



Name:----- ID: -----

Q1) Represent the following sentences in first-order logic

NOTE: the following translation is not unique

- There are exactly two students studying A.I.
$$\exists x \exists y \text{ std}(x) \wedge \text{study}(x, \text{AI}) \wedge \text{std}(y) \wedge \text{study}(y, \text{AI}) \wedge \neg (x=y)$$
$$\wedge (\forall z) (\text{std}(z) \wedge \text{study}(z, \text{AI}) \rightarrow z=x \vee z=y)$$
- There was no student who finishes every exam
$$\forall s \exists e \text{ Std}(s) \rightarrow [\text{exam}(e) \wedge \neg \text{finish}(s, e)]$$
- For every quiz, there is a student who finish it.”
$$\forall q \exists s \text{ Quiz}(q) \rightarrow [\text{Student}(s) \wedge \text{finish}(s, q)]$$
- Everyone has a favorite food.”
$$\forall x \exists y \text{ Person}(x) \rightarrow [\text{Food}(y) \wedge \text{Favorite}(y, x)]$$
- Every person likes every food.
$$\forall x \forall y [\text{Person}(x) \wedge \text{Food}(y)] \Rightarrow \text{Likes}(x, y)$$
- “There is a person who likes every food.”
$$\exists x \forall y \text{ Person}(x) \wedge [\text{Food}(y) \Rightarrow \text{Likes}(x, y)]$$

Q2) Put in the CNF Form B

a. $A \wedge B \Rightarrow C$

Ans: $\neg A \vee \neg B \vee C$

b. $\exists y \text{ course}(x) \wedge \text{std}(y) \Rightarrow \text{pass}(y, x)$

Ans: $\neg \text{course}(x) \vee \neg \text{std}(F(x)) \vee \text{pass}(F(x), x)$