

1 International Journal of Modern Physics E
2 Vol. 27, No. 10 (2018) 1850086 (13 pages)
3 © World Scientific Publishing Company
4 DOI: 10.1142/S0218301318500866



5 **Possible mechanisms for production of slow target fragments**

6 A. Abdelsalam
7 *Mohamed EL-Nadi-High Energy Lab, Physics Department,*
8 *Faculty of Science, Cairo University, Giza, Egypt*
9 *Abdallaham@hotmail.com*

10 M. S. El-Nagdy
11 *Physics Department, Faculty of Science,*
12 *Helwan University, Helwan, Egypt*
13 *Physicshelwan@yahoo.com*

14 A. M. Abdalla* and A. Saber†
15 *Mathematics and Physics Engineering Department,*
16 *Faculty of Engineering in Shoubra,*
17 *Banha University, Cairo, Egypt*
18 **a_abdalla65@hotmail.com*
19 *†nasser.s2009@yahoo.com*

20 Received 2 April 2018
21 Revised 12 August 2018
22 Accepted 12 October 2018
23 Published

24 In this paper, we investigate the possible mechanisms, which are responsible for the
25 production of slow target fragments with energy ≤ 400 MeV that are emitted from inter-
26 actions of ^{28}Si nucleus with emulsion nuclei at energy 14.6 GeV per nucleon. Angular
27 distributions of slow fragments are compared with the corresponding results from colli-
28 sions of ^1H , ^3He , ^4He , ^7Li and ^{12}C with emulsion at the energy range 2.2–3.7 A GeV.
29 We investigate the effects of both projectile energy and mass number on the angular
30 distributions for slow secondary charged fragments called gray and black track produc-
31 ing particles. The average emission angles are found to be 64° and 82° for gray and
32 black tracks, respectively. These values are nearly constant for all compared experi-
33 ments. There are two different mechanisms of gray particle production in forward and
34 backward directions while there is a single symmetric mechanism for black particles in
35 both directions. The temperatures are found to be 58 and 6 MeV for systems of emis-
36 sions for gray and black particles, respectively. There are strong effects of target size on
37 those mechanisms. The emission system of these particles becomes slower and shows low
38 temperature with the increase in volume of target nucleus.

39 *Keywords:* Slow fragments; angular distribution; forward and backward emission angles.

40 PACS Number: 25.75.-q

*Corresponding author.

A. Abdelsalam et al.

1 **1. Introduction**

2 Heavy ion collisions, with energy above few GeV per nucleon, are suitable condi-
3 tions for studying the fine properties of nuclear matter. It gives information on
4 the properties at high temperatures such as density, mechanism of nuclear frag-
5 mentations and initial structure of the nucleus. Much works have been performed
6 both experimentally and theoretically for such investigations because it is more
7 complicated due to the possible formation of new states of non-thermal equilib-
8 rium. Searching for unusual signals from formation, other intermediate nuclear
9 states and their properties consider as very important tool for studying the new
10 phases of the nuclear materials. These new states¹ are produced during interac-
11 tions between nucleons of the interacting nuclei with sufficient collision energies.
12 Its physical properties play the major role and control the characteristics of sec-
13 ondary particles. Studying the behavior of interactions helps to get some important
14 information about the dynamics of the collisions. In experiments, it is impossible
15 to measure all parameters that describe the kinematic of the interactions but it
16 can be calculated from theoretical models, which are assumed according to the
17 predictions of different assumptions. One of the experimental parameters that is
18 used to describe the nucleus–nucleus collisions is the angular distributions of fission
19 fragments.² This parameter is an important probe and it can describe the possible
20 mechanisms of fragmentation for both projectile, target nuclei, and investigate the
21 particular flow of the observables and production of secondary particles. In addi-
22 tion, it describes the formation and decay of some intermediate stages of interacting
23 nuclei. The main aim of this work is studying experimental behavior of the angular
24 distributions of slow and heavy fission fragments produced from interactions of sil-
25 icon ions with composite target of emulsion nuclei at energy 14.6 GeV per nucleon.
26 In previous work² analysis of the experimental results concluded that the angular
27 distributions of secondary fragments are sensitive to entrance channel parameters
28 as well as the statistical aspects of intermediate system as it evolves in time. In
29 this work, the obtained data will be studied in terms of the prediction of the sta-
30 tistical model^{3,4} to investigate the mechanism responsible for secondary particle
31 production.

