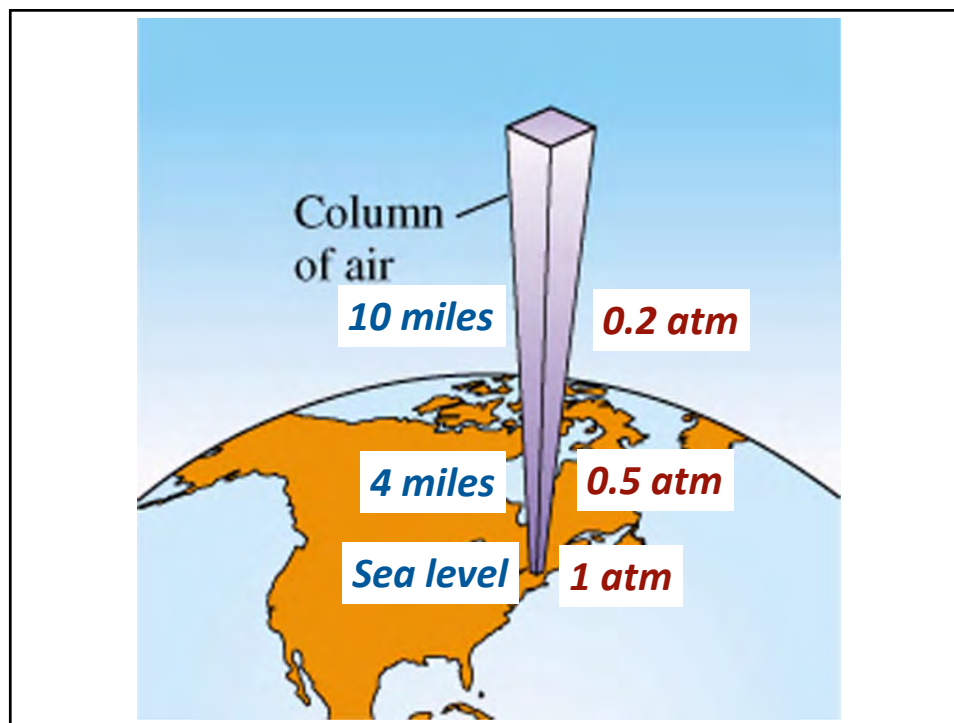
- ✓ how a person can walk on fresh snow without sinking by wearing large snowshoes.
- ✓ how a person cuts with little effort when using a sharp knife.

