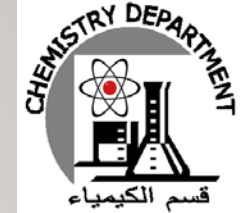




General Chemistry II

Chem 102



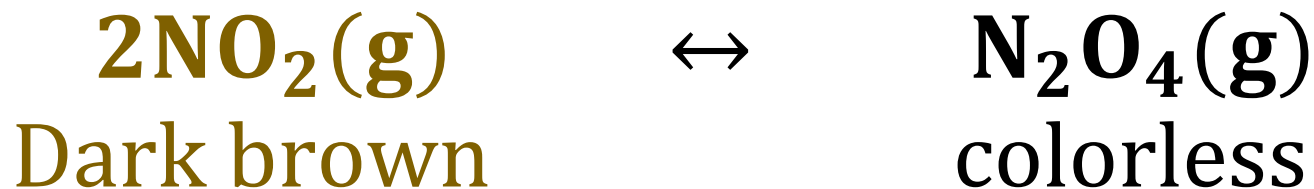
Lecture 9

Chemical Equilibrium

Ahmad Alakraa

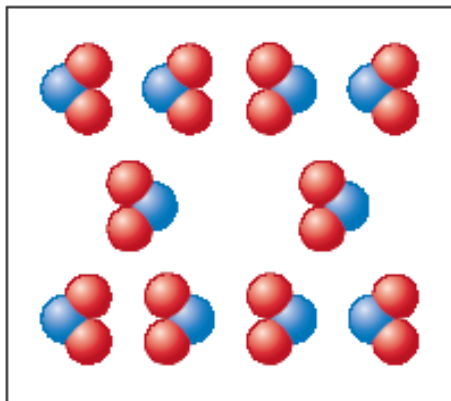
Meaning of equilibrium

- Reactions proceed either to **completion** or to **equilibrium**.

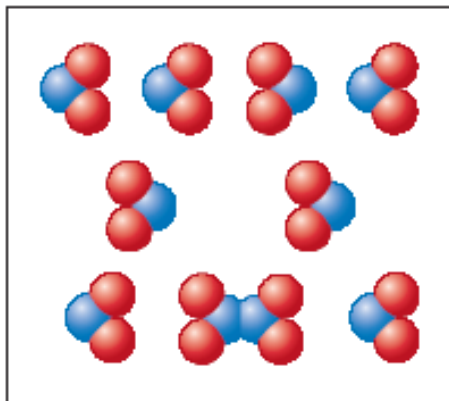


- When NO_2 is placed in an evacuated, sealed glass vessel at 25°C , the **intensity** of the **dark brown color decreases** with time but **does not become colorless**.
- Eventually**, the intensity of the brown color becomes constant, which means that the concentration of NO_2 is no longer changing.
- The system has reached **chemical equilibrium**, the state where the concentrations of all reactants and products remain **constant** with time.

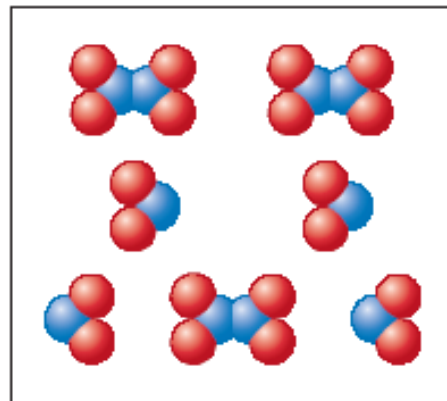
Dynamic not Static equilibrium



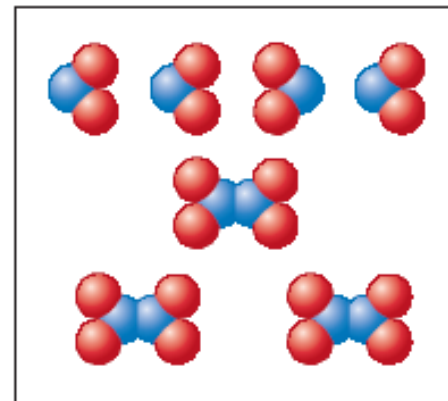
(a)



(b)



(c)



(d)

Time →

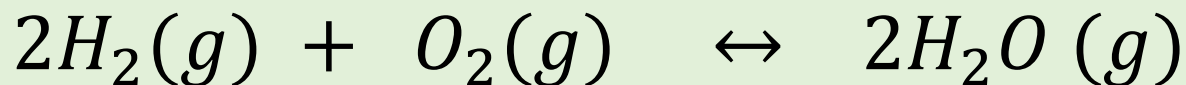


Numbers of NO_2 and N_2O_4 in the container become constant (c and d) after sufficient time has passed.

Equilibrium Position

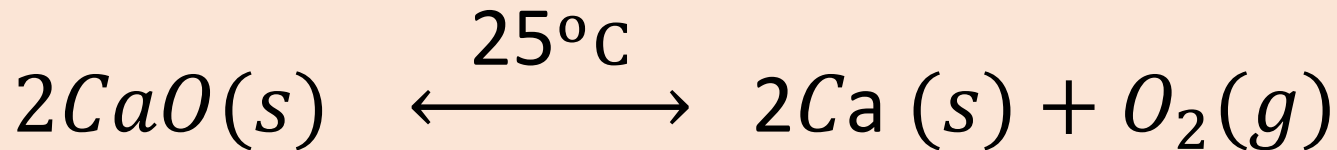
✚ Any chemical reactions carried out in a **closed vessel** will reach equilibrium.

✚ Some lies far to **right** (in the products direction)



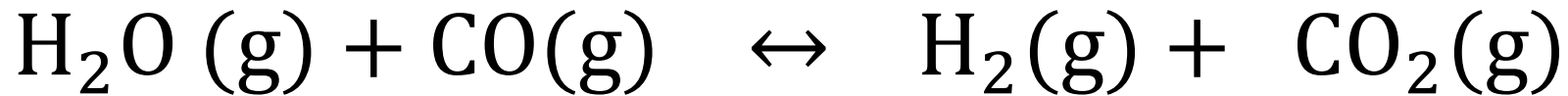
✓ The amounts of the reactants that remain when the system reaches equilibrium are so tiny as to be **negligible**.

✚ Some lies far to **left** (in the direction of the reactants)

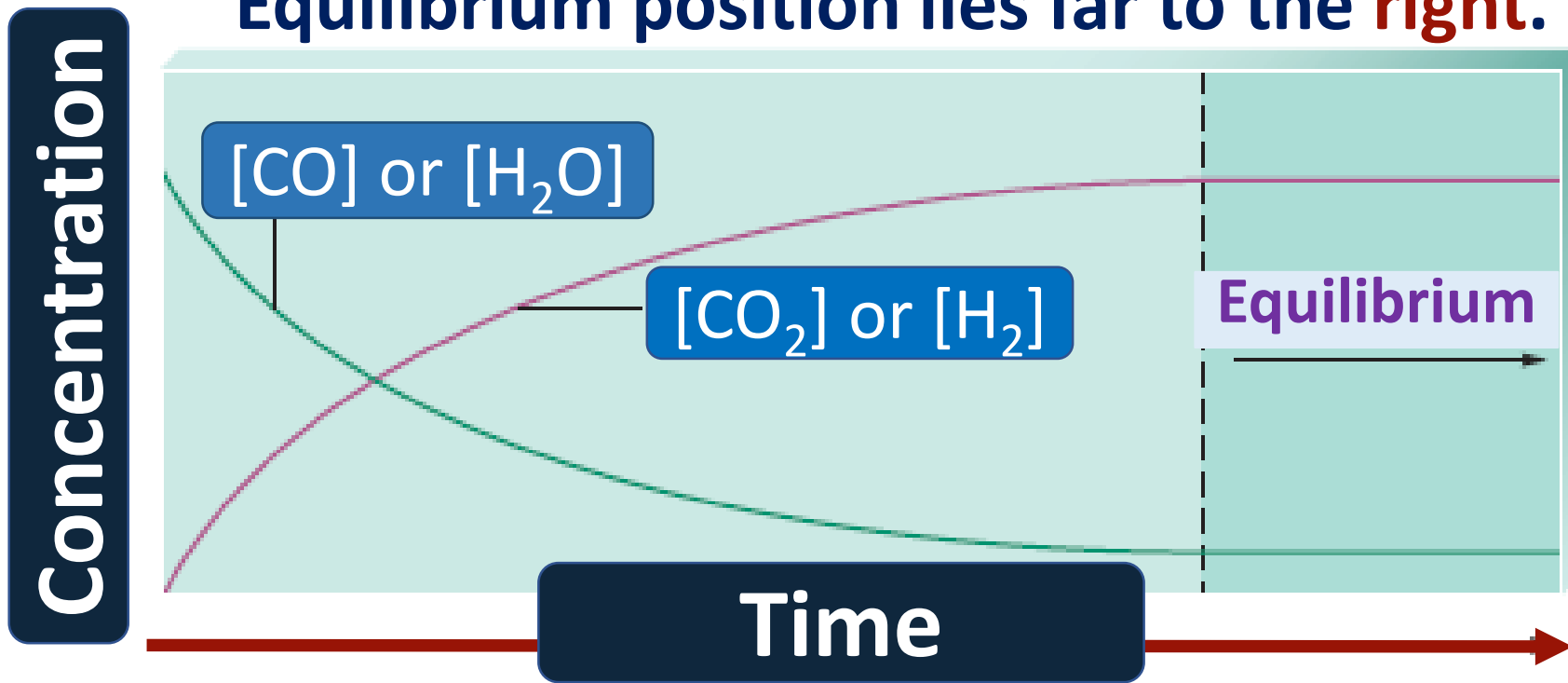


- ✓ Reactions occur only to a slight (**negligible**) extent.
- ✓ Decomposition to Ca (s) and O₂ (g) is virtually undetectable.