32 **2. Statistical Model**

33 Statistical model defines a mathematical relationship between collections of vari-
34 ables, each variable being a vector of readings of a specific trait on the samples in
35 an experiment. It explains in what way a variable depends on other variables in the
36 study. Statistical model gives mathematical formulation, which embodies a set of
37 assumptions concerning the generation of some sample data. This formulation cor-
38 relates some of expected and other random variables. The assumptions embodied
39 by statistical model generate a set of probability distributions some of which may be
40 adequate to the experiment results than other models. The distribution of emitted
41 secondary particles as a function of the emission angle θ , which are measured from

Possible mechanisms for production of slow target fragments

1 direction of incident projectile, is one of the important experimental parameters
 2 that describes the temperature and mechanism responsible for particle emission.
 3 To study this mechanism, we will use statistical model for Maxwell distribution³
 4 for secondary emitted particle and their multiplicities according to their momentum
 5 as (let $c = 1$)

$$\frac{d^2N}{dPd\mu} \propto P^2 \exp\left\{-\frac{(P^2 - 2M\bar{\beta}_{\parallel}P_{\mu})}{P_o^2}\right\}, \quad (1)$$

6 where β_{\parallel} , is the longitudinal velocity of the particle-emitting system. $\mu = \cos\theta$,
 7 where θ is the laboratory angle between the momentum of the fragment of mass
 8 M and the momentum of the initial projectile, and $P_o = \sqrt{2ME_o}$, where E_o is the
 9 characteristic energy per particle in the hypothetical moving system. Equation (1)
 10 would be modified when it is expressed in terms of range of the tracks and angle
 11 of emissions or μ , where the two quantities are measured in the experiment. Good
 12 approximation is applied for particle production according to the angle of emis-
 13 sion into forward and backward emissions with predicted ratio F/B , and rational
 14 velocity χ_o , where

$$\chi_o = \frac{\beta_{\parallel}}{\beta_o} = \frac{\bar{\beta}_{\parallel}}{\beta_o} \quad (2)$$

15 which is the ratio of the longitudinal velocity of the center of mass, β_{\parallel} , to the
 16 characteristic spectral velocity β_o , of the fragmenting system. When the angular
 17 distributions are measured without regard to fragment velocity, $dN/d\mu$ becomes a
 18 function of the single fitting parameter χ_o only where

$$\frac{dN}{d\mu} \approx \exp\left(\frac{4}{\sqrt{\pi}}\chi_o\mu\right), \quad (3a)$$

$$\frac{F}{B} \approx \exp\left(\frac{4}{\sqrt{\pi}}\chi_o\right). \quad (3b)$$

19 Hence,

$$\frac{dN}{d\mu} \approx \left(\frac{F}{B}\right)^{\mu}, \quad (3c)$$

$$\frac{dN}{d\theta} \approx \sin\theta \left(\frac{F}{B}\right)^{\cos\theta}. \quad (3d)$$

20 The values of F/B were obtained in the experiment and Eq. (3a) was a suitable
 21 approximation of the exact expression $dN/d\mu$.

22 3. Experimental Details

23 The data, which are used in this work, are the experimental results of nucleus-
 24 nucleus collisions using the nuclear photo-emulsion detector. The details of these
 experiments and primary results are published in Refs. 5–7. Nuclear emulsion plates

A. Abdelsalam et al.

1 are photographic plates with a particularly thick emulsion layer and with uniform
 2 grain size. Emulsion plates record the tracks of charged particles passing through.
 3 Charged particle in emulsion makes many inelastic collisions with atoms such as
 4 silver halides. Atoms along this path lost electrons and became ionized forming
 5 a latent image. After chemical development, they formed image could be seen as
 6 collection of bulbs and specified by grain density g , which characterizes the charge
 7 and velocity of the moving particle. The sensitivity of the used emulsion of FUJI
 8 type for single relativistic charged particle is $g_o = 30$ grains per $100 \mu\text{m}$ of track
 9 length. It exposed to ^{28}Si beam with energy 14.6 A GeV at Brookhaven National
 10 Laboratory (BNL) Alternating Gradient Synchrotron (AGS). The identification of
 11 any secondary charged particles is completed by counting the grain density g and
 12 so the normalized grain density g^* , where $g^* = g/g_o$. According to the magnitudes
 13 of g^* of the tracks, the secondary charged particles are identified and classified into
 14 three groups of tracks. First are particles with tracks appearing as slower tracks
 15 with $g^* \leq 1.4$ corresponding to relativistic particles with velocity $\beta = v/c \geq 0.7$.
 16 Most of these tracks are due to mesons of energy above 50 MeV and small fraction
 17 of fast protons with energy above 400 MeV . The second group of tracks consists of
 18 gray tracks producing particles or gray particles (g -particles) with $1.4 < g^* \leq 10$
 19 and velocity with $0.3 < \beta < 0.7$. These tracks are recoil protons with energy 26 up
 20 to 400 MeV and contaminated deuterons, tritons and helium nuclei. The last group
 21 of tracks is called black track producing particles or black particles (b -particles).
 22 These particles take $g^* \geq 10$ and velocity of $\beta \leq 0.3$. It represents slow protons of
 23 energy below 26 MeV and deuteron, alpha particles and heavy fragments. The gray
 24 tracks and the black tracks are known as tracks of the heavily ionizing particles
 25 with the value of the velocity $\beta < 0.7$. The heavily ionizing particles multiplicity is
 26 denoted by N_h .

