

THERMODYNAMICS OF MATERIALS CHE701

ANSWER TO PROBLEMS

CHAPTER 1

1.

$$\Delta H = \int_{300}^{1000} 110 + 16.21 \times 10^{-3}T - 25.79 \times 10^5 T^{-2} \cdot dT = 78358 \text{ J. mol}^{-1}$$
$$\equiv \mathbf{78.36 \text{ kJ. mol}^{-1}}$$

2. First, we must obtain the following data:

- Specific heats of components ($\text{J. mol}^{-1}\text{K}^{-1}$)

For CaO: $C_p = 49.95 + 4.88 \times 10^{-3}T - 8.25 \times 10^5 T^{-2}$ (NIST WebBook)

For CO₂: $C_p = 24.99 + 5.518 \times 10^{-2}T - 1.366 \times 10^5 T^{-2}$ (NIST WebBook)

For CaCO₃: $C_p = 83.43$ (MatWeb)

- Heats of formation of components (kJ. mol^{-1}) from Table (1.2)

For CaO: $\Delta H_f^0 = -636$

For CO₂: $\Delta H_f^0 = -394$

For CaCO₃: $\Delta H_f^0 = -1206$

Heat of reaction at standard conditions: $\Delta H_R^0 = (-636 - 394) - (-1206) = 176$

$$\Delta H_1 = \int_{1000}^{298} 83.43 \cdot dT = -58567.86 \text{ J. mol}^{-1} \equiv -58.57 \text{ kJ. mol}^{-1}$$

$$\Delta H_R^0 = 176 \text{ kJ. mol}^{-1}$$

$$\Delta H_3 = \int_{298}^{1000} (49.95 + 24.99) + (4.88 + 55.18) \times 10^{-3}T - (8.25 + 1.366) \times 10^5 T^{-2} \cdot dT = 77705 \text{ J. mol}^{-1} \equiv 77.705 \text{ kJ. mol}^{-1}$$

Hence: $\Delta H_{1000} = \Delta H_1 + \Delta H_R^0 + \Delta H_3 = \mathbf{195.135 \text{ kJ. mol}^{-1}}$

3. $dS = \frac{\delta Q}{T}$

Since the process is isothermal, then, from the first law: $\delta Q = p \cdot dV$

$$dS = \frac{p \cdot dV}{T}$$

For an ideal gas: $p = \frac{RT}{V}$

$$dS = \frac{R.dV}{V} \rightarrow \Delta S = \int_{V_1}^{V_2} \frac{R.dV}{V} = R \ln \frac{V_2}{V_1} = R \ln \frac{p_1}{p_2} \quad (\text{Since } p.V = \text{constant})$$

4. $\text{NaCl} (l) \rightarrow \text{NaCl} (l)$: 973 K to 1074 K:

$$\Delta S_1 = \int_{973}^{1074} \frac{c_p(l).dT}{T} = 61.5 \ln \frac{1074}{973} = 6.074 \text{ J.mol}^{-1}\text{K}^{-1}$$

$$\text{NaCl} (l) \rightarrow \text{NaCl} (s): \text{at } 1074 \text{ K: } \Delta S_2 = \frac{-27950}{1074} = -26.02 \text{ J.mol}^{-1}\text{K}^{-1}$$

$\text{NaCl} (s) \rightarrow \text{NaCl} (s)$: 1074 K to 973 K:

$$\Delta S_3 = \int_{1074}^{973} \frac{c_p(s).dT}{T} = \int_{1074}^{973} \frac{50.dT}{T} = 50 \ln \frac{973}{1074} = -4.94 \text{ J.mol}^{-1}\text{K}^{-1}$$

Thus, the change in entropy = $6.074 - 26.02 - 4.94 = -24.886 \text{ J.mol}^{-1}\text{K}^{-1}$

To obtain the entropy change of surroundings, one first must calculate the amount of heat transferred to the surroundings which is the amount of heat produced by the cycle.

$$\text{NaCl} (l) \rightarrow \text{NaCl} (l): 973 \text{ K to } 1074 \text{ K: } \Delta H_1 = \int_{973}^{1074} C_{pl}.dT = 61.5 \times (1074 - 973) = 6211.5 \text{ J.mol}^{-1}$$

$$\text{NaCl} (l) \rightarrow \text{NaCl} (s): \text{at } 1074 \text{ K: } \Delta H_2 = -27950 \text{ J.mol}^{-1}$$

$\text{NaCl} (s) \rightarrow \text{NaCl} (s)$: 1074 K to 973 K:

$$\Delta H_3 = \int_{1074}^{973} 50.dT = -5050 \text{ J.mol}^{-1}$$

Thus, the heat transferred to surroundings = $6211.5 - 27950 - 5050 = -26788.5 \text{ J.mol}^{-1}$.

Hence, the heat gained by the surroundings = $26788.5 \text{ J.mol}^{-1}$

$$\text{The change in entropy of surroundings} = \Delta S_{surr} = \frac{26788.5}{973} = 27.53 \text{ J.mol}^{-1}\text{K}^{-1}$$

(We note that the total change in entropy = $-25.1 + 27.53 = 2.43 \text{ J.mol}^{-1}\text{K}^{-1} > 0$)

5. The pressure is increased from $p_1 = 101325$ to $p_2 = 1013250000 \text{ Pa}$

$$dS = \frac{\delta Q}{T}$$

Since the process is isothermal, then, from the first law: $\delta Q = p.dV$

$$\Delta S = \frac{p.dV}{T} = - \int_{p_1}^{p_2} \frac{V\beta p.dp}{T} = \frac{-0.005 \times 0.762 \times 10^{-11} \times 0.5 \times [1013250000^2 - 101325^2]}{300} = -65.19 \text{ J.K}^{-1}.$$