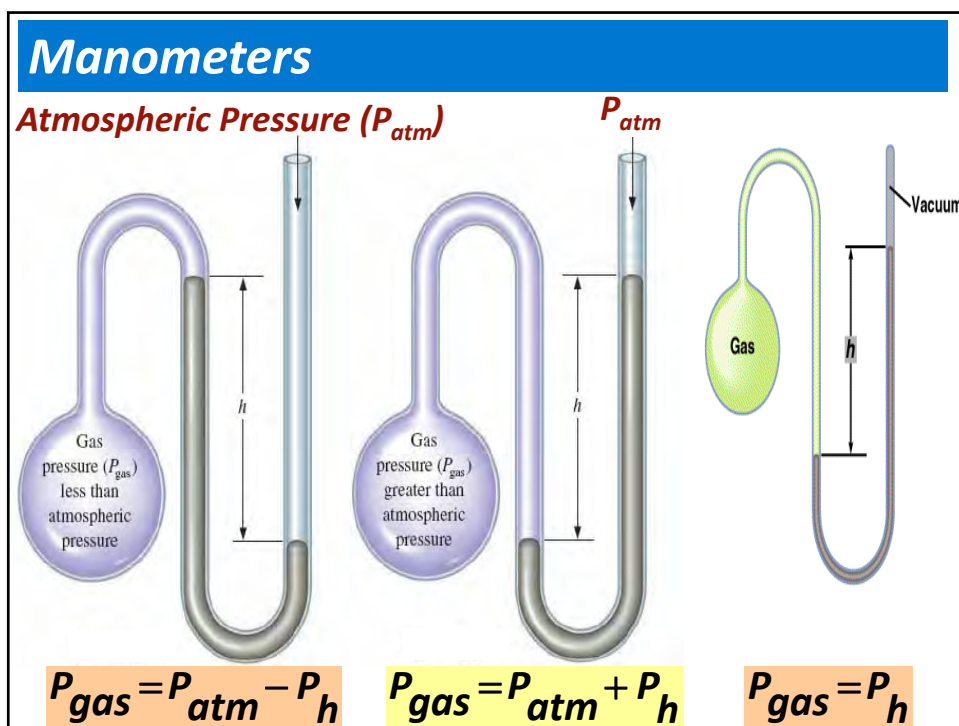
Pressure

- ✦ A gas mixes completely with any other gas.
- ✦ Gases exert pressure on its surroundings.
- ✦ A device to measure atmospheric pressure, **the barometer**, was invented in 1643 by an Italian scientist named **Evangelista Torricelli** (1608–1647), who had been a student of **Galileo**.
- ✦ Torricelli's barometer is constructed by filling a glass tube with liquid mercury and inverting it in a dish of mercury



At sea level the height of this column of mercury averages 760 mm.





- In **CGS** system, P is measured in **dyne cm^{-2}**
- The **standard atmosphere** is the pressure exerted by a **76 cm** high column of mercury of **density $13.6 g cm^{-3}$** in a place where the acceleration due to **gravity is $980 cm s^{-2}$** .

$$\begin{aligned}
 \text{Pressure (1 atm)} &= \frac{\text{Force}}{\text{Area}} = \frac{\text{Mass} \times \text{Acceleration}}{\text{Area}} = \\
 &= \frac{\text{Volume} \times \text{density} \times \text{Acceleration}}{\text{Area}} = \\
 &= \text{Length} \times \text{density} \times \text{Acceleration} = \\
 &= 76 \text{ cm} \times 13.6 \text{ g cm}^{-3} \times 980 \text{ cm s}^{-2} \\
 &= 1.01325 \times 10^6 \text{ g cm}^{-1} \text{ s}^{-2} \text{ (dyne cm}^{-2}\text{)}
 \end{aligned}$$

Pressure

- In **SI** system, P is measured in N m^{-2} (**Pa: Pascal**)

$$\begin{aligned} \text{Pressure (1 atm)} &= \frac{\text{Force}}{\text{Area}} = \\ & \text{Length} \times \text{density} \times \text{Acceleration} = \\ & 0.76 \text{ m} \times 1.36 \times 10^4 \text{ kg m}^{-3} \times 9.8 \text{ m s}^{-2} \\ & 1.01325 \times 10^5 \text{ kg m}^{-1} \text{ s}^{-2} (\text{N m}^{-2}) (\text{Pa}) \end{aligned}$$

$$\begin{aligned} 1 \text{ atm} &= 1.0325 \text{ bar} = 760 \text{ mmHg} = 760 \text{ torr} = \\ & 101,325 \text{ N/m}^2 = 101,325 \text{ Pa} \end{aligned}$$

Exercise (Pressure conversion)

- The pressure of a gas is measured as 49 torr. Represent this pressure in both atmospheres and pascals?

$$49 \text{ torr} \times \frac{1 \text{ atm}}{760 \text{ torr}} = 6.4 \times 10^{-2} \text{ atm}$$

$$6.4 \times 10^{-2} \text{ atm} \times \frac{101,325 \text{ Pa}}{1 \text{ atm}} = 6.5 \times 10^3 \text{ Pa}$$

The state of a gas can be fully described in terms of **4 variables** (**Mass, Volume, Pressure, Temperature**). By knowing 3 of them, the fourth can be calculated

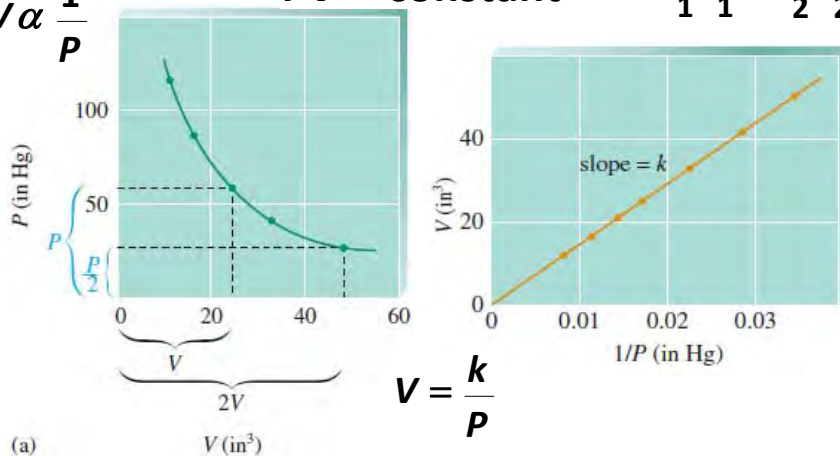
Boyle's Law

At a constant temperature, the volume of a fixed amount of gas is inversely proportional to its pressure.