27 In this experiment, the target is composite nucleus. The inelastic interactions
 28 are classified into three groups, first is the interaction of ^{28}Si with hydrogen nucleus,
 29 H. The second group includes interactions with light emulsion component carbon,
 30 nitrogen, and oxygen, CNO. The third group includes interactions with heavy emul-
 31 sion components silver and bromine AgBr. The separation of the interactions is
 32 based on the multiplicity N_h . Experimental tools for separation of interactions are
 33 explained in detail in Refs. 8 and 9. Interactions of $N_h \leq 1$ are with hydrogen nuclei
 34 while with CNO are those of $2 \leq N_h \leq 7$. The third interactions with heavy target
 35 group AgBr are of $N_h \geq 8$ with contaminated in range $N_h \leq 7$. The overlapped
 36 region is small to change the results for interactions with CNO group.

37 4. Experimental Results

38 4.1. Angular distribution of gray particles

39 Initially, we study different mechanisms responsible for gray particle (g -particle)
 40 production from interactions of different projectiles with compound target nuclei
 41 of emulsion. Figure 1 shows the experimental results for angular distributions of

Possible mechanisms for production of slow target fragments

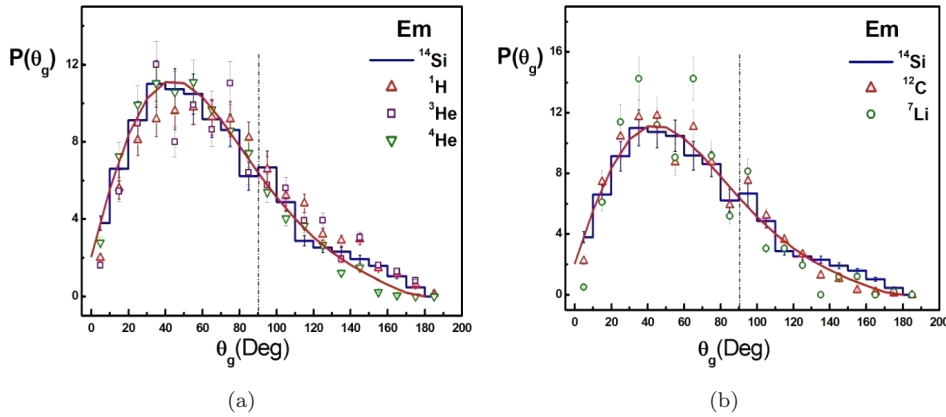


Fig. 1. The angular distribution of gray particles emitted in ^{28}Si -Em interactions at 14.6 A GeV compared with corresponding ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model.

1 g -particles emitted from ^{28}Si -Em at 14.6 A GeV (histogram) compared with the
 2 corresponding distributions at energy 3.7 A GeV for ^1H ,⁴ ^3He ,¹⁰ ^4He ⁴ in (a), ^7Li
 3 and ^{12}C ¹¹ in (b). Generally, all distributions are in the same trend irrespective
 4 of both projectile energy and mass number. These results explain that the effect
 5 of projectile energy, in this range, is sufficient to make each projectile and target
 6 nuclei in a state of full destruction with limited fragmentation processes. The effect
 7 of projectile mass number on angles of the production system of g -particles is absent
 8 because such mechanism is constant and independent on a number of participant
 9 projectile nucleons.

10 The angular distributions of g -particles for all projectiles can be described by
 11 Rayleigh distribution that is often observed when the overall magnitude of a vector
 12 is related to the directional components. It comes from in-isotropic medium with
 13 two trends observed at separation angle of 90° . The first is the forward emission
 14 at $\theta \leq 90^\circ$ and the second is the backward emission at $\theta > 90^\circ$. In the forward emis-
 15 sion, experimental data is represented by Rayleigh distribution, which is Gaussian-
 16 like distribution, with two symmetric sides. It can describe particle production due
 17 to homogenous source around the average value of the emission angle. The forward
 18 emission mechanism of g -particles production is explained in terms of the effect
 19 of momentum of projectile nucleons on target nucleus to be fragment in the for-
 20 ward angles. The second mechanism is the backward emission which is represented
 21 by exponential decay curve where particles production gradually decreases with
 22 increasing angle of emission. Its behavior is explained as cooling curve of target
 23 nucleus and backward emission is due to evaporated target fragments.¹⁹ These two
 24 trends are observed for the all used projectiles. In Fig. 1, the smooth line represents
 25 the predictions for statistical model according to the fitting shape from Eq. (3d)
 26 when applied for g -particles. The predicted rational velocity χ_g^g , is calculated from

A. Abdelsalam et al.

1 the statistical model by using the following equation

$$\chi_o^g = \frac{\beta_{\parallel g}}{\beta_o} = \cos(\langle \theta_g \rangle). \quad (4)$$