6. To get the value of ΔH , we use the relation: $\left(\frac{\partial\left(\frac{\Delta G}{T}\right)}{\partial\left(\frac{1}{T}\right)}\right)_P = \Delta H = \left(\frac{\partial\left(\frac{\Delta G}{T}\right)}{\partial T}\right)_P \cdot -T^2$

$$\frac{\Delta G}{T} = -16.8T^{-1} + 0.00368 - 0.0721T^{-1} \ln T$$

$$\left(\frac{\partial\left(\frac{\Delta G}{T}\right)}{\partial T}\right)_P = 16.8T^{-2} - 0.0721(-T^{-2} \cdot \ln T + T^{-1}T^{-1})$$

$$= 16.8T^{-2} - 0.0721T^{-2}(1 - \ln T) \rightarrow \Delta H = -T^2T^2[16.8 - 0.0721(1 - \ln T)]$$

$$\text{At } 400\text{K: } \Delta H = [-16.8 + 0.0721(1 - \ln 400)] = \mathbf{-17.16 \text{ kJ.mol}^{-1}}$$

To get the value of ΔS , we first obtain the value of ΔG at 400:

$$\Delta G = -16.8 + 0.00368 \times 400 - 0.0721 \ln 400 = -15.76$$

$$\Delta G = \Delta H - T \cdot \Delta S \rightarrow$$

$$-15.76 = -17.16 - 400\Delta S \rightarrow \Delta S = \mathbf{-0.0035 \text{ kJ.mol}^{-1}\text{K}^{-1} \equiv -3.5 \text{ J.mol}^{-1}\text{K}^{-1}}$$

7. Since the molecules are **similar**, we apply the expression: $W = \frac{n+i-1!}{n!i-1!}$

$$W = \frac{100+50-1!}{100!50-1!} = \frac{149!}{100!49!}$$

$$\text{Hence: } \ln W = \ln 149! - \ln 100! - \ln 49!$$

Applying Stirling approximation:

$$\ln W = (149 \ln 149 - 149) - (100 \ln 100 - 100) - (49 \ln 49 - 49) = 94.37$$

$$\text{Hence } W = e^{94.37} = \mathbf{9.66 \times 10^{40}}$$

8. $dG = V \cdot dp - S \cdot dT$ Since T is constant, hence: $dG = V \cdot dp = \frac{RT}{p} dp$

$$\text{Therefore: } \Delta G = \int_1^{100} \frac{8.314 \times 298}{p} dp = 8.314 \times 298 \times \ln \frac{100}{1} = \mathbf{11409.6 \text{ J.mol}^{-1}}$$

CHAPTER 2

1. $\Delta T = 1090 - 1083 = 7 \text{ K}$

$$\Delta H_t = 13590 \text{ J.mol}^{-1}$$

$$T_t = 1083 + 273 = 1356 \text{ K}$$

$$\text{Atomic volume of solid} = V_1 = \frac{63.55}{8.95} = 7.1 \text{ cm}^3.\text{mol}^{-1} \equiv 7.1 \times 10^{-6} \text{ m}^3.\text{mol}^{-1}$$

$$\text{Atomic volume of liquid} = V_2 = \frac{63.55}{7.93} = 8.014 \text{ cm}^3.\text{mol}^{-1} \equiv 8.014 \times 10^{-6} \text{ m}^3.\text{mol}^{-1}$$

$$\Delta V = 0.914 \times 10^{-6} \text{ m}^3.\text{mol}^{-1}$$

$$\text{Substituting in the equation } \frac{\Delta p}{\Delta T} = \frac{\Delta H_t}{\Delta V.T_t}$$

$$\frac{\Delta p}{7} = \frac{13590}{0.914 \times 10^{-6} \times 1356}$$

$$\text{Hence: } \Delta p = 76755872 \text{ Pa} \equiv \mathbf{756.7 \text{ atm}}$$

2.

log p	-7	-6	-5	-4	-3	-2	-1	0	1	2
$T \text{ K}$	1020	1075	1172	1243	1374	1498	1669	1805	2023	2255
ln p	0.00098	0.00093	0.00085	0.0008	0.00073	0.00067	0.0006	0.00055	0.00049	0.00044
$1/T$	-16.121	-13.818	-11.515	-9.212	-6.909	-4.606	-2.303	0	2.303	4.606

The plot between ln p and $1/T$ yields a straight line of equation $\ln p = -\frac{37693}{T} + 20.84$

This slope (37693) corresponds to a latent heat of vaporization = $313.4 \text{ kJ.mol}^{-1}$

The normal boiling point is the boiling point at 1 atm $\equiv$ 1013.2 millibar.

Substitution in the equation of the straight line, we get: $T_{\text{normal b}} = \mathbf{2708 \text{ K}}$
(Actually 2743 K).

3. The reaction under study is: $\text{C} (a = 0.0038) = \text{C} (a = 0.00572)$

The free energy of carbon at its standard state = 0, hence:

$$\Delta G = \Delta G^0 + RT \ln \frac{0.00572}{0.0038} = 0 + 8.314 \times 1600 \ln \frac{0.00572}{0.0038} \rightarrow \Delta G = \mathbf{5440.3 \text{ J.mol}^{-1}}$$

The positive sign of free energy change indicates that this increase cannot take place spontaneously.

4. The reaction is: $\text{Cu} (a = 1) = \text{Cu} (a)$

The activity of Cu in solution = $\frac{p}{p^0}$.