Concentration Profiles



Equilibrium position lies far to the **right**.



- Same **number of moles** of CO and H₂O are mixed.
- [CO] and [H₂O] are always equal. **Stoichiometry**
- [H₂] and [CO₂] are always equal.

Why equilibrium?

- ✚ Molecules react upon collision (Higher concentrations lead to more collisions and faster reactions).
- ✚ As the reaction proceeds, the reactants' concentration decreases and the rate of forward reaction decreases

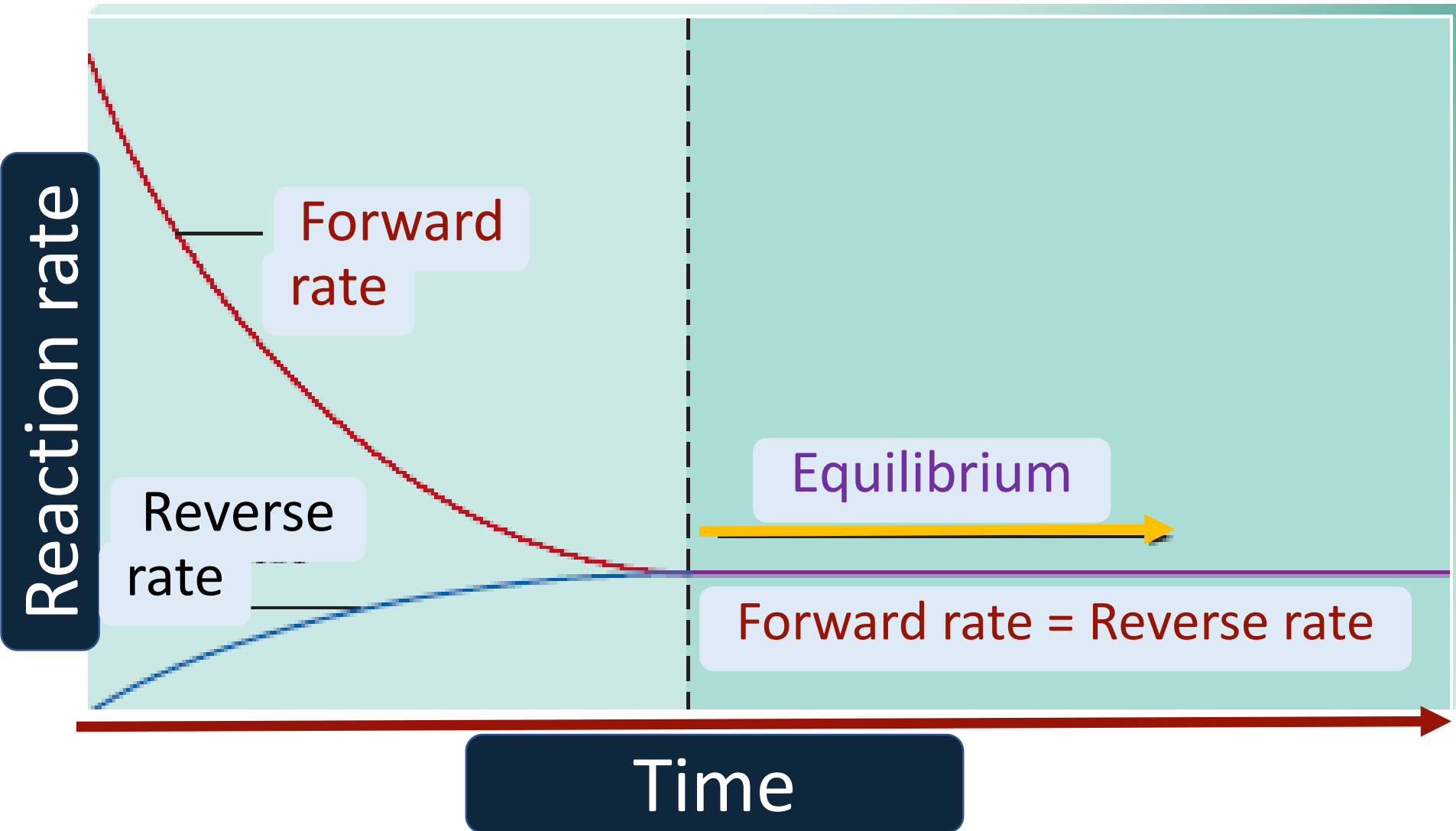
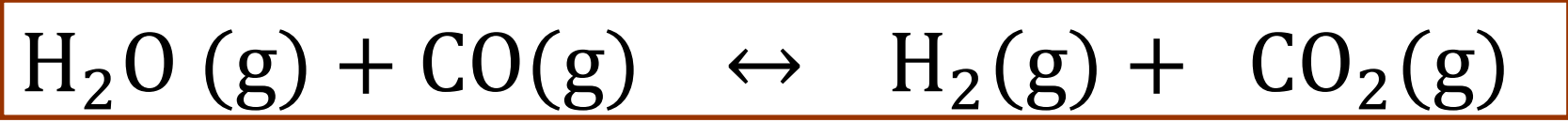


- ✚ Initially, there was neither H_2 nor CO_2 ; the rate of the reverse reaction was **zero**. **As the forward reaction proceeds**, the $[\text{H}_2]$ and $[\text{CO}_2]$ build up, and the rate of the reverse reaction increases.



- Eventually, the concentrations reach levels where the rates of forward and reverse reactions become equal . The system is in equilibrium.

Rate Profile



Equilibrium Position

The equilibrium position of a reaction—left, right, or somewhere in between—is determined by many factors:

- ✚ The initial **concentrations**,
- ✚ the relative **energies** of the reactants and products, and
- ✚ the relative degree of “**ordering**” of the reactants and products.

■ Reactions move in the direction achieving the **minimum energy and maximum disorder**.



Start/mol 1

3

0

- H_2 disappears three times as fast as N_2 .
- NH_3 forms twice as fast as N_2 disappears.