2 It is noticed that within experimental errors the distribution predicted by statistical
 3 model is in good agreement with experimental data. The mean value of the emission
 4 angles $\langle \theta_g \rangle$ for gray particles is defined as the medium angle, i.e., the angle at
 5 which half of the number of the specified particles is emitted. It is compared with
 6 the different projectiles in the range of energy 3.7–14.6 A GeV and magnitudes of
 7 the parameter χ_o^g and $\beta_{\parallel g}$ are given in Table 1. The comparison shows that these
 8 parameters are nearly constant and independent on projectile mass number which
 9 reflects the constancy of the mechanisms which are responsible for emission of this
 10 particles. From Table 1 and Fig. 1 it is noticed that, the constancy in the values of
 11 $\langle \theta_g \rangle \sim 64^\circ$, independent of the variation of the projectile mass number as well as
 12 incident energy. The rational velocity for the system of gray particle emission χ_o^g is
 13 nearly equal to 0.5 for all interactions. The emitting system of the g -particles is fast
 14 with typical longitudinal velocities $\beta_{\parallel g}^g \approx 0.13$ –0.20. The anisotropic ratio $(F/B)_g$
 15 is the ratio of the number of forward fragments of g -particles to that emitted in the
 16 backward fragment for different projectiles are given in Table 1. These ratios appear
 17 constant and range between 2.5 to 3.9. It proves that all predictions of statistical
 18 models for all given projectiles are similar and controlled by two fixed mechanisms
 19 for g -particle production. In Ref. 10, similar conclusions were observed for oxygen
 20 and sulfur at 200 A GeV.

21 In this section, we explain the effect of target size on the angular distribution
 22 of g -particles. In Sec. 3 and in our previous work^{20,21} we stated that the emulsion
 23 is compound target and collisions are classified into three main groups according
 24 to multiplicity of heavily ionizing the secondary charged particle N_h . These parti-
 25 cles are pure target fragments and can be considered as experimental parameters,
 26 which describe the degree of overlapping of projectile and target nuclei. First group

Table 1. The average values of the emission angles of the gray particles $\langle \theta_g \rangle$ in different interactions with emulsion at energy 3.7–14.6 A GeV, in addition $^{28}\text{Si} + \text{CNO}$ and $^{28}\text{Si} + \text{AgBr}$. The rational velocity of the system χ_o^g , ratio $(F/B)_g$ and longitudinal velocity $\beta_{\parallel g}$ based on statistical model.

Projectile	$\langle \theta_g^\circ \rangle$	χ_o^g	$(F/B)_g$	$\beta_{\parallel g}$	Ref.
^1H	67.80 ± 1.2	0.59	3.80 ± 0.20	0.20	4
^4He	62.80 ± 3.1	0.48	3.00 ± 0.30	0.17	4
^6Li	64.90 ± 2.2	0.47	2.90 ± 0.20	0.16	12
^7Li	63.50 ± 2.0	0.45	3.82 ± 0.20	0.16	11 and 13
^{12}C	64.00 ± 1.9	0.55	3.51 ± 0.20	0.19	4
^{22}Ne	63.70 ± 1.6	0.55	3.50 ± 0.12	0.19	13
^{28}Si	63.30 ± 1.4	0.55	3.52 ± 0.16	0.19	4, 14–16
^{28}Si	64.76 ± 2.1	0.49	3.05 ± 0.27	0.17	Present work
$^{28}\text{Si} + \text{CNO}$	62.44 ± 5.2	0.46	2.84 ± 0.24	0.16	Present work
$^{28}\text{Si} + \text{AgBr}$	65.56 ± 3.5	0.41	2.54 ± 0.25	0.14	Present work

Possible mechanisms for production of slow target fragments

1 with multiplicity $N_h \leq 1$ includes interactions with hydrogen and low statistics
 2 are excluded from this consideration. Second group includes the interactions with
 3 light emulsion components CNO, where $2 \leq N_h \leq 7$ and are considered as gentle
 4 interactions. Third group includes interactions of ^{28}Si with heavy emulsion nuclei
 5 AgBr. It is considered as hard interactions and characterized by $N_h \geq 8$. Fig-
 6 ure 2 shows the angular distributions of g -particles emitted from interactions of
 7 ^{28}Si with CNO compared with ^1H , ^3He and ^4He in Fig. 2(a) and ^{12}C and ^7Li
 8 in Fig. 2(b). Figure 3 shows the corresponding distributions for collisions with AgBr.
 9 The figures show that the angular distributions for both two-target components are
 10 different from each other. For gentle interactions, most probable angles are in for-
 11 ward hemisphere and minimum probability for angles in backward direction because
 12 the effect of projectile momentum in forward direction strongly appears for inter-
 13 actions with light target nuclei. In hard interactions, fluctuation is limited in the
 14 forward direction while most fluctuations are observed in the backward hemisphere
 15 which gradually decrease with angles to reach minimum multiplicity in opposite
 16 direction ($\theta = 180^\circ$). This is noticed in ratio $(F/B)_g$ in Table 1. For gentle inter-
 17 actions, its value is 2.84 ± 0.24 while it decreases to 2.54 ± 0.25 for hard interactions.
 18 In addition, the average angle of emission for gentle interactions is $62.44^\circ \pm 5.18$
 19 and it increases to $65.56^\circ \pm 3.51$ for hard interactions. The rational parameter χ_g^g
 20 decreases with target mass number, i.e., the system responsible for emission of g -
 21 particles becomes slower. This is expected due to the effect of target size on the
 22 velocity of the system responsible for particle production. This becomes sufficient
 23 for projectile nucleons to lose its momentum up to be emitted as recoil fragments
 24 in wide range of angles. This results are noticed for all compared and different
 25 projectiles, which proved that there are two different mechanisms responsible for