The vapor pressure in solution = 0.03 mmHg $\equiv \frac{0.03 \times 1.013 \times 10^5}{760} = 4 \text{ Pa}$

Hence, $a = \frac{4}{975} = 0.0041$

$$\Delta G = \Delta G^0 + RT \ln \frac{0.0041}{1} = 0 + 8.314 \times 873 \ln \frac{0.0041}{1} \rightarrow \Delta G = -\mathbf{39896 \text{ J}}$$

The negative sign of free energy change indicates that dissolution can take place spontaneously.

5. The reaction is: $\text{CaCO}_3 (\text{s}) = \text{CaO} (\text{s}) + \text{CO}_2 (\text{g})$

Since $p_{\text{CO}_2} = 0.0005 \text{ atm}$, hence the calcination temperature can be calculated from:

$$p_{\text{CO}_2} = 4.137 \times 10^7 e^{-\frac{20474}{T}}$$

$$0.0005 = 4.137 \times 10^7 e^{-\frac{20474}{T}} \rightarrow \mathbf{T = 814.4 \text{ K}}$$

The two solid phases being at their standard states, the standard free energy change can be written as:

$$\Delta G^0 = -RT \ln p_{\text{CO}_2} = -8.314 \times 814.4 \times \ln 0.0005 = 51465 = \Delta H^0 - T\Delta S^0$$

Calculation of ΔH^0 at 814.4 K:

- Cool CaCO_3 from 814.4 to 298: $\Delta H_1 = 83.48 \times (298 - 814.4) = -43109$
- Reaction at 298 K: $\Delta H_R = -394 - 635.5 - (-1205.6) = 176.1 \text{ kJ/mol}^{-1}$
- Heat $\text{CaO} + \text{CO}_2$ to 814.4 K: $\Delta H_1 = (47.5 + 36) \times (814.4 - 298) = 43119.4$

$$\Delta H^0 \text{ at } 814.4 \text{ K} = -43.109 + 176.1 + 43.119 = 176.11 \text{ kJ/mol}^{-1}$$

Since $\Delta G^0 = \Delta H^0 - T\Delta S^0$, therefore: $51376 = 176110 - 814.4\Delta S^0$

Hence, $\Delta S^0 = \mathbf{153.16 \text{ J.mol}^{-1}.\text{K}^{-1}}$

6. $\Delta G^0 = -75.7 \times 10^4 - 7.5 \times 1500 \times \log 1500 + 145 \times 1500 = -575231 \text{ J.mol}^{-1}$

$$-575231 = -8.314 \times 1500 \ln K_e \rightarrow \mathbf{K_e = 1.076 \times 10^{20}}$$

$$\left(\frac{\partial \left(\frac{\Delta G}{T} \right)}{\partial \left(\frac{1}{T} \right)} \right)_P = \Delta H = \left(\frac{\partial \left(\frac{\Delta G}{T} \right)}{\partial T} \right)_P \cdot -T^2$$

$$\frac{\Delta G}{T} = -75.7 \times 10^4 T^{-1} - 7.5 \times 0.4343 \ln T + 145$$

$$-\frac{\Delta H}{T^2} = \left(\frac{\partial \left(\frac{\Delta G}{T} \right)}{\partial T} \right)_P = 75.7 \times 10^4 T^{-2} - 7.5 \times 0.4343/T$$

$$\Delta H = -(75.7 \times 10^4 T^{-2} - 7.5 \times 0.4343/T) \times T^2$$

$$\Delta H = -75.7 \times 10^4 + 7.5 \times 0.4343 \times 1500 = -\mathbf{752114 \text{ J.mol}^{-1}}$$

$$1500\Delta S = -752114 - (-575231) \rightarrow \Delta S = -\mathbf{117.9 \text{ J.mol}^{-1}.K^{-1}}$$

$$7. \left(\frac{\partial \ln K_e}{\partial T} \right)_p = \frac{-410000}{8.314 \times T^2} = -49314.4 T^{-2}$$

$$\int_{1500}^{1400} -49314.4 T^{-2} \cdot dT = \ln K_{e,1400} - \ln 8.903 \times 10^{15}$$

$$\ln K_{e,1400} = 39.074 \rightarrow K_{e,1500} = \mathbf{9.33 \times 10^{16}}$$

(Note that the reaction being exothermic, the value of the equilibrium constant has increased on decreasing the temperature).

$$8. \Delta H_R = -1860 + 0.013T, \text{ at } 1000\text{K: } \Delta H_R = -1847 \text{ kJ.mol}^{-1}$$

$$\frac{\Delta H}{T^2} = - \left(\frac{\partial \left(\frac{\Delta G}{T} \right)}{\partial T} \right)_p \rightarrow \frac{\Delta G}{T} = - \int \frac{\Delta H}{T^2} \cdot dT = - \int -1860 T^{-2} + 0.013 T^{-1} \cdot dT$$

$$\frac{\Delta G}{T} = -1860 T^{-1} - 0.013 \ln T + C \rightarrow \Delta G = -1860 - 0.013 T \cdot \ln T + C T$$

$$\text{At } T = 298, \Delta G = -1705 = -1860 - 0.013 \times 298 \times \ln 298 + 298C \rightarrow C = 0.594$$

At 1000K:

$$\Delta G = -1860 - 0.013 \times 1000 \times \ln 1000 + 0.594 \times 1000 = -\mathbf{1355.8 \text{ kJ.mol}^{-1}}$$

$$\Delta G = \Delta H - T\Delta S \rightarrow -1355.8 = -1847 - 1000\Delta S \rightarrow \Delta S = -\mathbf{0.491 \text{ kJ.mol}^{-1}.K^{-1}}$$

9.