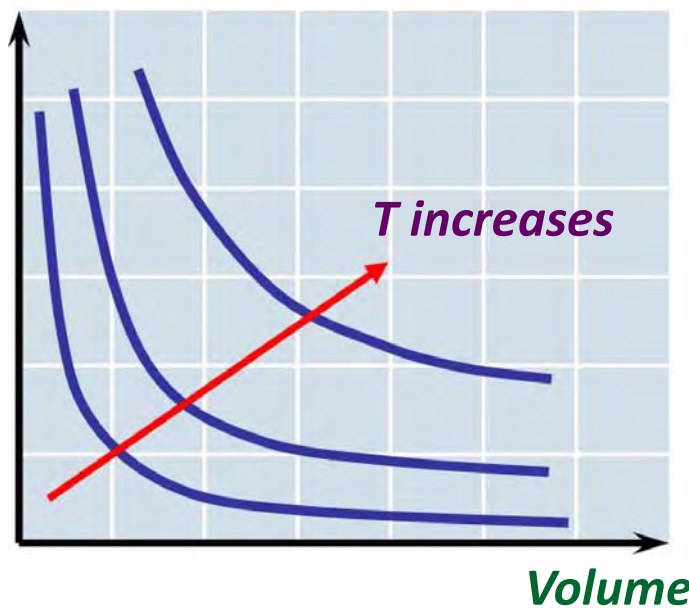
$$V \propto \frac{1}{P}$$

$$PV = \text{constant}$$

$$P_1 V_1 = P_2 V_2$$

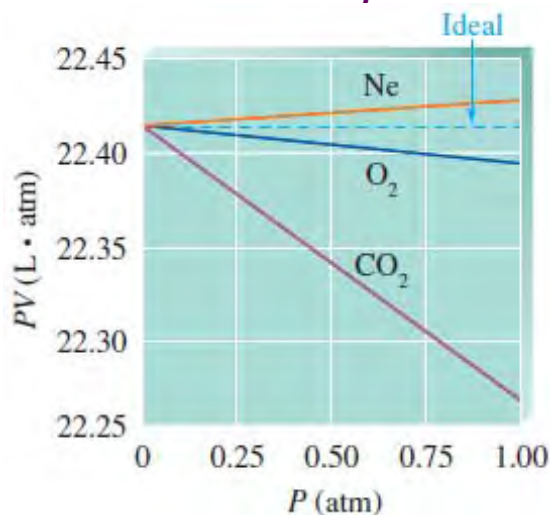


Pressure



Boyle's Law holds precisely only at very low pressures

- Measurements at higher pressures reveal that PV is not constant but varies as the pressure is varied



Exercise

Sulfur dioxide (SO_2), a gas that plays a central role in the formation of acid rain, is found in the exhaust of automobiles and power plants. Consider a 1.53 L sample of gaseous SO_2 at a pressure of $5.6 \times 10^3 \text{ Pa}$. If the pressure is changed to $1.5 \times 10^4 \text{ Pa}$ at a constant temperature, what will be the new volume of the gas?

Solution

$$P_1 = 5.6 \times 10^3 \text{ Pa} \quad \longrightarrow \quad V_1 = 1.53 \text{ L}$$

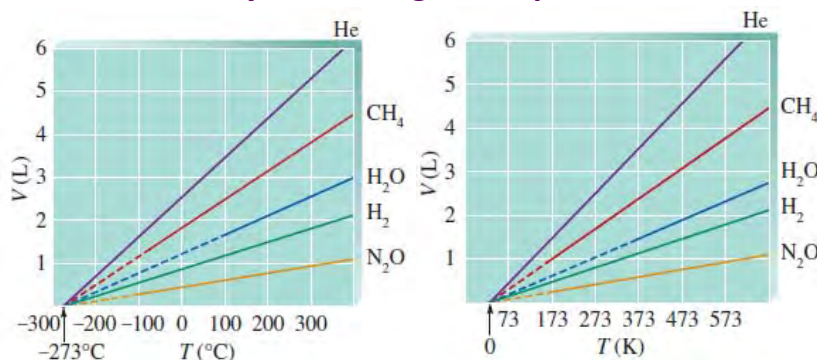
$$P_2 = 1.5 \times 10^4 \text{ Pa} \quad \longrightarrow \quad V_2 = ? \text{ L}$$

$$P_1 V_1 = P_2 V_2 \quad V_2 = \frac{P_1 V_1}{P_2} = \frac{5.6 \times 10^3 \cancel{\text{Pa}} \times 1.53 \text{ L}}{1.5 \times 10^4 \cancel{\text{Pa}}} = 0.57 \text{ L}$$