Equilibrium

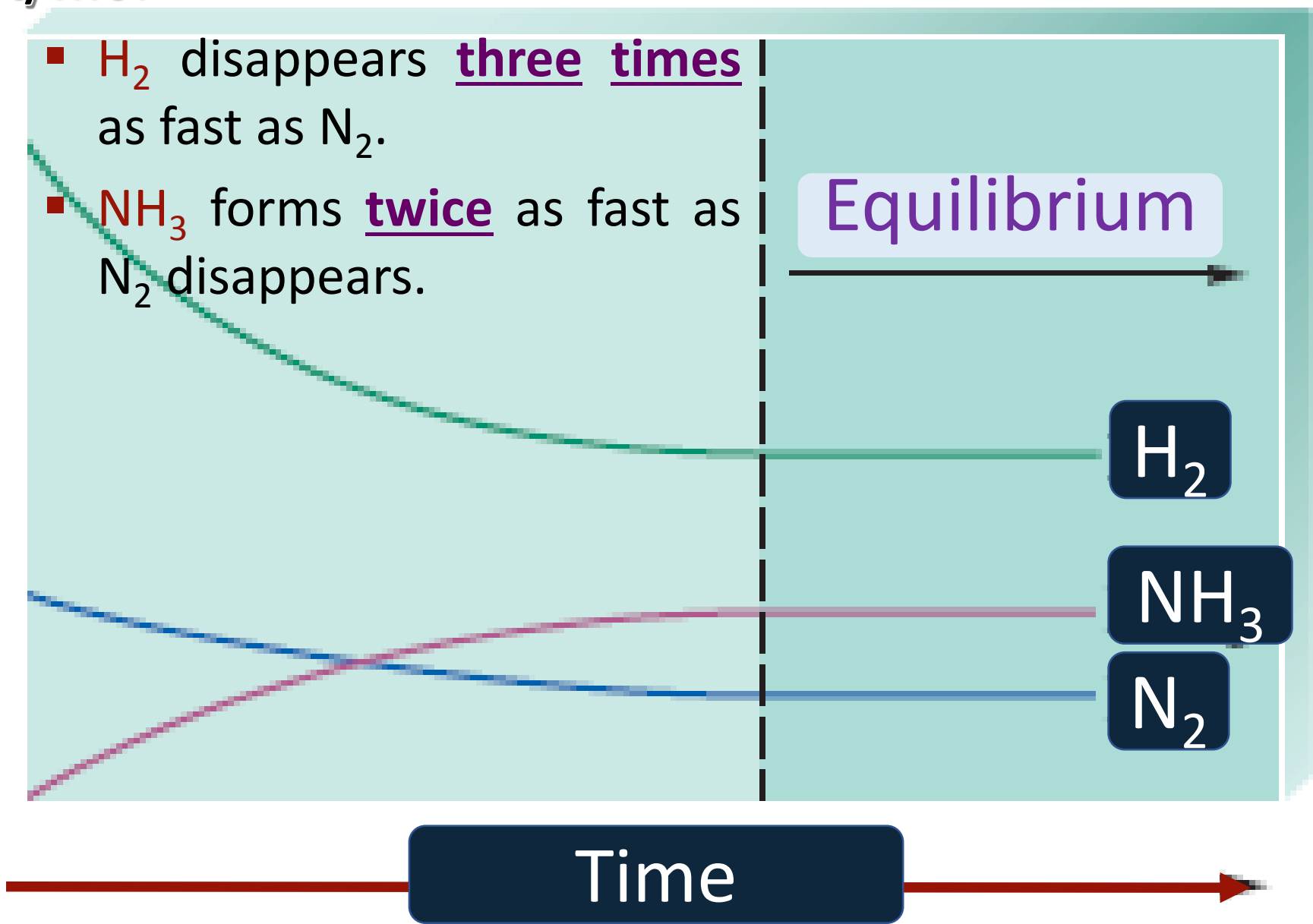
Concentration

H_2

NH_3

N_2

Time



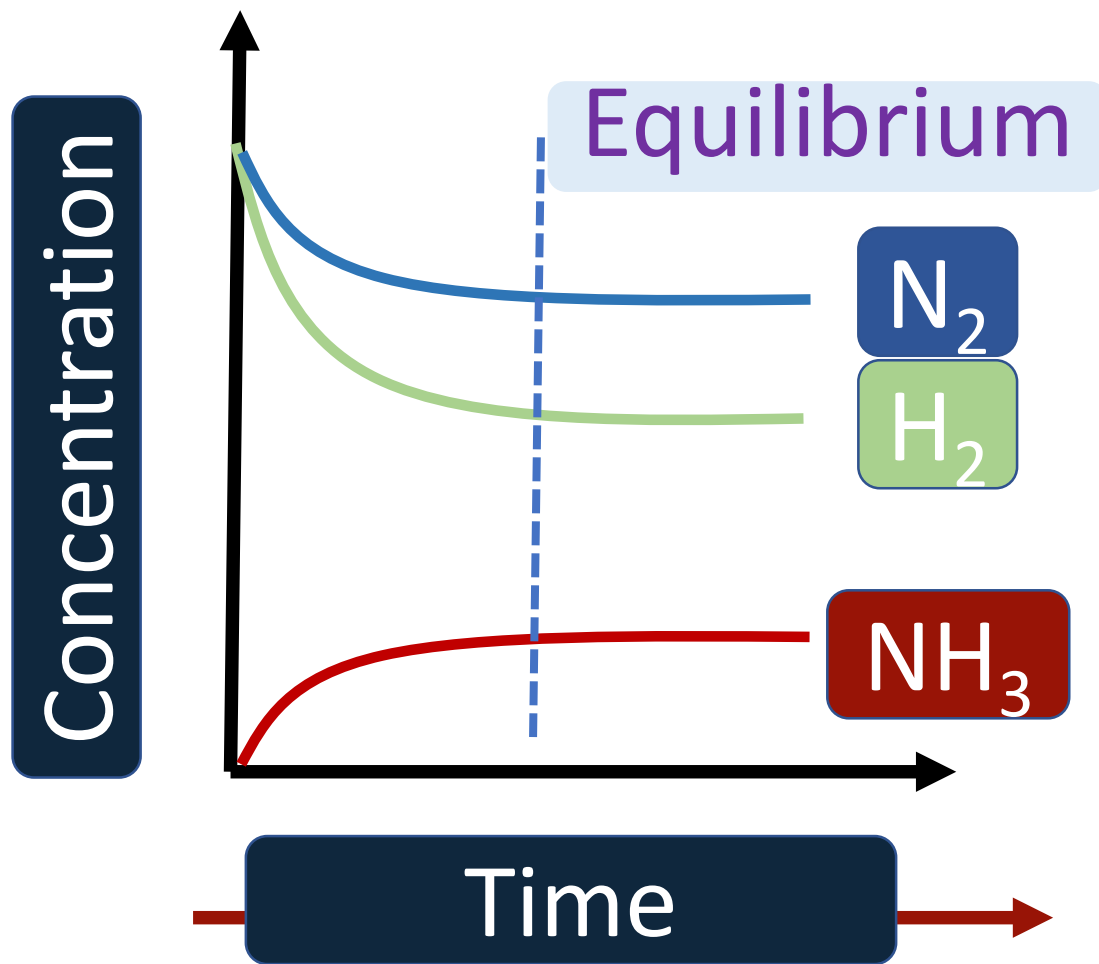


Start/mol

3

3

0



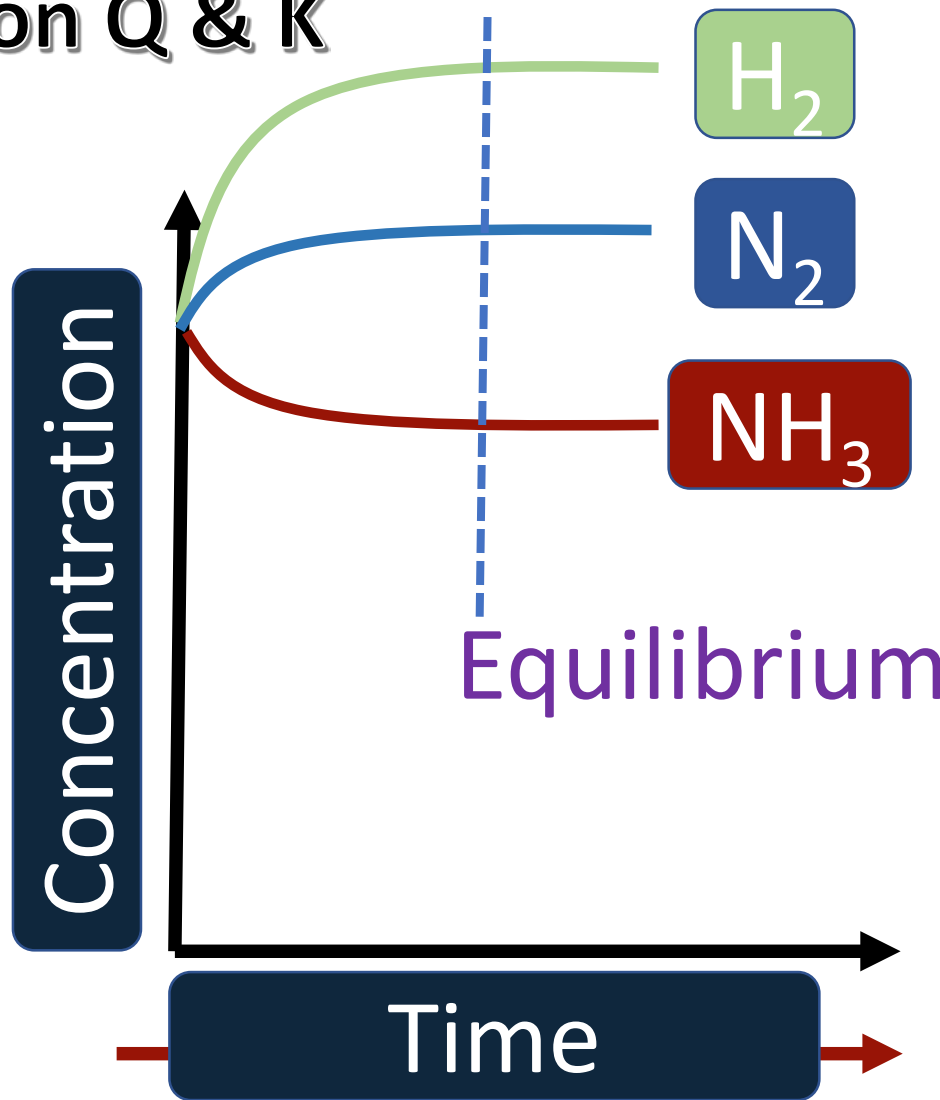
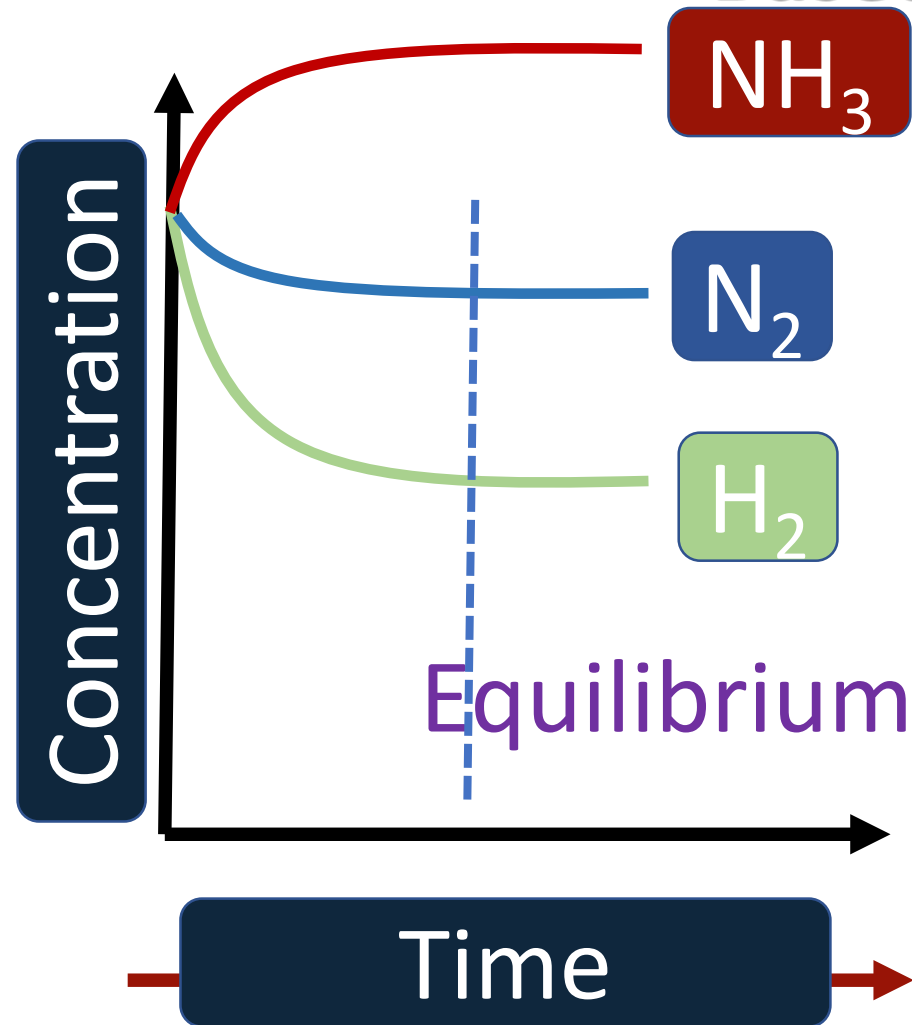


Start/mol 3

3

3

Based on Q & K





✚ When gaseous nitrogen, hydrogen, and ammonia are mixed in a closed vessel at 25°C, no apparent change in the concentrations occurs over time, regardless of the original amounts of the gases. Why?

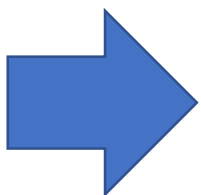
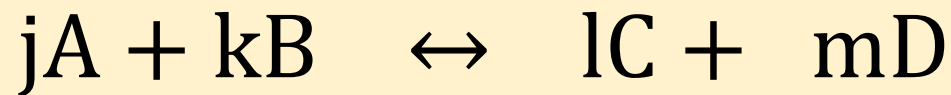
Possibly

- 1) The system is at chemical equilibrium.
- 2) The forward and reverse reactions are so **slow** that the system moves toward equilibrium at a rate that cannot be detected.

The second reason applies because of the **very strong bonds** in N_2 and H_2

Equilibrium Constant

✚ The law of **mass action** proposes this general equation at equilibrium:



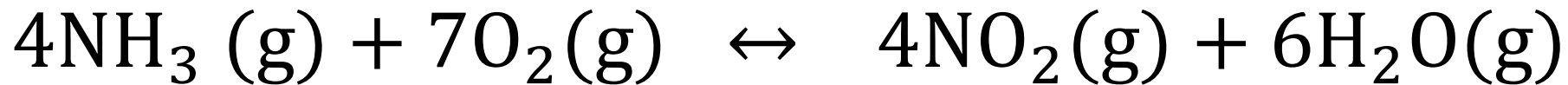
$$K = \frac{[C]^l [D]^m}{[A]^j [B]^k}$$

Where

- ✚ A, B, C and D represent chemical species.
- ✚ j, k, l and m are their coefficients in the balanced equation.