	Cu
Melting point K	1358
$\Delta H_m \text{ kJ.mol}^{-1}$	13.26
Boiling point K	2835
$\Delta H_v \text{ kJ.mol}^{-1}$	300.4

For melting:

$$\ln p^0 = \frac{-13260}{8.314T} + C \quad \text{To get the value of } C, \text{ we note that if } p^0 = 1 \text{ atm, } T = 1358$$

$$0 = \frac{-13260}{8.314 \times 1358} + C \rightarrow C = 1.1745$$

$$\ln p^0 = \frac{-13260}{8.314T} + 1.1745 \quad (\text{i})$$

For vaporization:

$$\ln p^0 = \frac{-300400}{8.314T} + C'$$

To get the value of C' , we note that if $p^0 = 1$ atm, $T = 2835$

$$0 = \frac{-300400}{8.314 \times 2835} + C \rightarrow C = 12.745$$

$$\ln p^0 = \frac{-300400}{8.314T} + 12.745 \quad (\text{ii})$$

The following table shows the values obtained by substituting T into equations (i) and (ii)

T K	$\ln p^0$ (i)	$\ln p^0$ (ii)
1400	0.0352	- 13.0635
1600	0.1776	- 9.8375
1800	0.2883	- 7.328
2000	0.377	- 5.321
2200	0.4495	- 3.678
2400	0.5099	- 2.31
2600	0.5610	- 1.1519
2800	0.6048	- 0.1593
2985	0.6401	0.6405

The value of $T = 2985$ K was obtained by using Goal – Seek technique to have the differences between the values of $\ln p^0$ in both columns equal to zero.

For sublimation:

$$\ln p^0 = -\frac{313660}{8.314T} + C''$$

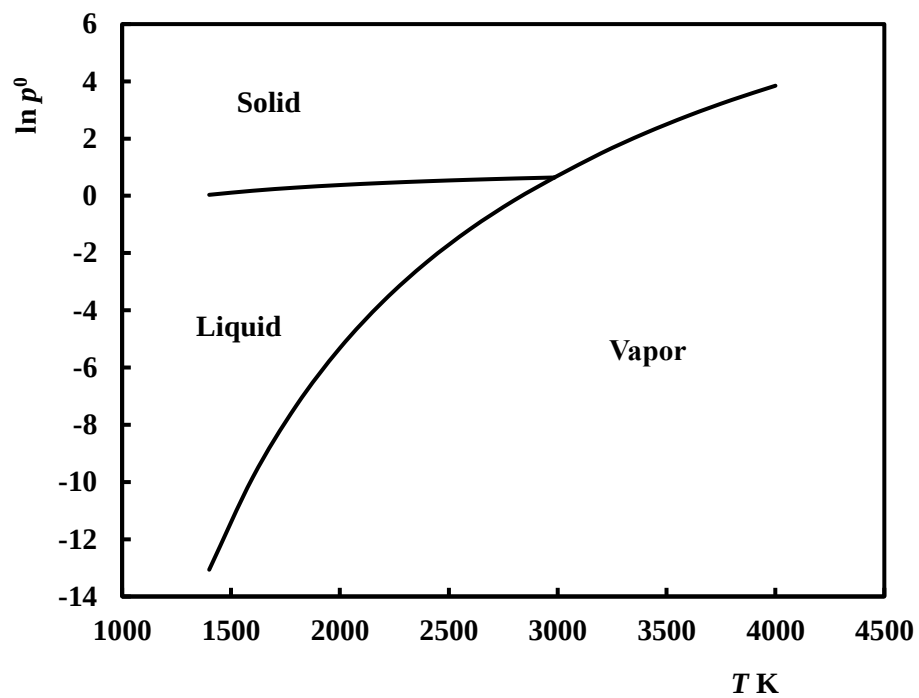
To get the value of C'' , we note that if $\ln p^0 = -0.64$ atm, $T = 2985$

$$-0.64 = \frac{-313660}{8.314 \times 2985} + C'' \rightarrow C'' = 13.279$$

$$\ln p^0 = \frac{313660}{8.314T} + 13.279 \quad (\text{iii})$$

The following table shows the values of $\ln p^0$ obtained from (iii) at $T \geq 2985$ K

2985	0.6399
3200	1.4891
3400	2.1826
3600	2.7991
3800	3.3506
4000	3.8471



CHAPTER 3

$$1. \text{ Moles Ni} = \frac{40}{58.7} = 0.681 \quad \text{Moles Cu} = \frac{100}{63.54} = 1.574$$

$$X_{Ni} = \frac{0.681}{0.681+1.574} = 0.302 \rightarrow X_{Cu} = 0.698$$

$$\Delta S_m = -R(X_A \ln X_A + X_B \ln X_B) = -8.314 \times (0.302 \ln 0.302 + 0.698 \ln 0.698)$$

$$\Delta S_m = \mathbf{5.093 \text{ J.mol}^{-1}.K^{-1}}$$

Since the solution is ideal, then $\Delta H_m = 0$

$$\Delta G_m = \Delta H_m - T\Delta S_m = 0 - 300.\Delta S_m \rightarrow \Delta G_m = \mathbf{-1527.9 \text{ J.mol}^{-1}}$$

2.