V decreases ✓

Charles's Law

The volume of a gas at a constant pressure increases linearly with the gas temperature



✓ **Different Slopes:** because of different numbers of moles of gas.

✓ **Volumes of gases extrapolate to zero at the same temperature, $-273^{\circ}\text{C} = 0\text{ K}$ (absolute Zero), $\text{K} = ^{\circ}\text{C} + 273$**

$$V \propto T$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\frac{V}{T} = k$$

Exercise

A sample of gas at 15°C and 1 atm has a volume of 2.58 L . What volume will this gas occupy at 38°C and 1 atm ?

Solution

P and $n = \text{constant}$

$$V_1 = 2.58\text{ L} \longrightarrow T_1 = 15^{\circ}\text{C} + 273 = 288\text{ K}$$

$$V_2 = ?\text{ L} \longrightarrow T_2 = 38^{\circ}\text{C} + 273 = 311\text{ K}$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$V_2 = \frac{V_1 T_2}{T_1} = \frac{2.58\text{ L} \times 311\text{ K}}{288\text{ K}} = 2.79\text{ L}$$

V increases ✓

Avogadro's Law

Equal volumes of gases at the same temperature and pressure contain the same number of "particles."

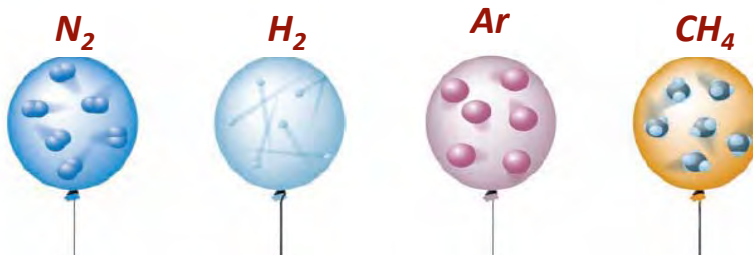
OR

$$V \propto n$$

$$\frac{V}{n} = k$$

$$\frac{V_1}{n_1} = \frac{V_2}{n_2}$$

For a gas at constant temperature and pressure, the volume is directly proportional to the number of moles



Exercise

Suppose we have a 12.2 L sample containing 0.50 mole of oxygen gas (O_2) at a pressure of 1 atm and a temperature of 25°C. If all this O_2 were converted to 0.33 mole of ozone (O_3) at the same temperature and pressure, what would be the volume of the ozone?

P and $T = \text{constant}$

Solution

$$V_1 = 12.2L \quad \longrightarrow \quad n_1 = 0.50 \text{ mol } O_2$$

$$V_2 = ?L \quad \longrightarrow \quad n_2 = 0.33 \text{ mol } O_3$$

$$\frac{V_1}{n_1} = \frac{V_2}{n_2} \quad V_2 = \frac{V_1 n_2}{n_1} = \frac{12.2L \times 0.33 \text{ mol}}{0.50 \text{ mol}} = 8.1L$$

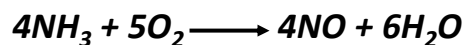
V decreases ✓

Exercise

Ammonia burns in oxygen to form nitric oxide (NO) and water vapor. How many volumes of NO are obtained from one volume of ammonia at the same temperature and pressure?