- ✚ The square brackets indicate the concentrations (**mol/L**) of the chemical species at equilibrium.
- ✚ K is the **equilibrium constant**.

Exercise

✚ Write the **equilibrium** expression for the following reaction:



Solution

$$K = \frac{[\text{NO}_2]^4 [\text{H}_2\text{O}]^6}{[\text{NH}_3]^4 [\text{O}_2]^7}$$

Note

K is customarily given without a unit due to corrections for the nonideal behavior of the substances taking part in the reaction. When these corrections are made, the units cancel out and the corrected K has no units. Thus we will not use units for K in this text.

Exercise

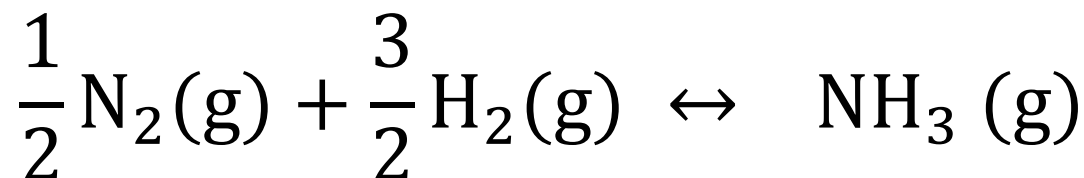
Haber Process

✚ The following equilibrium concentrations (mol/L) were observed for the Haber process for synthesis of ammonia at 127°C: $[\text{NH}_3] = 3.1 \times 10^{-2}$, $[\text{N}_2] = 8.5 \times 10^{-1}$, $[\text{H}_2] = 3.1 \times 10^{-3}$.

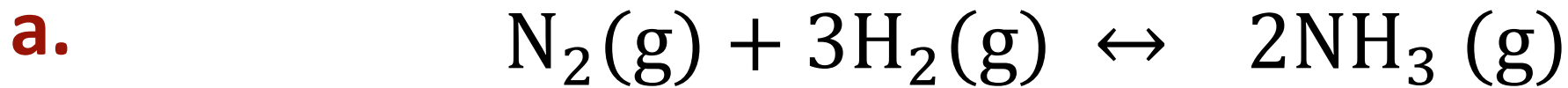
- Calculate the value of K at 127°C for this reaction?
- Calculate the value of the equilibrium constant at 127°C for the reaction?



- Calculate the value of the equilibrium constant at 127°C for the reaction given by the equation?