X_{Zn}	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
$\Delta G \text{ kJ.mol}^{-1}$	0	-0.28	-0.43	-0.5	-0.57	-0.58	-0.55	-0.5	-0.4	-0.29	0

The expression for dependence of free energy on mol fraction Zn is:

$$\Delta G_m = 2.2483X_{Zn}^2 - 2.2419X_{Zn} - 0.0387$$

We get the slope of tangent at $X_{Zn} = 0.4$:

$$\frac{d(\Delta G_m)}{dX_{Zn}} = 4.4966X_{Zn} - 2.2419 \rightarrow 4.4966 \times 0.4 - 2.2419 = -0.4433$$

$$\text{Equation of tangent at } X_{Zn} = 0.4: \Delta G_m = -0.4433X_{Zn} + C$$

$$\text{At } X_{Zn} = 0.4, \Delta G_m = -0.57 \rightarrow C = -0.3927 \rightarrow \Delta G_m = -0.4433X_{Zn} - 0.3927$$

$$\text{At } X_{Zn} = 0, \Delta G_m = -0.3927 \rightarrow \bar{G}_{Ga} = \mathbf{-0.3927 \text{ kJ.mol}^{-1}}$$

$$\text{At } X_{Zn} = 1, \Delta G_m = -0.8527 \rightarrow \bar{G}_{Zn} = \mathbf{-0.827 \text{ kJ.mol}^{-1}}$$

$$3. p_{BeO}^0 = 4.6 \times 10^{-3} \text{ and } \gamma_{BeO} = 0.91$$

$$a_{BeO} = 0.91 \times 0.02 = 0.0182$$

$$\text{And, since } a_B = \frac{p_B}{p_B^0}$$

Therefore:

$$p_{BeO} = 0.0182 \times 4.6 \times 10^{-3} = 8.37 \times 10^{-5} \text{ atm.}$$

$$\text{Also, } a_{TiO_2} = X_{TiO_2} = 0.98$$

$$p_{TiO_2} = p_{TiO_2}^0 X_{TiO_2}$$

$$p_{TiO_2} = 7.8 \times 10^{-5} \times 0.98 = 7.644 \times 10^{-5} \text{ atm}$$

Hence:

$$p = 8.37 \times 10^{-5} + 7.644 \times 10^{-5} = \mathbf{1.604 \times 10^{-4} \text{ atm.}}$$

$$4. T_{Al} = 660 + 273 = 933K \quad \Delta H_f = 10800 \text{ J.mol}^{-1} \quad X_{Si} = 0.023$$

$$\Delta T_f \approx \frac{RT_f^2}{\Delta H_{fA}} X_B = \frac{8.314 \times 933^2 \times 0.023}{-10800} = -15.4K \text{ (The negative sign is due to freezing)}$$

Therefore, the solution starts melting at $660 - 15.4 = \mathbf{644.6^\circ C}$

$$5. \Delta S_m = -R(X_A \ln X_A + X_B \ln X_B) =$$

$$-8.314 \times (0.4 \ln 0.4 + 0.6 \ln 0.6) = \mathbf{5.595 \text{ J.mol}^{-1}K^{-1}}$$

$$\Delta H_m = 4510X_{NiO}^2 - 4510X_{NiO} = 4510 \times 0.4^2 - 4510 \times 0.4 = -1082.4$$

$$\Delta G_m = \Delta H_m - T\Delta S_m = -1082.4 - 700 \times 5.595 = \mathbf{-4998.9 \text{ J.mol}^{-1}}$$

To get the partial molal enthalpy, we need to get the equation of the tangent at the enthalpy – composition curve at $X_{NiO} = 0.4$

$$\frac{d(\Delta H_m)}{dX_{Ni}} = 9020X_{Ni} - 4510 \rightarrow 9020 \times 0.4 - 4510 = -902$$

$$\cdot \text{ Equation of tangent at } X_{Ni} = 0.4: \Delta H_m = -902X_{Ni} + C$$

$$\text{At } X_{Ni} = 0.4, \Delta H_m = -1082.4 \rightarrow C = -721.6 \rightarrow \Delta H_m = -902X_{Ni} - 721.6$$

$$\text{At } X_{Ni} = 0, \Delta H_m = -721.6 \rightarrow \bar{H}_{MgO} = \mathbf{-721.6 \text{ J.mol}^{-1}}$$

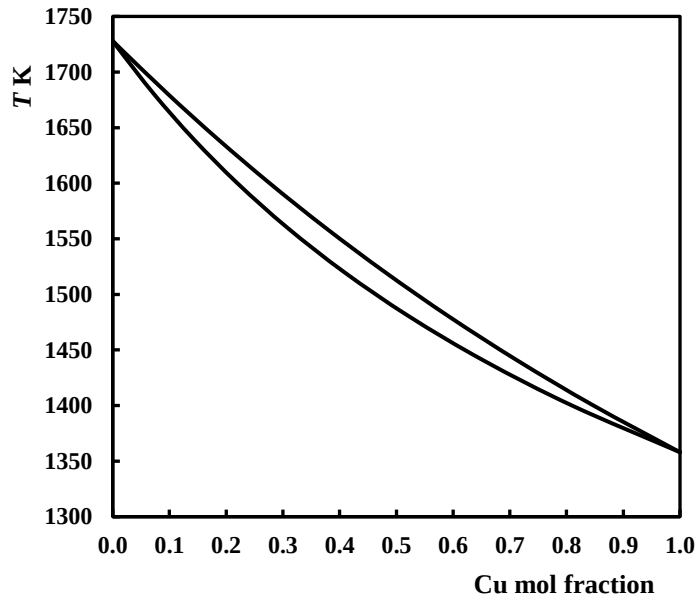
$$\text{At } X_{Ni} = 1, \Delta H_m = -902 - 721.6 \rightarrow \bar{H}_{NiO} = \mathbf{-1623.6 \text{ J.mol}^{-1}}$$

6. The components are written as: Ni = A and Cu = B.

	Ni (A)	Cu (B)
Melting point K	1728	1358
$\Delta H_m \text{ kJ.mol}^{-1}$	17200	13600

T K		1358	1400	1440	1480	1520	1560	1600	1640	1680	1720	1728
$\ln X_L/X_S$			0.046	0.087	0.126	0.162	0.197	0.230	0.262	0.292	0.321	0.326
X_L/X_S			1.047	1.091	1.134	1.176	1.218	1.259	1.299	1.339	1.378	1.386
$\ln(1 - X_L)/(1 - X_S)$			-0.281	-0.222	-0.189	-0.159	-0.130	-0.102	-0.076	-0.051	-0.027	0
$(1 - X_L)/(1 - X_S)$			0.755	0.801	0.828	0.853	0.878	0.903	0.927	0.950	0.973	1
X_S		1	0.810	0.656	0.523	0.408	0.308	0.220	0.142	0.073	0.011	0
X_L		1	0.848	0.715	0.593	0.480	0.375	0.277	0.184	0.098	0.016	0

The corresponding phase diagram is shown in the figure.