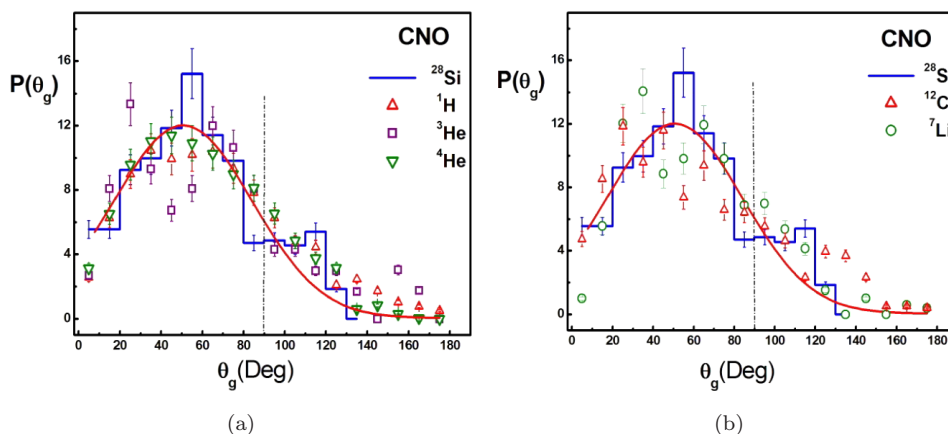


Fig. 2. The angular distribution of gray particle emitted ^{28}Si interactions at 14.6 A GeV with light emulsion component CNO compared with the corresponding distribution for ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model using Gaussian-fitting shape.

A. Abdelsalam et al.

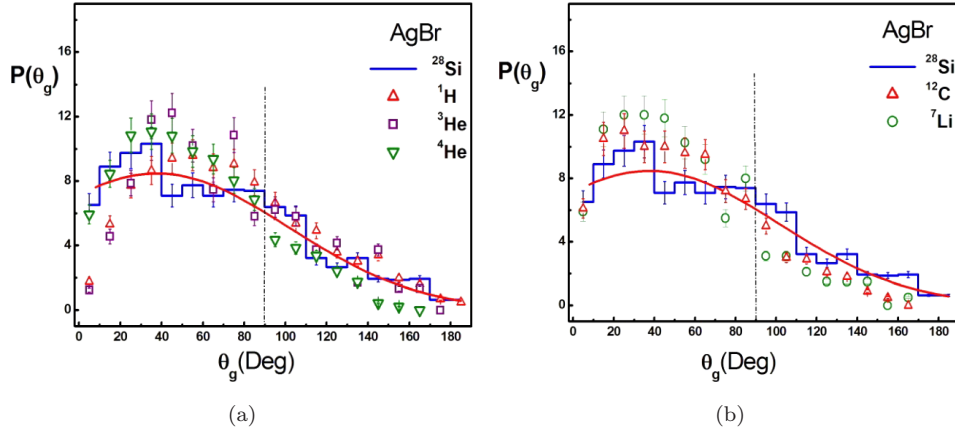


Fig. 3. The angular distribution of gray particle emitted ^{28}Si interactions at 14.6 A GeV with heavy emulsion component AgBr compared with the corresponding distribution for ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model using Gaussian-fitting shape.

- 1 g -particles production one for forward emission and other for backward direction.
- 2 The effect of the target size is observed on the two production mechanisms.

3 4.2. Angular distribution of black particles

- 4 Secondly, we study the angular distributions and properties of the mechanism
- 5 responsible for the production of slow particles, which appear as black tracks in
- 6 emulsion experiments. These particles play an important role in describing the
- 7 nature of the interactions between projectile and target nuclei. Figure 4 shows the

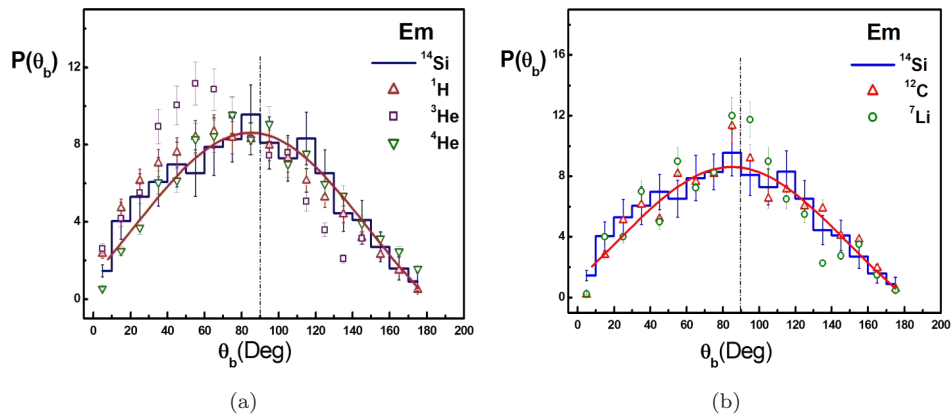


Fig. 4. The angular distribution of black particles emitted in ^{28}Si -Em interactions at 14.6 A GeV compared with corresponding ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model.