Solution



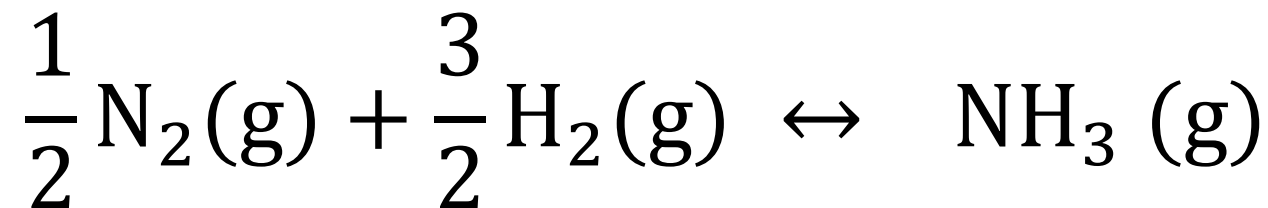
$$K = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3} = \frac{(3.1 \times 10^{-2})^2}{(8.5 \times 10^{-1})(3.1 \times 10^{-3})^3} = 3.8 \times 10^4$$

b. Rx is written in **reverse** order



$$K' = \frac{1}{K} = \frac{[\text{N}_2][\text{H}_2]^3}{[\text{NH}_3]^2} = \frac{1}{3.8 \times 10^4} = 2.6 \times 10^{-5}$$

c. Rx is multiplied by a **factor**



$$K'' = \frac{[\text{NH}_3]}{[\text{N}_2]^{1/2} [\text{H}_2]^{3/2}} = \left(\frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3} \right)^{1/2}$$

$$= K^{1/2} = (3.8 \times 10^4)^{1/2}$$

$$= 1.9 \times 10^2$$

Generally,

For a reaction $jA + kB \leftrightarrow lC + mD$

→
$$K = \frac{[C]^l [D]^m}{[A]^j [B]^k}$$

For a reverse reaction $lC + mD \leftrightarrow jA + kB$

→
$$K' = \frac{1}{K} = \frac{[A]^j [B]^k}{[C]^l [D]^m}$$

Multiplying in a factor n $n l C + n m D \leftrightarrow n j A + n k B$

→
$$K'' = K^n = \frac{[C]^{nl} [D]^{nm}}{[A]^{nj} [B]^{nk}} = \left(\frac{[C]^l [D]^m}{[A]^j [B]^k} \right)^n$$

Adding 2 or more equations

If two equations are added, the equilibrium constant for the reaction is the product of the equilibrium constants of the equations added.

Example

Calculate K for $2\text{NO}(\text{g}) + \text{Br}_2(\text{g}) \leftrightarrow 2\text{NOBr}(\text{g})$ using the following information.

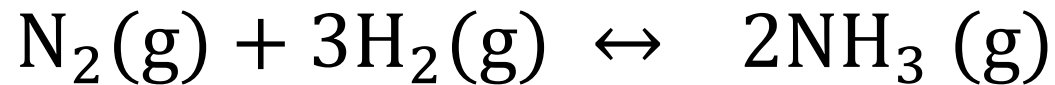


Answer  Add equations

$$K = K_1 K_2 = 1.0 \times 10^{30} \times 2.0 \times 10^{-27} = 2.0 \times 10^3$$

Equilibrium Position

For a Rx at 500 °C



$$K = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3} = 6.0 \times 10^{-2}$$

- Whenever N_2 , H_2 , and NH_3 are mixed together at 500 °C, system will reach an equilibrium position such that $K = 6.0 \times 10^{-2}$, **regardless** of the amounts of the gases that are mixed together initially.
- The **equilibrium concentrations** will not always be the same but influenced by the initial concentrations mixed.
- Each set of equilibrium concentrations is called an **equilibrium position**.



$$K = \frac{[\text{NH}_3]^2}{[\text{N}_2][\text{H}_2]^3} = 6.0 \times 10^{-2}$$

Exp.	Initial Conc./M	Eq. Conc./M	K
1	$[\text{N}_2]_0 = 1.000$	$[\text{N}_2] = 0.921$	6.02×10^{-2}
	$[\text{H}_2]_0 = 1.000$	$[\text{H}_2] = 0.763$	
	$[\text{NH}_3]_0 = 0$	$[\text{NH}_3] = 0.157$	
2	$[\text{N}_2]_0 = 0$	$[\text{N}_2] = 0.399$	6.02×10^{-2}
	$[\text{H}_2]_0 = 0$	$[\text{H}_2] = 1.197$	
	$[\text{NH}_3]_0 = 1.000$	$[\text{NH}_3] = 0.203$	
3	$[\text{N}_2]_0 = 2.000$	$[\text{N}_2] = 2.59$	6.02×10^{-2}
	$[\text{H}_2]_0 = 1.000$	$[\text{H}_2] = 2.77$	
	$[\text{NH}_3]_0 = 3.000$	$[\text{NH}_3] = 1.82$	

Note

- There is only **one** equilibrium constant for a particular system at a **particular temperature**, but there are an **infinite** number of equilibrium positions.
- The specific **equilibrium position** adopted by a system **depends** on the **initial concentrations**, but the **equilibrium constant** does not.

Equilibrium_Pressure

For gases reactions

C: mol/L

$$PV = nRT$$



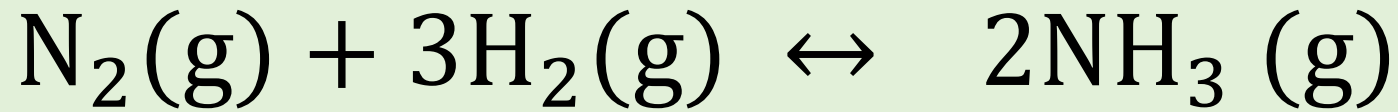
$$P = \frac{n}{V} RT$$



$$P = CRT$$

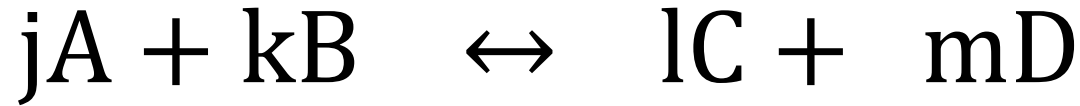
Ammonia Synthesis





$$\begin{aligned} K_C = K &= \frac{C_{\text{NH}_3}^2}{C_{\text{N}_2} C_{\text{H}_2}^3} = \frac{\left(\frac{P_{\text{NH}_3}}{RT}\right)^2}{\left(\frac{P_{\text{N}_2}}{RT}\right) \left(\frac{P_{\text{H}_2}}{RT}\right)^3} \\ &= \left(\frac{P_{\text{NH}_3}^2}{P_{\text{N}_2} P_{\text{H}_2}^3}\right) (RT)^2 = K_P (RT)^2 \end{aligned}$$

Generally, for the following gaseous reaction



$$K = K_p (RT)^{-\Delta n}$$

Or

$$K_p = K(RT)^{\Delta n}$$

where

$$\Delta n = (l + m) - (j + k)$$

Gaseous reactants and products are only involved

Exercise

Using the value of $K_p = 1.9 \times 10^3$, calculate the value of K at 25°C for the reaction



Solution

$$\Delta n = (2) - (2 + 1) = -1$$

$$K = K_p (RT)^{-\Delta n} =$$

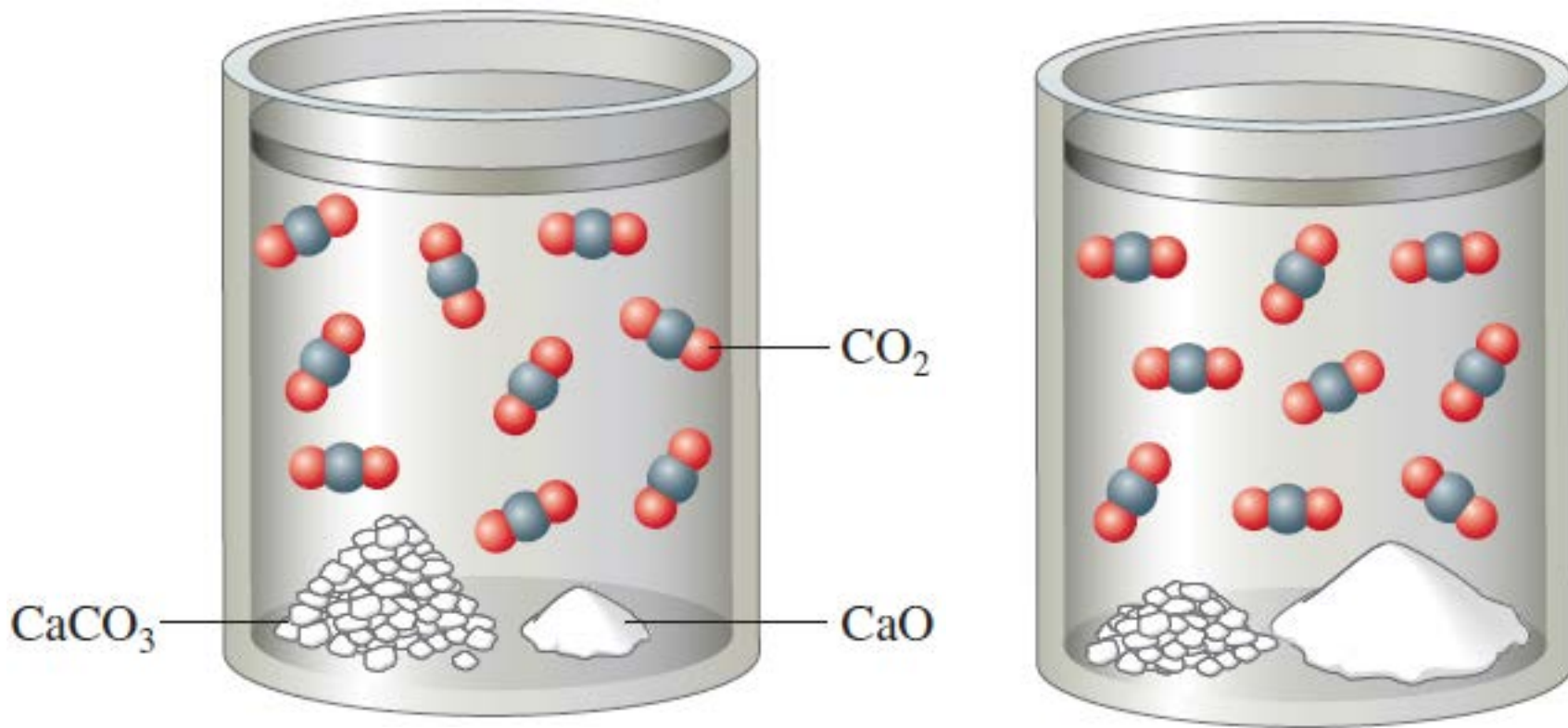
$$(1.9 \times 10^3)(0.08206 \times 298) = 4.6 \times 10^4$$