7. $\Delta H_m = -20150X_B(1 - X_B)$

The enthalpy of mixing reaches its minimum value as $\frac{d(\Delta H_m)}{dX_B} = 0$

$$\Delta H_m = 20150X_B^2 - 20150X_B \rightarrow \frac{d(\Delta H_m)}{dX_B} = 40300X_B - 20150 = 0 \rightarrow X_B = 0.5$$

$$\Delta S_m = -R(X_A \ln X_A + X_B \ln X_B) =$$

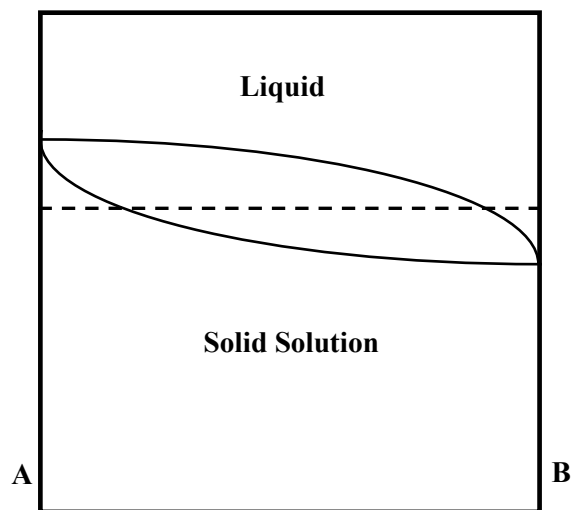
$$-8.314 \times (0.5 \ln 0.5 + 0.5 \ln 0.5) = \mathbf{5.763 \text{ J}\cdot\text{mol}^{-1}\text{K}^{-1}}$$

$$\Delta H_m = -20150 \times (1 - 0.5) = -10075 \text{ J}\cdot\text{mol}^{-1}$$

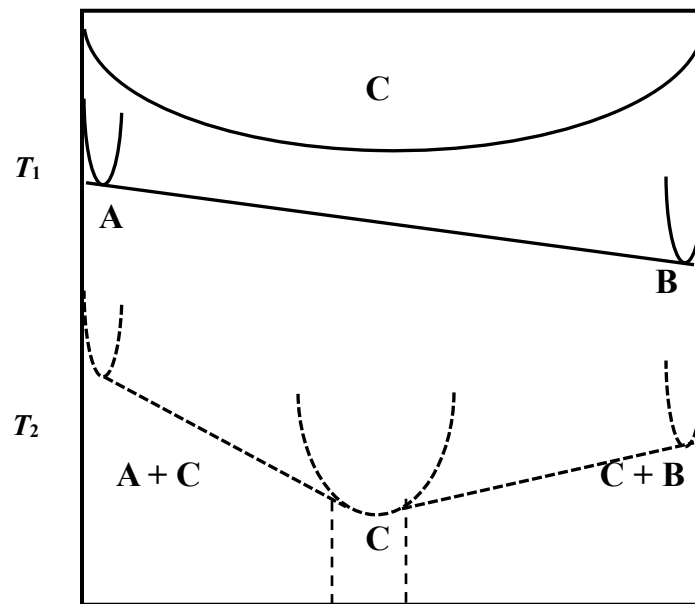
$$\Delta G_m = \Delta H_m - T\Delta S_m \text{ at } T = 1200\text{K}$$

$$\Delta G_m = -10075 - 1200 \times 5.763 = \mathbf{-16990.6 \text{ J}\cdot\text{mol}^{-1}}$$

8.



9.



CHAPTER 4

1. Reaction: $2 \text{Mn}_3\text{O}_4 (\text{s}) = 6 \text{MnO} (\text{s}) + \text{O}_2 (\text{g})$

$$\text{Hence, } \Delta H^0 = 6. \Delta H_{f, \text{MnO}}^0 - 2. \Delta H_{f, \text{Mn}_3\text{O}_4}^0 = \mathbf{465 \text{ kJ.mol}^{-1}}$$