Possible mechanisms for production of slow target fragments

Table 2. The average values of the emission angles of the black particles $\langle\theta_b\rangle$ in different interactions at energy 2.2–14.6 A GeV, in addition to the rational χ_o^b velocity of the system, the ratio $(F/B)_b$ and longitudinal velocity $\beta_{\parallel b}$ of black particle emission, on the basis of statistical model.

Projectile	$\langle\theta_b\rangle$	χ_o^b	$(F/B)_b$	$\beta_{\parallel b}$	Ref.
^1H	85.3 ± 1.9	0.11	1.28 ± 0.1	0.013	4
^4He	83.0 ± 3.8	0.13	1.35 ± 0.1	0.015	4
^6Li	82.2 ± 2.6	0.12	1.30 ± 0.2	0.018	12
^7Li	81.3 ± 2.3	0.11	1.28 ± 0.1	0.013	11 and 13
^{12}C	79.5 ± 2.4	0.11	1.27 ± 0.1	0.013	4
^{28}Si	83.3 ± 1.2	0.20	1.59 ± 0.1	0.023	14, 18, 19
^{28}Si	83.5 ± 1.9	0.11	1.26 ± 0.1	0.013	Present work
$^{28}\text{Si} + \text{CNO}$	79.9 ± 3.7	0.17	1.48 ± 0.1	0.019	Present work
$^{28}\text{Si} + \text{AgBr}$	84.9 ± 2.2	0.09	1.22 ± 0.1	0.010	Present work

1 angular distributions of the b -particles compared to those recorded for ^1H , ^3He and
 2 ^4He in (a) and for ^7Li and ^{12}C in (b). The average values of the emission angle for
 3 different interactions are given in Table 2. Within experimental errors, the angular
 4 distributions for using projectiles are in the same trend and the mean emission
 5 angles approximately take fixed value. It concludes that the mechanism responsible
 6 for emission of b -particles is independent of projectile size and its energy because
 7 these particles are pure target fragments. It is noted that the spectrum seems to be
 8 symmetric around the peak position, which is near the mean value $\langle\theta_b\rangle$.

9 The feature of this spectrum implies that the emission of b -particles, in forward
 10 and backward hemispheres, tends to be symmetric in both directions where the
 11 maximum particle multiplicity approaches the region of $\theta_{\text{lab}} \sim 90^\circ$. The similarity
 12 for particle emission is different from that observed for g -particles. It proves that,
 13 for both directions, there is a single mechanism responsible for b -particle produc-
 14 tion. This mechanism is independent of projectile mass number and interaction
 15 energy. It is characterized by isotropic thermal excitation of target nucleus and the
 16 system temperature is uniformly distributed over most target nucleons. In the last
 17 stage of collision, target nucleus begins to cool by the emission of heavy fragments
 18 along the wide range of angles, which are independent of the direction of incident
 19 projectile. The fragments are massive particles with minimum energy and residual
 20 target nucleus.

21 Angular distribution of b -particles emitted from ^{28}Si –Em interactions at energy
 22 14.6 A GeV compared with the corresponding prediction of statistical model
 23 (smooth line) are shown in Fig. 4. The predicted distribution by the model shows
 24 good agreement with experimental results. The model predicts the rational velocity
 25 χ_o^b and longitudinal velocity $\beta_{\parallel b}$ where their values are given in Table 2. The magni-
 26 tude of β_o^b is taken to be ~ 0.115 from Ref. 4. We can conclude that the constancy in
 27 the values of $\langle\theta_b\rangle \sim 83^\circ$ is independent of the variation of projectile mass number as
 28 well as projectile energy. The rational velocity χ_o^b tends to be ~ 0.13 for the system
 29 of black particles. The ratio $(F/B)_b$ for different projectiles is more concise in small

A. Abdelsalam et al.

1 range 1.2–1.6 which supports the prediction of the fixed mechanism of b -particle
 2 production and different from that for the gray system. The emitting system of
 3 the b -particles is slow and has a typical longitudinal velocities $\beta_{||}^b$ whose range
 4 is $\beta_{||}^b \sim 0.010$ – 0.023 . The temperature of the emitting system can be calculated
 5 using $T = 1/2M\beta_0^2$ where M is the nucleon mass. Its value for black particles is
 6 found to be 6 MeV per nucleon. It is approximately equal to the binding energy per
 7 nucleon at the normal state of the nucleus. The corresponding temperature for the
 8 system responsible for g -particle production is calculated by using the magnitude of