Heterogeneous Equilibria



- ✚ **Experimental** results show that the position of a heterogeneous equilibrium does not depend on the amounts of pure solids or liquids (changed a little).
- ✚ If pure solids or liquids are involved in a chemical reaction, their concentrations are not included in the equilibrium expression for the reaction.

$$K = [\text{CO}_2]$$



The position of the equilibrium

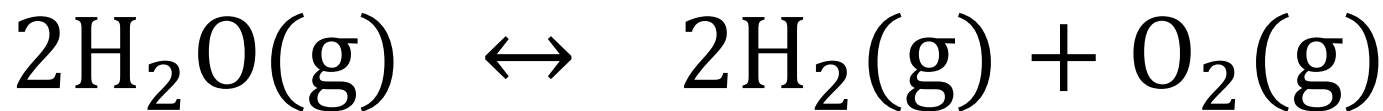


does not depend on the amounts of $\text{CaCO}_3(\text{s})$ and $\text{CaO}(\text{s})$ present.



$$K = [\text{H}_2]^2 [\text{O}_2]$$

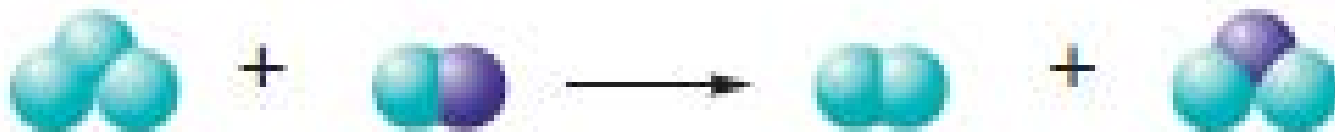
$$K_P = (P_{\text{H}_2}^2)(P_{\text{O}_2})$$



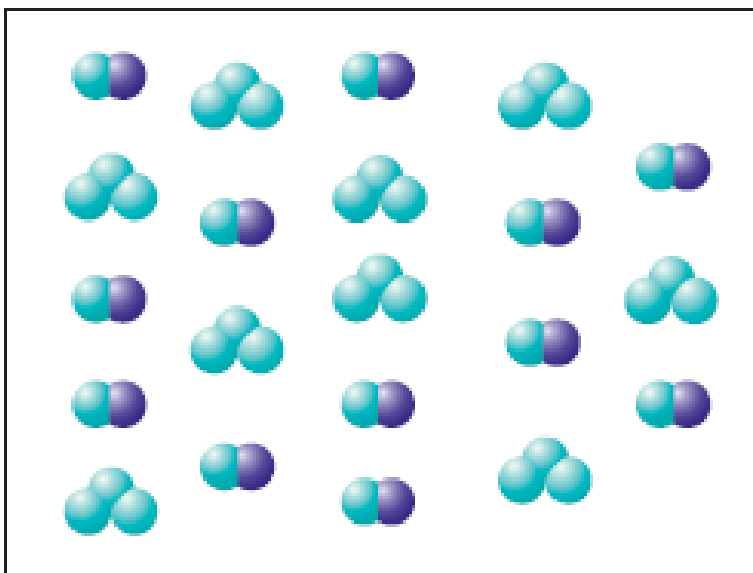
$$K = \frac{[\text{H}_2]^2 [\text{O}_2]}{[\text{H}_2\text{O}]^2}$$

$$K_P = \frac{(P_{\text{H}_2}^2)(P_{\text{O}_2})}{(P_{\text{H}_2\text{O}}^2)}$$

Consider

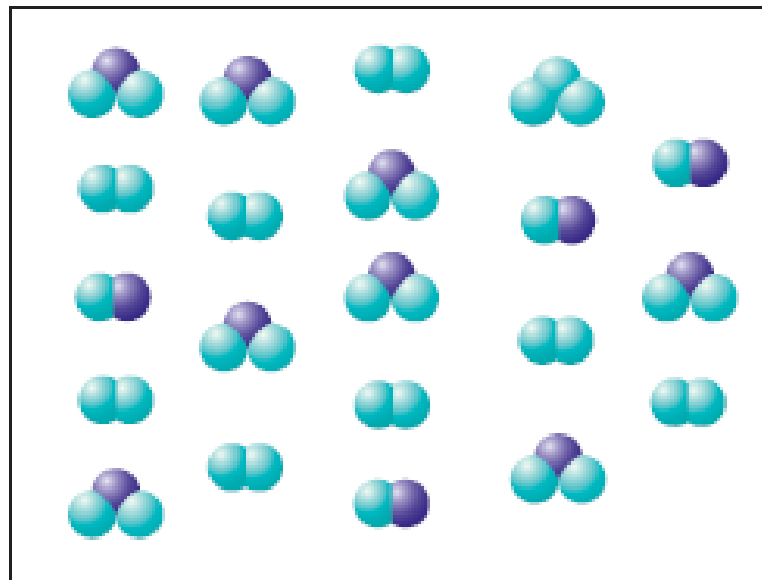


where  and  represent two different types of atoms.



A=9, B=12, C=D=0

Initially











A=1, B=4, C=D=8

Equilibrium





$$\frac{(N_{\text{AB}})(N_{\text{C}_2})}{(N_{\text{A}_2})(N_{\text{BC}})} = 16 = \frac{(x)(x)}{(9-x)(12-x)}$$

Initial Conditions

9  molecules
 12  molecules
 0  molecules
 0  molecules

x  disappear
 x  disappear
 x  form
 x  form

Equilibrium Conditions

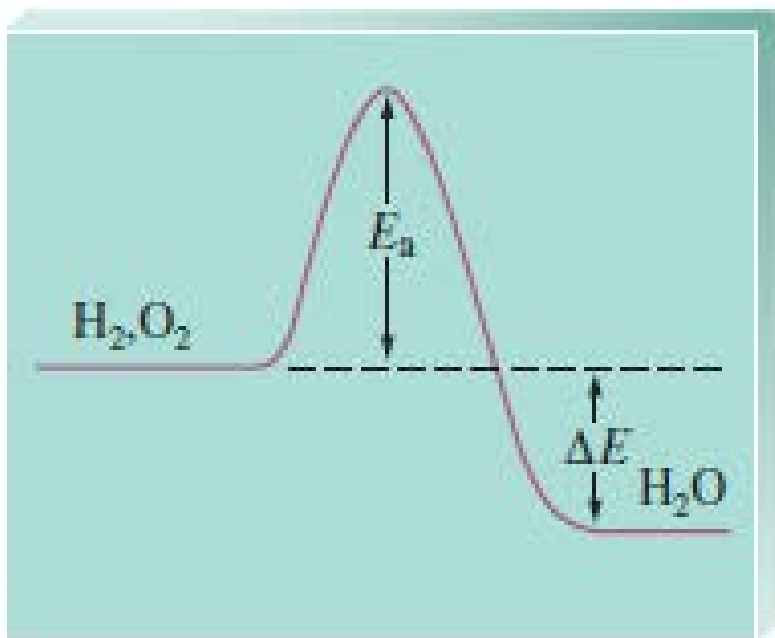
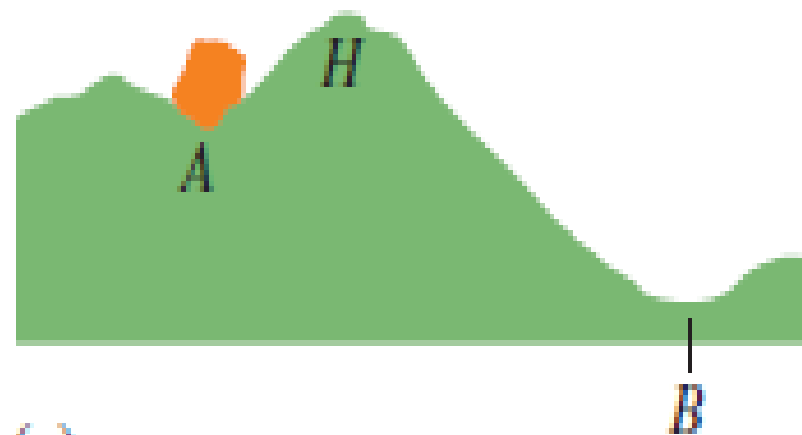
$9 - x$  molecules
 $12 - x$  molecules
 x  molecules
 x  molecules