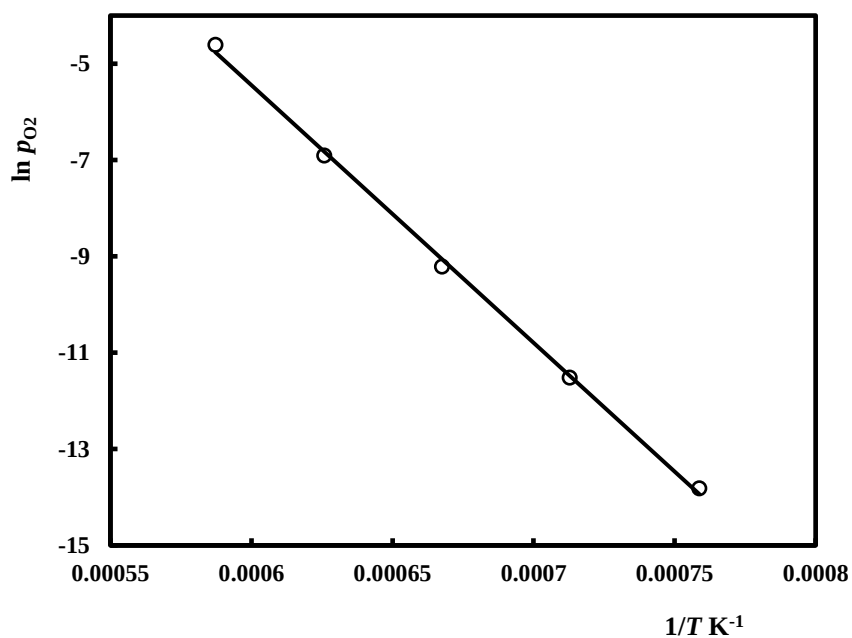
$$\Delta S^0 = 6. \Delta S_{f, \text{MnO}}^0 - 2. \Delta S_{f, \text{Mn}_3\text{O}_4}^0 = \mathbf{117 \text{ J.mol}^{-1}\text{K}^{-1}}$$

p_{O_2}	$\ln p_{\text{O}_2}$	$T^\circ\text{C}$	$1/T \text{ K}^{-1}$
10^{-6}	-13.816	1045	0.000759
10^{-5}	-11.513	1130	0.000713
10^{-4}	-9.2103	1225	0.000668
10^{-3}	-6.9078	1325	0.000626
10^{-2}	-4.6052	1430	0.000587

The $\ln p_{\text{O}_2} - 1/T$ diagram is shown below.

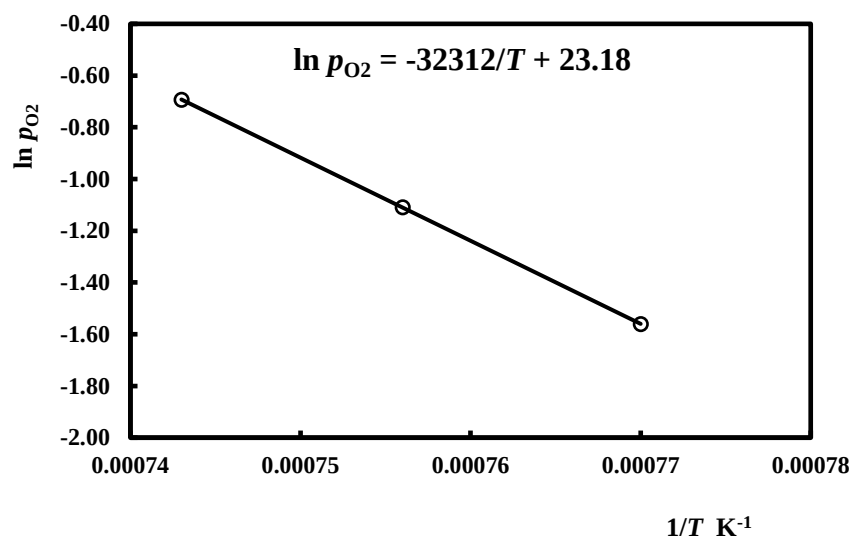
The slope = -53454 corresponding to an enthalpy of reaction = $\mathbf{444.6 \text{ kJ.mol}^{-1}}$

The intercept = 26.64 corresponding to an entropy of reaction = $\mathbf{111.4 \text{ J.mol}^{-1}}$



2.

p_{O_2}	$\ln p_{\text{O}_2}$	$T^\circ\text{C}$	$1/T \text{ K}^{-1}$
0.21	-1.5606	1026	0.00077
0.33	-1.1087	1050	0.000756
0.5	-0.6931	1072	0.000743



The slope = -32312 corresponding to an enthalpy of reaction = **131.31 kJ.mol⁻¹**

The intercept = 23.18 corresponding to an entropy of reaction = **96.9 J.mol⁻¹**

3. The following table can be set:

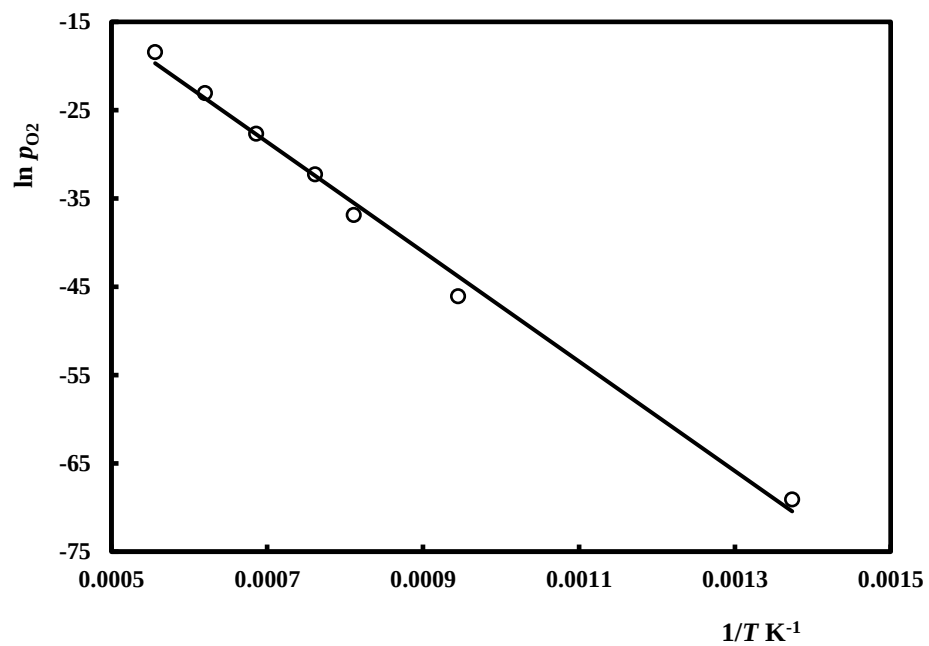
p_{O_2}	$\ln p_{O_2}$	$T^{\circ}\text{C}$	$1/T \text{ K}^{-1}$
10^{-30}	-69.078	455	0.001383
10^{-20}	-46.052	785	0.000950
10^{-16}	-36.841	960	0.000811
10^{-14}	-32.236	1040	0.000762
10^{-12}	-27.631	1185	0.000686
10^{-10}	-23.026	1340	0.000620
10^{-8}	-18.421	1525	0.000556