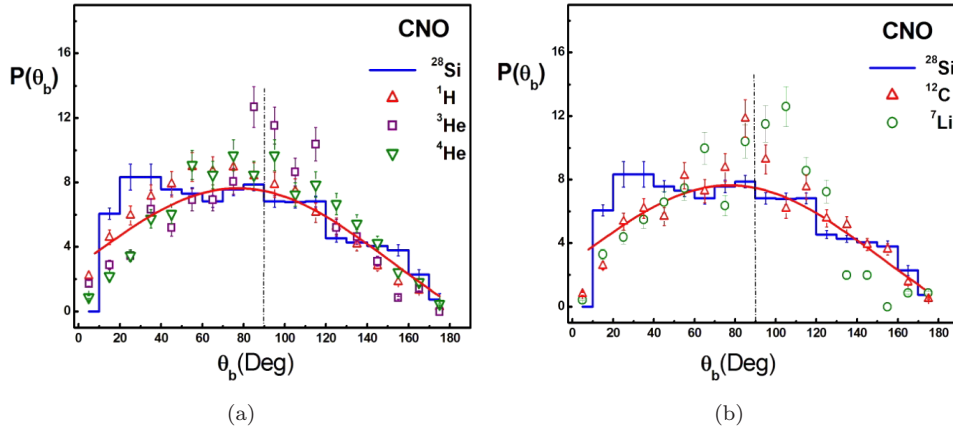


Fig. 5. The angular distribution of black particle emitted ^{28}Si interactions at 14.6 A GeV with light emulsion component CNO compared with the corresponding distribution for ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model using Gaussian-fitting shape.

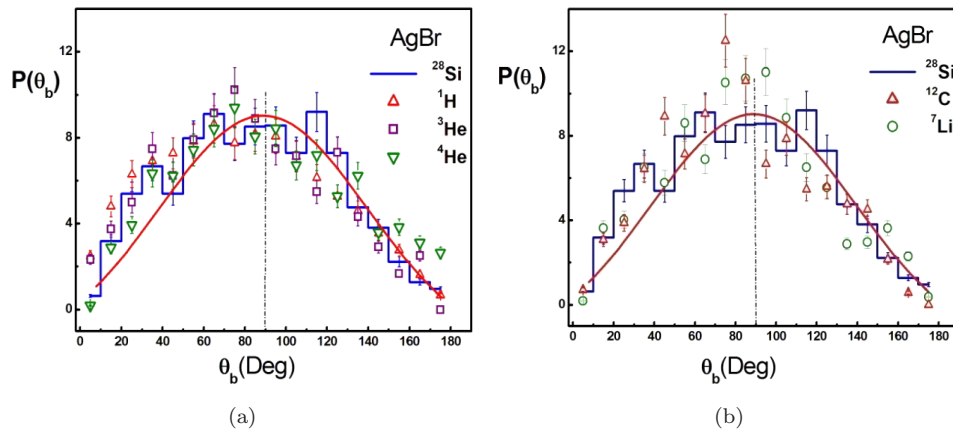


Fig. 6. The angular distribution of black particle emitted ^{28}Si interactions at 14.6 A GeV with light emulsion component AgBr compared with the corresponding distribution for ^1H , ^3He and ^4He in (a) and with ^{12}C and ^7Li in (b). Smooth curve represents the corresponding prediction of the statistical model using Gaussian-fitting shape.

Possible mechanisms for production of slow target fragments

1 $\beta_o^g \sim 0.35$ (Ref. 4). The value is found to be 58 MeV per nucleon, which is sufficient
 2 for nucleon to make a cascade of secondary interactions before escaping from hot
 3 size of interactions.

4 The final point of interest is the effect of target size on angular distributions of
 5 b -particles. The effects for both two-target components are shown in Fig. 5 for gentle
 6 interaction with CNO and Fig. 6 for hard interaction with AgBr. The experimental
 7 and predicted parameters are given in Table 2.

8 It is noticed that there is clear effect of target size on mechanism responsible
 9 for black particle productions. For gentle interactions, the emission of evaporated
 10 b -particles begins from angles 20° and most probabilities are nearly constant in
 11 forward direction up to 90° while in backward directions, the probability begins,
 12 fast decreasing with angles. This could be explained by assuming that for small tar-
 13 get size (CNO), there is strong effect of projectile momentum on the angles of the
 14 emission of black fragments. This effect disappears for hard interactions and distri-
 15 butions show clear symmetric around middle angle. The mean values of emission
 16 angles are about 85° and 80° for hard and gentle interactions, respectively. These
 17 values proved that the angular distributions are more symmetric for hard inter-
 18 actions and slightly deviate for gentle interactions. The ratio $(F/B)_b$ and rational
 19 parameter χ_o^b increase from 1.22 ± 0.07 and 0.09 for hard interactions to 1.48 ± 0.08
 20 and 0.17 for gentle interactions, respectively. It proves that the system of emission
 21 for black particles becomes slower and shows low temperature with increasing mass
 22 number of the interacting target nucleus.

23 5. Conclusions

- 24 (1) The angular distributions of each of gray and black particles are independent
 25 of each projectile mass number and projectile energy.
- 26 (2) The angular distribution for g -particles indicates two mechanisms for particle
 27 production: one for forward particle which takes homogenous Gaussian distri-
 28 bution due to the effect of projectile momentum and the second in backward
 29 emissions due to recoil protons from both projectile and target nucleons.
- 30 (3) The angular distributions of gray and black particles, which emitted from ^{28}Si -
 31 Em interactions at energy 14.6 A GeV, are well described by the statistical
 32 model.
- 33 (4) The experimental parameters such as mean values of the emission angles for
 34 g -particles are $\langle\theta_g\rangle \sim 64^\circ$ and for b -particles are $\langle\theta_b\rangle \sim 83^\circ$. These values are
 35 nearly constant for the corresponding collisions using different mass number
 36 of the projectiles in the range of collisions energies 2.2–14.6 A GeV.
- 37 (5) The predicted rational velocity by statistical model χ_o which describes the
 38 system that is responsible for emission of the secondary particles is nearly
 39 equal to 0.5 for g -particles and tends to be ~ 0.13 for b -particles.
- 40 (6) The velocity of the emitting system is described by the parameter $\beta_{//}$, where
 the emitting system for g -particles is fast and with typical longitudinal