$x = 8$

Equilibrium: thermodynamics & Kinetics

- ✚ The size of K (**thermodynamics parameter**) and the time (**Kinetic parameter** depending on **activation energy**) required to reach equilibrium **are not** directly related.
- ✚ The size of K is determined by thermodynamic factors such as the difference in energy between products and reactants.
- ✚ Reactions having K much larger than 1 will have their equilibria **lying to the right** — the reaction system will consist mostly of products. The extreme of these reactions is to go almost to completion.
- ✚ Reactions having very small K values will have their equilibria **lying to the left** — the reaction system will consist mostly of reactants.

Reaction Extent



- The reactants H_2 and O_2 have a strong tendency to form H_2O .
- That is, H_2O has lower energy than H_2 and O_2 .
- However, the large activation energy E_a prevents the reaction at 25°C .
- In other words, the magnitude of K for the reaction depends on ΔE , but the reaction rate depends on E_a .

Reaction Quotient, Q

✚ It applies the law of mass action for initial concentrations

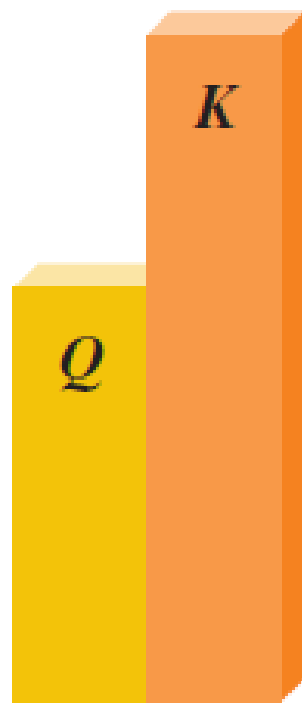


$$Q = \frac{[\text{NH}_3]_0^2}{[\text{N}_2]_0 [\text{H}_2]_0^3}$$

Q/K

- 1) Q is equal to K. The system is at equilibrium; no shift will occur.
- 2) Q is greater than K. To reach equilibrium, a net change of products to reactants must occur. The system shifts to the left, consuming products and forming reactants, until equilibrium is achieved.
- 3) Q is less than K. The system must shift to the right, consuming reactants and forming products, to attain equilibrium.

System has too much reactant

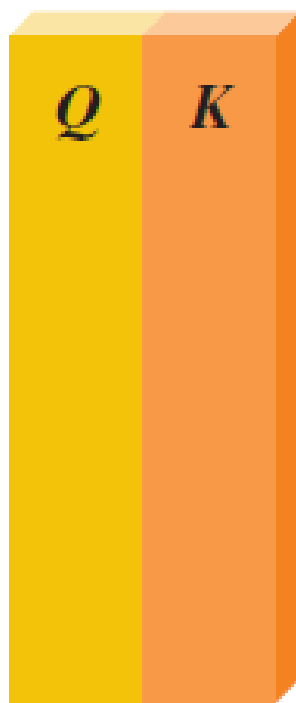


$$Q < K$$

Shift reaction to the right



System is at equilibrium

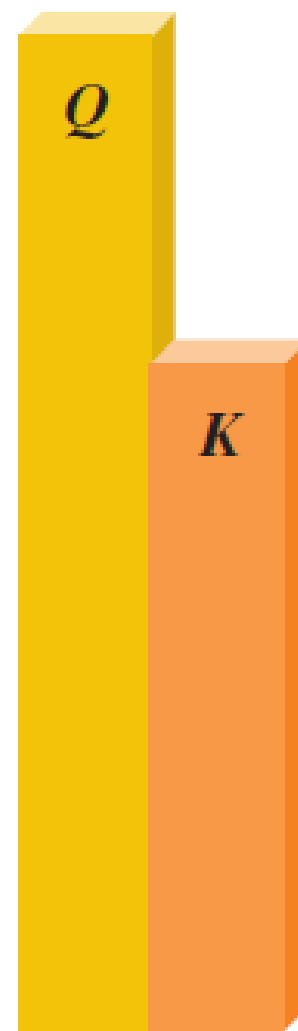


$$Q = K$$

Shift reaction to the left



System has too much product



$$Q > K$$

Exercise

✚ For the synthesis of ammonia at 500°C, $K = 6.0 \times 10^{-2}$. Predict the direction in which the system will shift to reach equilibrium in each of the following cases:

a

$$[N_2]_0 = 1.0 \times 10^{-5} \text{ M}$$
$$[H_2]_0 = 2.0 \times 10^{-3} \text{ M}$$
$$[NH_3]_0 = 1.0 \times 10^{-3} \text{ M}$$

b

$$[N_2]_0 = 1.5 \times 10^{-5} \text{ M}$$
$$[H_2]_0 = 3.54 \times 10^{-1} \text{ M}$$
$$[NH_3]_0 = 2.0 \times 10^{-4} \text{ M}$$

c

$$[N_2]_0 = 5 \text{ M}$$
$$[H_2]_0 = 1.0 \times 10^{-2} \text{ M}$$
$$[NH_3]_0 = 1.0 \times 10^{-4} \text{ M}$$

Solution



$$Q = \frac{[\text{NH}_3]_0^2}{[\text{N}_2]_0[\text{H}_2]_0^3} = \frac{(1.0 \times 10^{-3})^2}{(1.0 \times 10^{-5})(2.0 \times 10^{-3})^3}$$
$$= 1.3 \times 10^7 \gg \gg K$$

System shifts to left



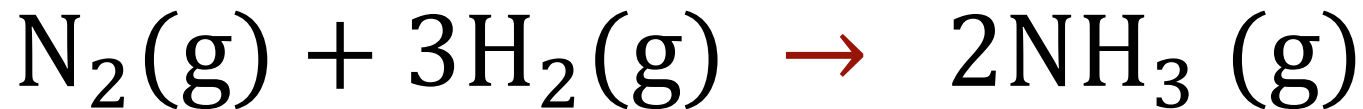
$$Q = \frac{[\text{NH}_3]_0^2}{[\text{N}_2]_0[\text{H}_2]_0^3} = \frac{(2.0 \times 10^{-4})^2}{(1.5 \times 10^{-5})(3.54 \times 10^{-1})^3}$$
$$= 6.01 \times 10^{-2} = K$$

System at equilibrium



$$Q = \frac{[\text{NH}_3]_0^2}{[\text{N}_2]_0[\text{H}_2]_0^3} = \frac{(1.0 \times 10^{-4})^2}{(5)(1.0 \times 10^{-2})^3}$$
$$= 2.0 \times 10^{-3} \lll K$$

System shifts to right



Solving Eq. Problems

- ✚ Write the **balanced** equation for the reaction.
- ✚ Write the **equilibrium expression** using the law of mass action.
- ✚ List the **initial** concentrations.
- ✚ **Calculate Q**, and determine the **direction** of the shift to equilibrium.
- ✚ Define the **change needed** to reach equilibrium, and define the equilibrium concentrations by applying the change to the initial concentrations.
- ✚ Substitute the equilibrium concentrations into the equilibrium expression, and **solve for the unknown**.
- ✚ **Check** your calculated equilibrium concentrations by making sure they give the correct value of K.

Exercise

Carbon monoxide reacts with steam to produce carbon dioxide and hydrogen. At 700 K the equilibrium constant is 5.10. Calculate the equilibrium concentrations of all species if 1.000 mole of each component is mixed in a 1.000-L flask.