The plot is shown in the following Figure.

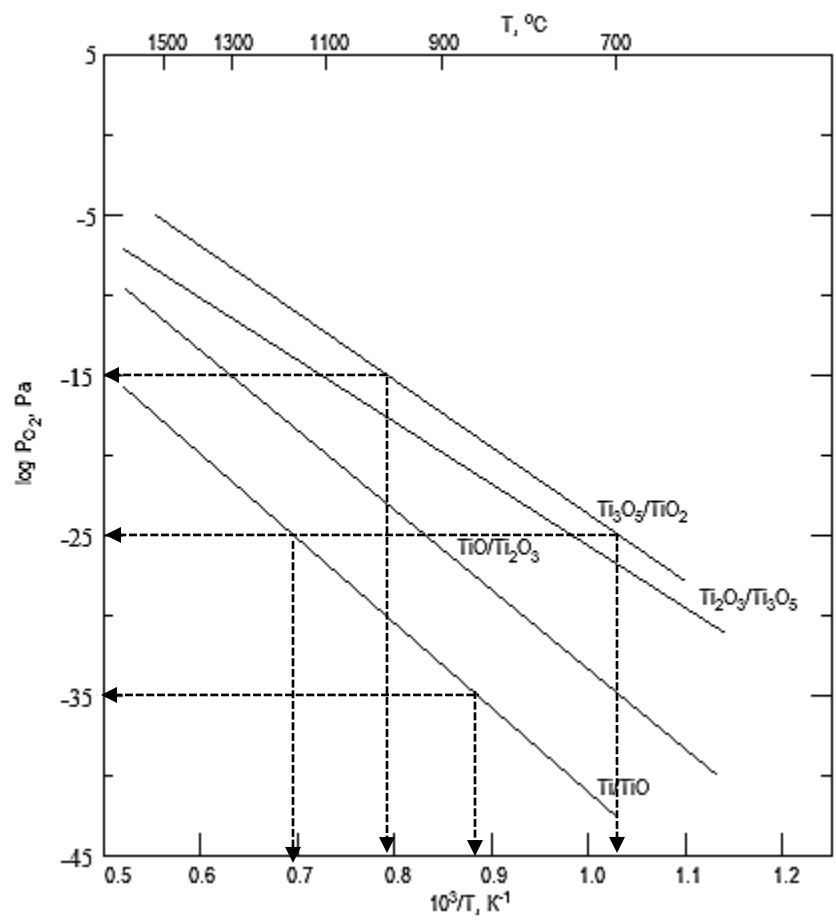
The slope = -60278 corresponding to an enthalpy of reaction = **516.11 kJ.mol⁻¹**

The intercept = 14.31 corresponding to an entropy of reaction = **119 J.mol⁻¹**

The difference with the experimental value of $0 - (-564.3) = 564.3$ amounts to an error of about 8.54%.



4.



For the reaction: $4 \text{TiO}_2 (\text{s}) = 2 \text{Ti}_2\text{O}_3 (\text{s}) + \text{O}_2 (\text{g})$

Two points are chosen on the line and moved to an EXCEL chart:

$$\frac{1}{T} = 0.795 \times 10^{-3}, \ln p_{\text{O}_2} = -2.303 \times 15 \text{ and}$$

$$\frac{1}{T} = 1.034 \times 10^{-3}, \ln p_{\text{O}_2} = -2.303 \times 25$$

$$\text{Slope} = \frac{-\Delta H}{R} = -96360 \rightarrow \Delta H_r = \mathbf{801.2 \text{ kJ.mol}^{-1}}$$

$$\text{Intercept} = \frac{\Delta S}{R} = 42.06 \rightarrow \Delta S_r = \mathbf{349.7 \text{ J.mol}^{-1}\text{K}^{-1}}$$

For the reaction: $2 \text{TiO} (\text{s}) = 2 \text{Ti} (\text{s}) + \text{O}_2 (\text{g})$

Two points are chosen on the line and moved to an EXCEL chart:

$$\frac{1}{T} = 0.696 \times 10^{-3}, \ln p_{\text{O}_2} = -2.303 \times 25 \text{ and}$$

$$\frac{1}{T} = 0.886 \times 10^{-3}, \ln p_{\text{O}_2} = -2.303 \times 35$$

$$\text{Slope} = \frac{-\Delta H}{R} = -121120 \rightarrow \Delta H_r = \mathbf{1008 \text{ kJ.mol}^{-1}}$$

$$\text{Intercept} = \frac{\Delta S}{R} = 26.79 \rightarrow \Delta S_r = \mathbf{222.7 \text{ J.mol}^{-1}\text{K}^{-1}}$$

5. The requested $\ln p_{\text{O}_2}$ vs $1/T$ diagram is shown in the Figure. Its equation takes the form:

$$\ln p_{\text{O}_2} = -\frac{76372}{T} + 4.584$$