A. Abdelsalam et al.

- 1 velocities $\beta_{||}^g \sim 0.13-0.20$ while it is slow for emission of b -particle in the
 2 range $\beta_{||}^b \sim 0.008-0.019$.
- 3 (7) The anisotropic ratio F/B is found to be 2–3 for the system that is respon-
 4 sible for g -particle productions while it is 1.2–1.6 for the system of b -particle
 5 production.
- 6 (8) The temperatures of the system, which is responsible for emission of secondary
 7 slow fragments, are found to be 58 MeV for g -particle productions while 6 MeV
 8 for b -particles.
- 9 (9) The angular distributions for both gray and black particles depend on the size
 10 of the target nucleus. Most of the emission angles for g -particles are mainly in
 11 forward angles for small target nuclei CNO, while it is in symmetry distribu-
 12 tions between forward and backward hemispheres for heavy target AgBr.
- 13 (10) The systems, which are responsible for gray and black particle productions,
 14 become slower and show low temperature with increasing target mass number.

15 Acknowledgment

16 The authors would like to thank P.L. Jain for supplements of the irradiated emulsion
 17 plates.

18 References

- 19 1. S. K. Karn, R. S. Kaashal and Y. K. Mathur, *Z. Phys. C* **72** (1996) 297.
 20 2. A. Abdelsalam, M. Šumbera and S. Vokál, *JINR Report* (Dubna) EL-82–509 (1982).
 21 3. H. H. Hackmann, H. J. Crawford, D. E. Greiner, P. J. Lindstrom and W. Wilson
 22 Lamce, *Phys. Rev. C* **17** (1978) 1651.
 23 4. A. Abdelsalam, *Phys. Scr.* **47** (1993) 124.
 24 5. M. El-Nadi, M. S. El-Nagdy, N. Ali-Mossa, A. Abdelsalam, A. M. Abdalla and A. A.
 25 Hamed, *J. Phys. G, Nucl. Phys.* **25** (1999) 1169.
 26 6. M. El-Nadi et al., *Eur. Phys. J. A, Hadrons Nuclei* **10** (2001) 177.
 27 7. M. El-Nadi et al., *J. Phys. G, Nucl. Part. Phys.* **28** (2002) 1251.
 28 8. J. R. Florian et al. Report submitted to the meeting of division of particles and fields,
 29 Berkely, California (1973).
 30 9. A. Abdelsalam, *JINR Report* (Dubna) EL-81–623 (1981).
 10. A. Abdelsalam, M. S. El-Nagdy, N. Rashed, B. M. Badawy and E. El-Falaky, *J. Nucl.*
 11. *Radiat. Phys.* **2** (2007) 49.
 12. M. El-Nadi, A. Abdelsalam, M. M. Sherif, N. Ali-Moussa, M. S. El-Nagdy, *IL Nuovo*
 13. *Cimento* **107** (1994).
 14. M. I. Adamovich et al., *LUND Report LUIP 8906* (1989).
 15. M. M. Sherif, *IL Nuovo Cimento* **109A** (1996) 1135.
 16. M. El-Nadi, A. Abdelsalam and N. Ali-Moussa, *Int. J. Mod. Phys. E.* **3** (1994) 811.
 17. Z. Dong-Hai and LI. Hui-Ling, *Chin. Phys. C* **33** (2009) 345.
 18. A. Abdelsalam, B. M. Badawy and E. El-Falaky, *Can. J. Phys.* **85** (2007) 837.
 19. A. Abdelsalam, M. S. El-Nagdy, A. M. Abdalla and A. Saber, *Int. J. Mod. Phys. E*
 20. **24** (2015) 1550084.
 21. M. El-Nadi, A. Abdelsalam, N. Ali-Moussa, Z. Abou-Moussa, Kh. Abdel-Waged,
 22. W. Osman and Badawy, *IL Nuovo Cimento A* **111** (1998) 1243.

AQ: Kindly
 provide
 page
 number.

Possible mechanisms for production of slow target fragments

- 1 19. M. El-Nadi, A. Abdelsalam and N. Ali-Moussa, *Radiat. Phys. Chem.* **47** (1996) 681.
- 2 20. M. S. El-Nagdy, A. Abdelsalam, B. M. Badawy, P. I. Zarubin, A. M. Abdalla and
- 3 A. Saber, *Chin. Phys. Lett.* **35** (2018) 032501.
- 4 21. M. S. El-Nagdy, A. Abdelsalam, B. M. Badawy, P. I. Zarubin, A. M. Abdalla, M. Nabil
- 5 Yasin, A. Saber, M. M. Mohamed and M. M. Ahmed, *J. Phys. Commun.* **2** (2018)
- 6 035010.