Solution



$$K = \frac{[\text{CO}_2][\text{H}_2]}{[\text{CO}][\text{H}_2\text{O}]} = 5.10$$

$$[\text{CO}]_0 = [\text{H}_2\text{O}]_0 = [\text{CO}_2]_0 = [\text{H}_2]_0 = \frac{1.0\text{mol}}{1.0\text{L}} = 1.0\text{M}$$

$$Q = \frac{[\text{CO}_2]_0[\text{H}_2]_0}{[\text{CO}]_0[\text{H}_2\text{O}]_0} = \frac{(1.0\text{mol/L})(1.0\text{mol/L})}{(1.0\text{mol/L})(1.0\text{mol/L})} = 1.0$$

$Q \ll K$

Rx shifts to right

Initial Conc. (mol/L)	Change (mol/L)	Eq. Conc. (mol/L)
$[\text{CO}]_0 = 1.0$	$-x$	$1.0 - x$
$[\text{H}_2\text{O}]_0 = 1.0$	$-x$	$1.0 - x$
$[\text{CO}_2]_0 = 1.0$	$+x$	$1.0 + x$
$[\text{H}_2]_0 = 1.0$	$+x$	$1.0 + x$

$$K = \frac{[\text{CO}_2][\text{H}_2]}{[\text{CO}][\text{H}_2\text{O}]} = 5.10$$
$$= \frac{(1.0 + x)(1.0 + x)}{(1.0 - x)(1.0 - x)} = \frac{(1.0 + x)^2}{(1.0 - x)^2}$$

$$\sqrt{5.10} = \frac{(1.0 + x)}{(1.0 - x)} \quad x = 0.387 \text{ mol/L}$$

Eq. Conc.

$$[\text{CO}] = [\text{H}_2\text{O}] = (1.0 - x) = 0.613 \text{ M}$$



$$[\text{CO}_2] = [\text{H}_2] = (1.0 + x) = 1.387 \text{ M}$$

Exercise

Assume that the reaction for the formation of gaseous hydrogen fluoride from hydrogen and fluorine has an equilibrium constant of 1.15×10^2 at a certain temperature. In a particular experiment, 3.000 moles of each component was added to a 1.500-L flask. Calculate the equilibrium concentrations of all species?

Solution

Solving a quadratic equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Exercise

Assume that gaseous hydrogen iodide is synthesized from hydrogen gas and iodine vapor at a temperature where the equilibrium constant, K_p , is 1.00×10^2 . Suppose HI at 5.000×10^{-1} atm, H_2 at 1.000×10^{-2} atm, and I_2 at 5.000×10^{-3} atm are mixed in a 5.000-L flask. Calculate the equilibrium pressures of all species.

Solution



$$K_p = \frac{(P_{HI})^2}{(P_{H_2})(P_{I_2})} = 1.0 \times 10^2$$

$$P_{HI}^0 = 5.0 \times 10^{-1} \text{ atm}, \quad P_{H_2}^0 = 1.0 \times 10^{-2} \text{ atm}$$

,

$$P_{I_2}^0 = 5.0 \times 10^{-3} \text{ atm}$$

$$Q_P = \frac{(P_{\text{HI}}^0)^2}{(P_{\text{H}_2}^0)(P_{\text{I}_2}^0)} =$$

$$Q \gg K$$

System shifts to left

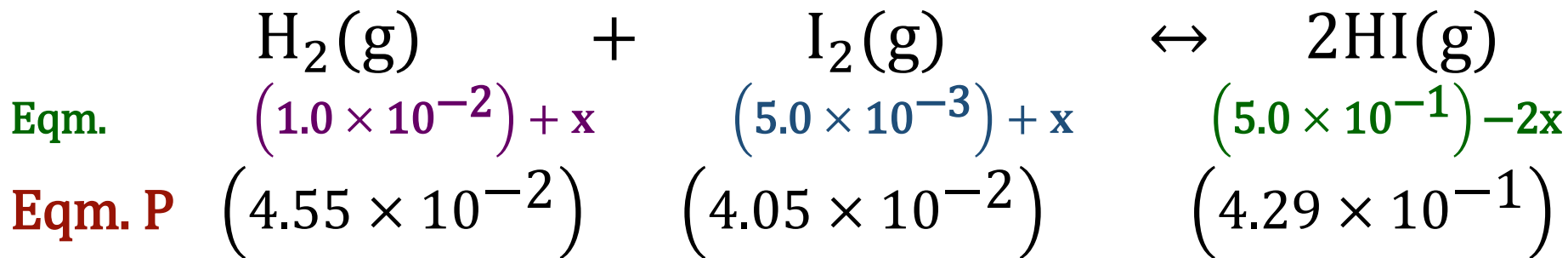
$$\frac{(5.0 \times 10^{-1} \text{ atm})^2}{(1.0 \times 10^{-2} \text{ atm})(5.0 \times 10^{-3} \text{ atm})} = 5.0 \times 10^3$$

	$\text{H}_2(\text{g})$	+	$\text{I}_2(\text{g})$	\leftarrow	$2\text{HI}(\text{g})$
Initial	1.0×10^{-2}		5.0×10^{-3}		5.0×10^{-1}
Change	+ x		+ x		-2x
Eqm.	$(1.0 \times 10^{-2}) + x$		$(5.0 \times 10^{-3}) + x$		$(5.0 \times 10^{-1}) - 2x$

$$K_P = \frac{(P_{\text{HI}})^2}{(P_{\text{H}_2})(P_{\text{I}_2})} = \frac{(5.0 \times 10^{-1} - 2x)^2}{(1.0 \times 10^{-2} + x)(5.0 \times 10^{-3} + x)} = 1.0 \times 10^2$$

$$9.6 \times 10^1 x^2 + 3.5x - (2.45 \times 10^{-1}) = 0$$

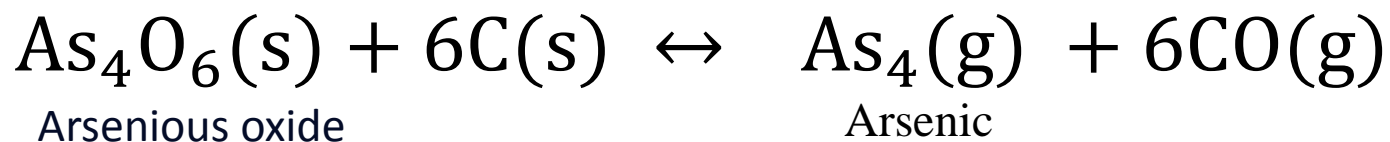
$$x = 3.55 \times 10^{-2}$$



Le Châtelier's principle

“if a change is imposed on a system at equilibrium, the position of the equilibrium will shift in a direction that tends to reduce that change”.

Exercise



Predict the direction the Rx should shift to attain an equilibrium position in case of:

- a. Addition of carbon monoxide (Left)
- b. Addition or removal of carbon or tetraarsenic hexoxide (As_4O_6)

Since the amount of a pure solid has no effect on the equilibrium position, changing the amount of carbon or tetraarsenic hexoxide will have no effect.

- c. Removal of gaseous arsenic (As_4) (Right)

Effect of Changing Pressure

There are three ways to change the pressure of a reaction system involving gaseous components:

- 1) Add or remove a gaseous reactant or product.
(previously considered)
- 2) Add an inert gas (one not involved in the reaction). That will increase the total pressure but has no effect on the concentrations or partial pressures of the reactants or products. The added molecules do not participate in the reaction in any way and thus cannot affect the equilibrium in any way. Thus the system remains at the original equilibrium position.

3) Change the volume of the container.

- When the volume of the container is changed, the concentrations (and thus the partial pressures) of both reactants and products are changed. We could calculate Q and predict the direction of the shift.

For systems involving gaseous components, We focus on the vessel volume (V).

- ✓ If V is reduced, the system responds by reducing its own volume. This is done by **decreasing the total number of gaseous molecules in the system.** $V \propto n$
- ✓ When the container volume is increased, the system will shift so as to increase its volume.

Changing Reaction Volume

For this Rx,

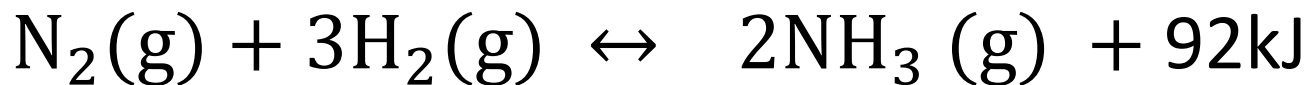


- If we suddenly reduce the volume, the reaction system can reduce its volume by reducing the number of molecules present. This means that the reaction will shift to the right.

Effect of Changing Temperature

Changing the temperature affects both the equilibrium position and equilibrium constants.

For exothermic Rx,



- Increasing T shifts the Rx to left, K decreases
- Decreasing T shifts the Rx to right, K increases

For endothermic Rx,



- Increasing T shifts the Rx to right, K increases
- Decreasing T shifts the Rx to left, K decreases