P and T = constant

Solution



At constant T and P



The Ideal Gas Law

Boyle's law: $V = \frac{k}{P}$ (constant T, n)

Charles's law: $V = bT$ (constant P, n)

Avogadro's law: $V = an$ (constant T, P)

$$V = R \left(\frac{Tn}{P} \right)$$

$$PV = nRT$$

An equation of state for a gas

R : Universal gas constant = 0.08206 L atm/K mol

This equation is mostly obeyed at low pressures and high temperatures

Universal Gas Constant

$$R = \frac{PV}{nT} = \frac{1 \text{ atm} \times 22.414 \text{ L}}{1 \text{ mol} \times 273.15 \text{ K}} =$$

$$0.082057 \text{ L atm K}^{-1} \text{ mol}^{-1}$$

$$= 82 \text{ mL atm K}^{-1} \text{ mol}^{-1}$$

$$= 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$$

$$= 2.0 \text{ cal K}^{-1} \text{ mol}^{-1}$$

Dalton's Law of Partial Pressures

"For a mixture of gases in a container, the total pressure exerted is the sum of the pressures that each gas would exert if it were alone"

Assuming ideal behavior

$$\begin{aligned} P_{\text{Total}} &= P_1 + P_2 + P_3 + \dots \\ &= \frac{n_1 RT}{V} + \frac{n_2 RT}{V} + \frac{n_3 RT}{V} + \dots \\ &= \left(n_1 + n_2 + n_3 + \dots \right) \frac{RT}{V} = \frac{n_{\text{Total}} RT}{V} \end{aligned}$$

Dalton's Law

🌸 The **pressure** exerted by an ideal gas is **not affected** by the **identity (composition)** of the gas particles. **This reveals:**

- ▶ The volume of the individual gas particle must not be important, and
- ▶ The forces among the particles must not be important.

Exercise

Mixtures of helium and oxygen can be used in scuba diving tanks to help prevent "the bends." For a particular dive, 46 L He at 25°C and 1.0 atm and 12 L O₂ at 25°C and 1.0 atm were pumped into a tank with a volume of 5.0 L. Calculate the partial pressure of each gas and the total pressure in the tank at 25°C.

Solution

$$n_{\text{He}} = \frac{(1.0 \text{ atm})(46 \text{ L})}{(0.08206 \text{ L} \cdot \text{atm}/\text{K} \cdot \text{mol})(298 \text{ K})} = 1.9 \text{ mol}$$

$$n_{\text{O}_2} = \frac{(1.0 \text{ atm})(12 \text{ L})}{(0.08206 \text{ L} \cdot \text{atm}/\text{K} \cdot \text{mol})(298 \text{ K})} = 0.49 \text{ mol}$$

Calculate the partial pressure for each gas in the tank

$$P_{\text{He}} = \frac{(1.9 \text{ mol})(0.08206 \text{ L} \cdot \text{atm}/\text{K} \cdot \text{mol})(298 \text{ K})}{(5 \text{ L})} = 9.3 \text{ atm}$$

$$P_{O_2} = \frac{(0.49 \text{ mol})(0.08206 \text{ L} \cdot \text{atm}/\text{K} \cdot \text{mol})(298 \text{ K})}{(5 \text{ L})} = 2.4 \text{ atm}$$

$$P_T = P_{He} + P_{O_2} = 9.3 + 2.4 = 11.7 \text{ atm}$$

Mole fraction, χ

The **ratio** of the number of moles of a given component in a mixture to the total number of moles in the mixture.

$$\chi_1 = \frac{n_1}{n_T} = \frac{n_1}{n_1 + n_2 + n_3 + \dots} = \frac{(V/RT)P_1}{(V/RT)(P_1 + P_2 + P_3 + \dots)}$$

$$= \frac{P_1}{(P_1 + P_2 + P_3 + \dots)} = \frac{P_1}{P_T}$$

► **The mole fraction of each component in a mixture of ideal gases is directly related to its partial pressure**

$$\chi_2 = \frac{n_2}{n_T} = \frac{P_2}{P_T}$$

$$\sum_i \chi_i = 1$$

Example

- The partial pressure of oxygen was observed to be 156 torr in air with a total atmospheric pressure of 743 torr. Calculate the mole fraction of O₂ present at 25°C?

Answer

$$\chi_{O_2} = \frac{P_{O_2}}{P_T} = \frac{156 \text{ torr}}{743 \text{ torr}} = 0.210$$

Homework

A rigid 9.50 L flask contained a mixture of 3.00 moles of hydrogen (H₂) gas, 1.00 moles of oxygen (O₂) gas, and enough neon (Ne) gas so that the partial pressure of neon in the flask was 3.00 atm. The temperature was 27°C.

- 1) Calculate the total pressure in the flask.
- 2) Calculate the mole fraction of oxygen in the flask.
- 3) Calculate the density in (g mL⁻¹) of the mixture in the flask
- 4) The gas mixture is ignited by a spark and the reaction below occurs until one of the reactants is totally consumed.



Give the mole fraction of all species present in the flask at the end of the reaction.